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WASTE HEAT UTILIZATION FROM A DIRECT  
CYCLE HIGH TEMPERATURE GAS COOLED NUCLEAR  
REACTOR FOR DISTRICT HEATING AND AIR CONDITIONING

BY

JOHN JOSEPH BLASE, 1947-

A THESIS

Presented to the Faculty of the Graduate School of the

UNIVERSITY OF MISSOURI-ROLLA

In Partial Fulfillment of the Requirements for the Degree

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D. Ray Edwards (Advisor) J. Wilson

Denny A. Wiebe A. Tsoufanidis

## ABSTRACT

An analysis was conducted to determine the economic as well as technical feasibility of waste heat utilization from the proposed direct cycle high temperature gas cooled nuclear reactor, as designed by the General Atomic Company.

The rejected heat from this system is at considerably higher temperatures than those normally encountered in conventional steam-electric Rankine cycles. By taking advantage of these higher rejection temperatures, heat was translated into energy available to a district heating and air conditioning service. The transportation of this energy was considered to be in the form of heated and chilled water.

A refrigeration capacity on the order of 100,000 Tons and a heating capability of  $5.0 \times 10^9$  BTU/hr at a distance of 70 miles was found to be a possibility.

An economic analysis using a discounted cash flow technique, indicated that most of the systems analyzed could be profitable ventures. During the operation of the district heating and air conditioning network, overall utilization of the total reactor heat generation would be in excess of 80.0 per cent.

## ACKNOWLEDGEMENT

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## TABLE OF CONTENTS

	Page
ABSTRACT. . . . .	ii
ACKNOWLEDGEMENT . . . . .	iii
LIST OF ILLUSTRATIONS . . . . .	vi
LIST OF TABLES. . . . .	viii
I . INTRODUCTION. . . . .	1
II . METHOD. . . . .	2
II.A. Outline of Procedure . . . . .	2
II.B. The Motive Energy Source . . . . .	3
II.B.1. Thermal balance on the precooler section to determine the steam available to the refrigeration units . . . . .	5
II.C. 40°F Water Available to the System . . . . .	8
II.C.1. Description of the cycle. . . . .	8
II.C.2. Refrigeration available at the plant site. . . . .	10
II.C.3. Cooling water available to the pipeline. . . . .	13
II.D. 200°F Water Available to the System. . . . .	14
III . HEAT TRANSFER AND PRESSURE DROP CALCULATIONS. . . . .	16
III.A. Pipeline Pressure Drop Calculations. . . . .	16
III.A.1. Pressure drop per mile of pipe. . . . .	17
III.A.2. Horsepower required per mile. . . . .	17

## TABLE OF CONTENTS (cont.)

	Page
III.B. Pipeline Heat Transfer Calculations. . . . .	18
III.C. Energy Available at the Load Center. . . . .	22
III.D. Demonstration of Method. . . . .	24
III.D.1. Program input . . . . .	24
III.E. Results. . . . .	25
IV . CASH FLOW ANALYSIS. . . . .	35
IV.A. Procedure. . . . .	35
IV.A.1. Rates . . . . .	36
IV.A.2. Example cash flow . . . . .	36
IV.A.3. Depreciation scheme . . . . .	38
IV.A.4. Income tax calculations . . . . .	38
IV.A.5. Net cash flow . . . . .	39
IV.B. Results of the Cash Flow Analysis. . . . .	44
V . DISCUSSION OF RESULTS . . . . .	52
VI. CONCLUSIONS . . . . .	55
BIBLIOGRAPHY. . . . .	56
VITA. . . . .	58
APPENDICES. . . . .	59
A. REVIEW OF LITERATURE . . . . .	59
B. FORTRAN IV COMPUTER PROGRAM LISTING. . . . .	62
C. COMPUTER PROGRAM FLOW CHART. . . . .	78
D. SAMPLE CASH FLOW PROBLEM . . . . .	83

## LIST OF ILLUSTRATIONS

Figure	Page
1.0. Direct Cycle High Temperature Gas Cooled Reactor.....	4
2.0. Precooler as Steam Generator.....	5
3.0. Schematic of the Steam Jet Cycle.....	9
4.0. Steam Jet Cycle Parameters.....	12
5.0. Cooling Unit Thermal Balance.....	13
6.0. Thermal Balance for Heating System.....	14
7.0. Pipeline Schematic.....	18
8.0. Cross Section of an Insulated Buried Pipe.....	20
9.0. Schematic of Pipeline Delivery System.....	22
10.0. Heat Rate vs. Distance. m1-m8.....	27
11.0. Heat Rate vs. Distance. m9-m13.....	28
12.0. Heat Rate vs. Distance. m6-m13.....	29
13.0. Heat Rate vs. Distance. m11-m13.....	30
14.0. Refrigeration vs. Distance. m1-m8.....	31
15.0. Refrigeration vs. Distance. m9-m13.....	32
16.0. Refrigeration vs. Distance. m6-m13.....	33
17.0. Refrigeration vs. Distance. m11-m13.....	34
18.0. Installed Cost of Refrigeration Systems vs. Refrigeration Capacity.....	41
19.0. Installed Cost of Pipe vs. Diameter.....	43
20.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years.m1-m4.....	46

## LIST OF ILLUSTRATIONS (cont.)

Figure	Page
21.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years. m5-m8.....	47
22.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years. m9-m12.....	48
23.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years. m6-m9.....	49
24.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years. m10-m13.....	50
25.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years. m11-m13.....	51



## LIST OF TABLES

Table	Page
1.0. \$1000 Investment Cash Flow Table . . . . .	37
D1.0. Schedule for Tax Calculations. . . . .	86
D2.0. Yearly Tax . . . . .	87
D3.0. Face Value Cash. . . . .	88
D4.0. Present Worth at Time 0. Discounted at 10%. . . . .	88
D5.0. Cumulative Cash Flow . . . . .	89

## I. INTRODUCTION

Direct cycle high temperature gas cooled reactor systems, designed for the generation of electricity, will operate at a cycle efficiency of 37.0 per cent.<sup>[11]</sup> The remainder of the energy will be rejected as waste heat to the local environment by way of dry air cooling towers.<sup>[11]</sup> The temperature range of the rejected heat in any one system is between 472°F and 130°F at the precooler stage of the cycle.

The objective of this analysis is to determine an economically and technically feasible method of utilizing the energy rejected from this cycle. The energy is transported to the load center by means of pumped hot and/or cold water, depending on the requirements of the season.

The rejected heat from the reactor cycle provides hot water for the heating system and dry saturated steam for a series of steam jet refrigeration units, that will in turn chill the water for the cooling season.

An investigation into the economic aspects of financing the purchase and construction costs, determination of the operating costs, depreciation allowances, and resultant revenues is of the utmost importance, if the ultimate feasibility of the system is to be determined. A discounted cash flow technique is employed in this aspect of the analysis.

A FORTRAN IV computer program (HOTNCOLD) was developed to assist in the technical and economic analysis of the district heating and cooling networks.

## II. METHOD

### II.A. Outline of Procedure

The method used in defining and analyzing the district heating and cooling system is as follows:

1. Briefly describe the direct cycle high temperature gas cooled reactor thermal cycle.
2. Analyze the energy source using the following procedure.
  - a. determine the heat rejected from the reactor cycle.
  - b. determine the heat available to the district heating system at the plant site.
  - c. briefly describe the steam jet refrigeration cycle.
  - d. determine the quantity of 100 psig steam available to the steam jet refrigeration units.
  - e. determine the refrigeration available to the district cooling network at the plant site.
3. Determine the quantity of heat and refrigeration actually delivered to the load center.
  - a. conduct a heat transfer analysis to determine the amount of heat and refrigeration that arrives at the load center. Use the computer program HOTNCOLD (routine TECH) to determine this delivery capability.
4. Conduct a discounted cash flow analysis.
  - a. determine the installed cost of each operating system.
  - b. determine the operating costs of each operating system.

- c. determine a cumulative present worth schedule for a thirty year life.

## II.B. The Motive Energy Source

As a starting point the energy source of the system must be considered. This source will provide the input energy required to heat and chill the water, that will in turn transport the energy to a district heating and cooling network.

Figure 1.0 is a typical schematic representation of a direct cycle high temperature gas cooled reactor, as designed by General Atomics International.<sup>[11]</sup> The precooler section is of particular interest here, since it is this area where nearly all the rejected heat of the cycle appears. The temperature of the rejected heat is relatively high when compared to the typical rejection temperatures encountered in conventional steam Rankine cycle. In this system the temperature drop across the precooler ranges from 470°F at the entrance of the precooler to 130°F at the exit; whereas, in the Rankine steam cycle condenser rejection temperatures would be around 105°F. For the case investigated herein a reactor with an electrical power output of 1100 MWe and a cycle efficiency of 37 per cent was chosen as being typical of design considerations at this time.<sup>[11]</sup>

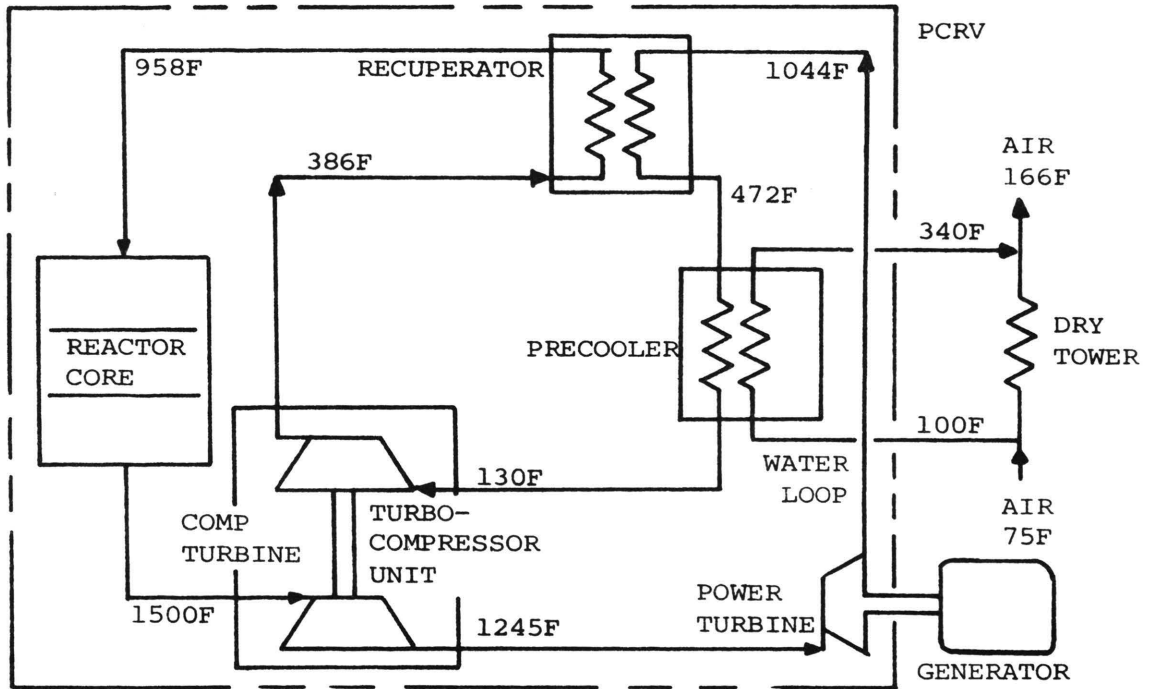


Fig. 1.0. Direct Cycle High Temperature Gas Cooled Reactor. [11]

II.B.1. Thermal balance on the precooler section to determine the steam available to the refrigeration units

Figure 2.0 is a schematic representation of a steam generator acting as the heat rejection point for the precooler stage of the cycle. The steam generator is designed such that helium can transfer heat through a temperature range of 472°F to an exit temperature of 103°F. This heat is transferred to water entering the steam generator at 80°F and exiting as dry saturated steam at 100 psig and a temperature of 338°F. What follows is a thermal balance on the steam generator to determine the mass rate of flow of 100 psig dry saturated steam that is available to the refrigeration units.

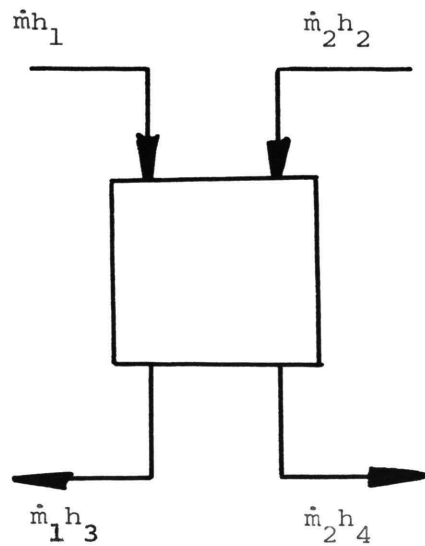


Fig. 2.0. Precooler as Steam Generator.

Where

$\dot{m}_1$  = incoming and exiting mass rate of flow of the helium (lbm/hr)

$\dot{m}_2$  = incoming and exiting mass rate of flow of either the water  
or steam (lbm/hr)

$h_1$  = incoming enthalpy of the helium (BTU/lbm)

$h_2$  = incoming enthalpy of the water (BTU/lbm)

$h_3$  = exit enthalpy of the helium (BTU/lbm)

$h_4$  = exit enthalpy of the steam (BTU/lbm)

Performing an energy balance:

$$\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_1 h_3 + \dot{m}_2 h_4 \quad (1)$$

rearranging

$$\dot{m}_1 (h_1 - h_3) = \dot{m}_2 (h_4 - h_3) \quad (2)$$

However, it is known that the left hand term in Equation (2) represents the rejected heat from the cycle. Thus,

$$Q_r = \dot{m}_2 (h_4 - h_3) \quad (3)$$

also

$$Q_{th} = Q_r + Q_e \quad (4)$$

and

$$Q_e = Q_{th} N_{cy} \quad (5)$$

Substituting (5) in (4),

$$Q_r = \frac{Q_e}{N_{cy}} - Q_e \quad (6)$$

where

$Q_r$  = rejected thermal energy (BTU/hr)

$Q_{th}$  = total energy output of the reactor (BTU/hr)

$Q_e$  = total electrical energy generated (BTU/hr)

$N_{cy}$  = cycle efficiency

hence from (6) and (3) we have:

$$\dot{m}_2 = \frac{Q_r}{h_4 - h_3} \quad (7)$$

from (6)  $Q_r$  may be determined:

$$Q_e = 1100 \text{ MWe}$$

$$N_{cy} = .37$$

$$Q_r = \frac{(1100 \text{ MWe})(3.414 \times 10^6) \text{ BTU/hr} - \text{MWe}}{.37}$$

$$- (1100 \text{ MWe})(3.414 \times 10^6 \text{ BTU/hr} - \text{MWe})$$

$$Q_r = 6.394 \times 10^9 \text{ BTU/hr}$$

For the refrigeration system that was selected, 100 psig dry saturated steam is required. [20]



Then at 115 psia saturated:

$$h_4 = 1189.6 \text{ BTU/lbm}$$

The water entering the steam generator is at 70°F then:

$$h_3 = 38.025 \text{ BTU/lbm}$$

solving for the mass rate of flow from (7):

$$\dot{m}_2 = \frac{6.394 \times 10^9 \text{ BTU/hr}}{(1189.6 - 38.025) \text{ BTU/lbm}}$$

$$\dot{m}_2 = 5.55 \times 10^6 \text{ lbm/hr} \quad (8)$$

#### II.C. 40°F Water Available to the System

The energy in the steam calculated in section II.B.1 will act as the motive energy source for a steam jet refrigeration cycle.

##### II.C.1. Description of the cycle

Water is used as the working fluid in this system. Figure 3.0 is a schematic representation of the refrigeration unit. [20] The evaporator, as in any refrigeration system, is the point at which the actual refrigeration takes place.

Water is evaporated under low pressure thereby cooling the water returning from the load. In order to maintain a sufficiently low pressure in the evaporator, water vapor must be continuously removed from the evaporator. Vapor is removed by entraining evaporator

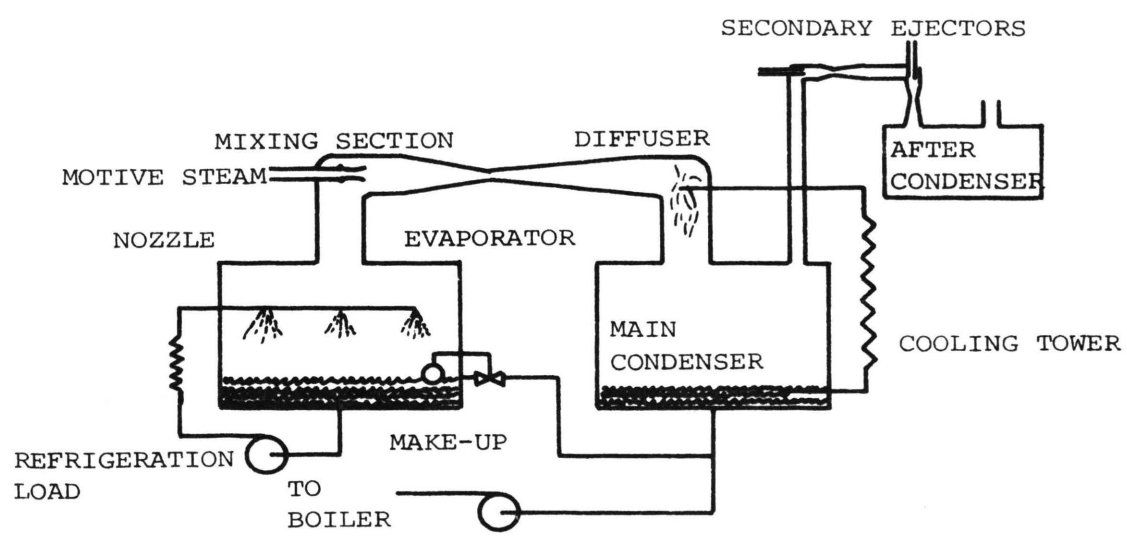


Fig. 3.0. Schematic of the Steam Jet Cycle.

vapor with a supersonic flow of steam from the jet nozzle. Steam leaves the jet nozzle at supersonic velocities and requires a back pressure usually between 20 and 100 psig. The supersonic flow entrains the evaporator vapor at a ratio between 2.0 lbm motive steam per lbm evaporator vapor and 3.0 lbm motive steam per lbm of evaporator vapor. The mixture moves at supersonic velocities through the mixing section at constant pressure to the throat where a shock wave is formed. The mixture compresses through the wave and is returned through the diffuser to the condenser at a higher pressure. Liquid water is pumped from the condenser to the boiler to create motive steam and some is valved to the evaporator as make up water. The cycle is now repeated to maintain a sufficiently low temperature at a continuous rate.

#### II.C.2. Refrigeration available at the plant site

The amount of refrigeration may now be determined by the use of a parametric graph.<sup>[20]</sup> Rather than solve the steam jet thermodynamic cycle to determine the refrigeration available, graphs plotting the parameters governing the thermodynamic cycle of the steam jet units are used. Figure 4.0 is a plot of the parameters that govern the operation of the steam jet cycle for standard manufactured units.<sup>[20]</sup> In this figure the parameters of condenser temperature, condenser water flow rate, booster steam consumption and chilled water temperatures are plotted in their relationships to each other at a constant steam back pressure of 100 psig.

For this case a condenser temperature of 100°F is typical for summer operation and a required chilled water temperature of 40°F is selected. Water in this temperature range is desirable due to the dew point requirements of humidity control. Then from Fig. 4.0

$$\text{at } T_c = 100^\circ\text{F}$$

$$T_{cw} = 40^\circ\text{F}$$

it is found that

1.0 Tons of refrigeration are available for every  
27.5 lbm/hr of 100 psig. dry saturated steam  
moved through the jet nozzle.

where

$T_c$  = condenser temperature

$T_{cw}$  = chilled water temperature

$$RA = \frac{\dot{m}_2}{SRA}$$

where

RA = refrigeration available (Tons)

SRA = specific refrigeration available

thus

$$RA = \frac{5.55 \times 10^6 \text{ lbm/hr}}{27.5 \text{ lbm/hr} - \text{Ton}}$$

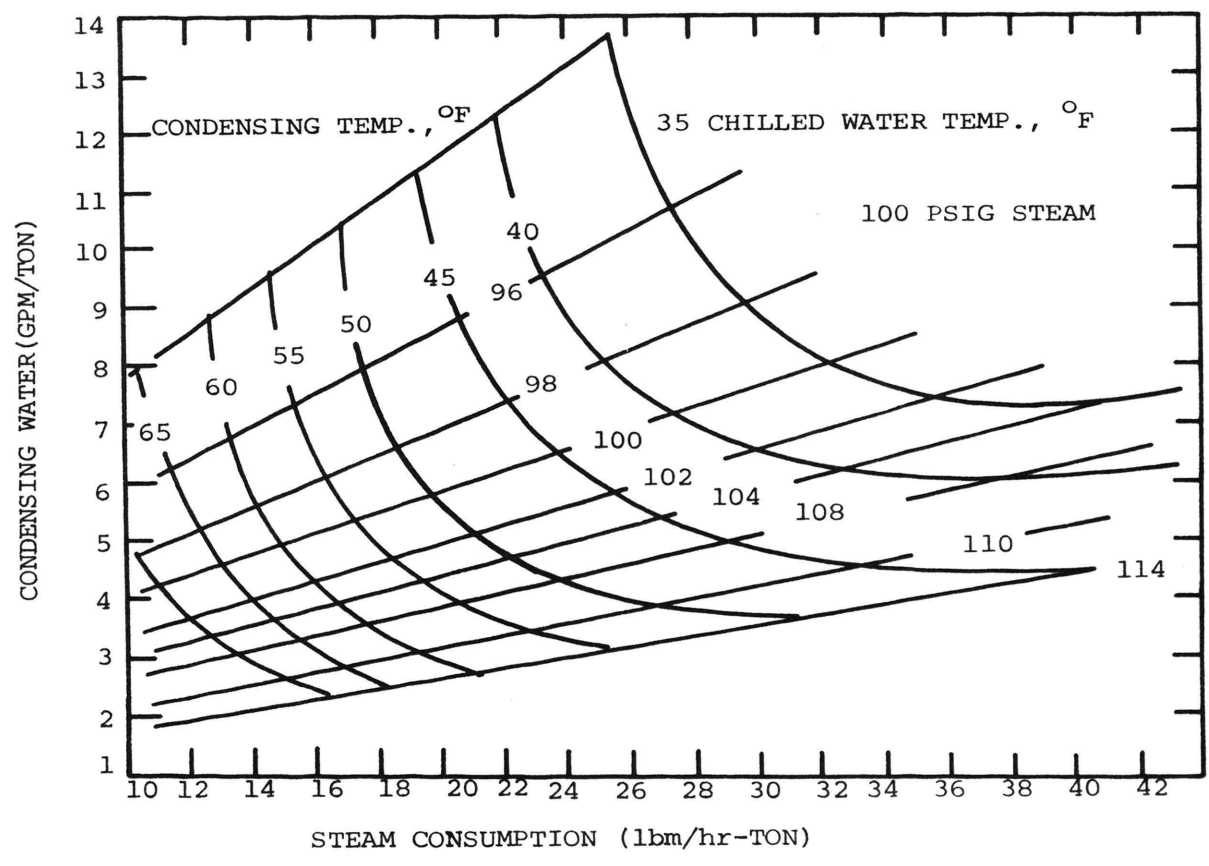


Fig. 4.0 Steam Jet Cycle Parameters

$$RA = 2.05 \times 10^5 \text{ Tons}$$

in terms of BTU/hr this would be

$$RA = (2.02 \times 10^5 \text{ Tons}) \times (12000 \text{ BTU/hr} - \text{Ton})$$

$$RA = 2.424 \times 10^9 \text{ BTU/hr}$$

### II.C.3. Cooling water available to the pipeline

Consider the thermal balance on the cooling unit given in Fig. 5.0, with water returning from the load, entering the refrigeration unit, being chilled, then returned to the load.

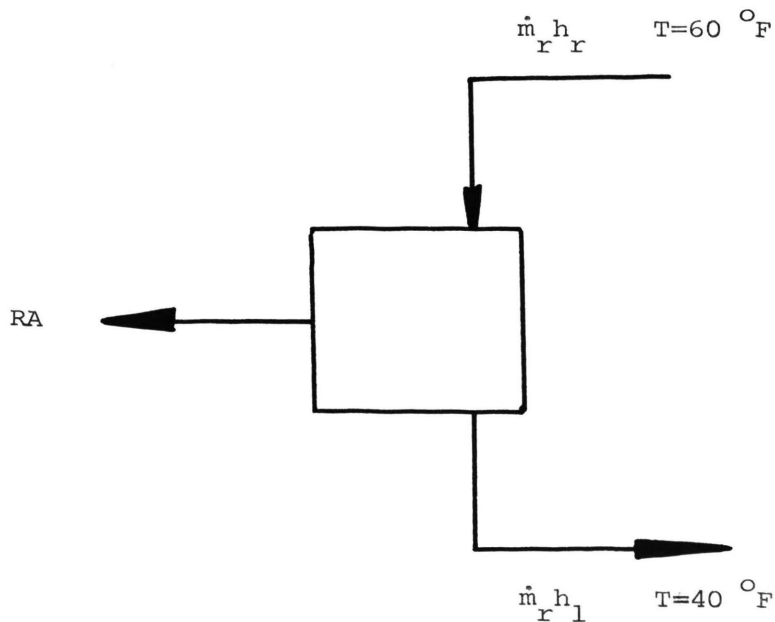


Fig. 5.0. Cooling Unit Thermal Balance.

where

$\dot{m}_r$  = mass rate of flow of chilled water available to the load (lbm/hr)

$h_r$  = enthalpy of the water returning from the load (BTU/lbm)

$h_l$  = enthalpy of water leaving the refrigeration unit

Performing a thermal balance yields:

$$RA = \dot{m}_r h_r - \dot{m}_r h_l$$

$$\dot{m}_l = \frac{RA}{h_r - h_l}$$

$$\dot{m}_l = \frac{2.424 \times 10^9 \text{ BTU/hr}}{(28.06 - 8.027) \text{ BTU/lbm}}$$

$$\dot{m}_l = 1.21 \times 10^8 \text{ lbm/hr}$$

#### II.D. 200°F Water Available to the System

It must now be determined how much hot water may be delivered from the plant at a temperature of 200°F.

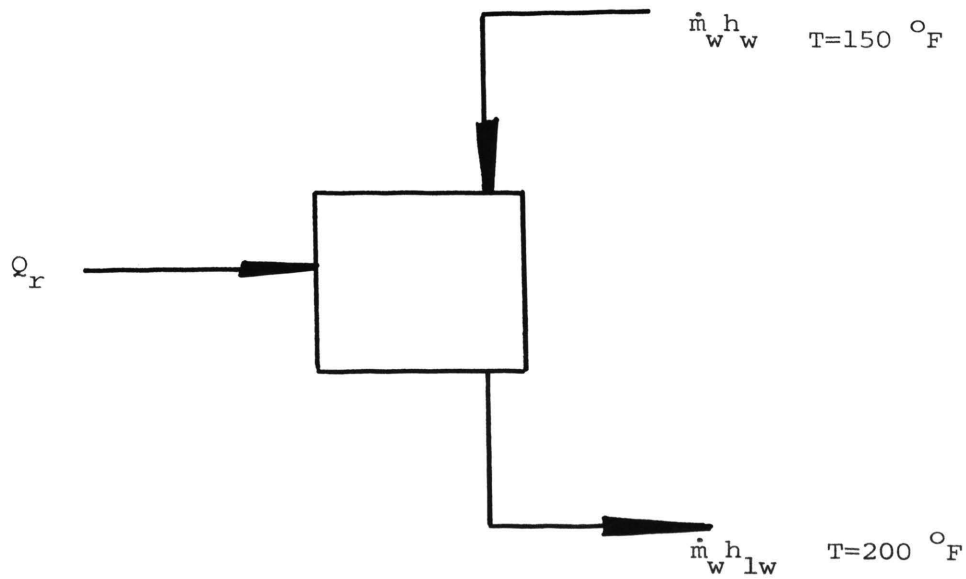


Fig. 6.0. Thermal Balance for Heating System.

where

$\dot{m}_w$  = mass rate of flow of heated water available to the system (lbm/hr)

$h_w$  = enthalpy of the water returning to the plant (BTU/lbm)

$h_{lw}$  = enthalpy of the water leaving the plant and returning to the load (BTU/lbm)

Performing an energy balance:

$$Q_r = \dot{m}_w h_{lw} - \dot{m}_w h_w \quad (12)$$

$$\dot{m}_w = \frac{Q_r}{h_{lw} - h_w} \quad (13)$$

Determining the enthalpies  $h_w$  and  $h_{lw}$  from the steam tables at the given temperatures and substituting these values in (13) we have:

$$\dot{m}_w = \frac{6.394 \times 10^9 \text{ BTU/hr}}{(168.09 - 117.95) \text{ BTU/lbm}}$$

$$\dot{m}_w = .910 \times 10^8 \text{ lbm/hr}$$

It is now known that  $0.910 \times 10^8$  lbm/hr of  $200^\circ\text{F}$  water and  $1.210 \times 10^8$  lbm/hr of  $40^\circ\text{F}$  water is available to the pipeline system.



### III. HEAT TRANSFER AND PRESSURE DROP CALCULATIONS

At this point the energy available to the system in the form of heated and chilled water is known. However, since the energy must be transmitted over some distance to the load center, additional factors affecting the actual quantity of energy delivered to the load center must be considered. These factors include; pressure drop calculations as a function of linear water velocity and pipe diameter, and heat transfer through the pipe over the distance to the load.

#### III.A. Pipeline Pressure Drop Calculations

For a given size pump rated for a fixed horsepower, the proper diameter pipe must be matched to the mass rate of flow at which the pump is rated. This will be done for various diameter pipes by the following procedure.

1. Select the size of the pump.
2. The maximum mass rate of flow has been determined in section II.
3. Determine the linear velocity of the water in the pipe.
4. Determine the pressure drop for a specific diameter linear velocity and friction factor in the pipe.
5. Determine the distance between the pumps in the pipeline.

## III.A.1. Pressure drop per mile of pipe

$$DP = \frac{(f)(SV)(5280 \text{ ft/mile})}{D} \frac{G}{10000}^2 \quad (14)$$

where

DP = pressure drop (psi)/unit length

f = friction factor (Moody determination)

D = pipe diameter (inches)

SV = specific volume (ft<sup>3</sup>/lbm)

G = mass rate of flow/pipe cross sectional area (lbm/hr-ft<sup>2</sup>)

## III.A.2. Horsepower required per mile

$$HP = \frac{(A)(H)}{36000} \quad (15)$$

where

HP = horsepower required/mile

H = pressure drop in feet of water/mile

A = mass rate of flow (lbm/sec)

and

$$DBP = \frac{\text{HORSEPOWER OF PUMP SELECTED}}{HP} \quad (16)$$

where

DBP = distance between pumps (miles)

### III.B. Pipeline Heat Transfer Calculations

There are two important determinations to be made at this point in the analysis.

1. Determine the heat transfer in or out of the pipeline for a given distance.
2. Determine the energy addition to the water by the pumps.

Consider the schematic in Fig. 7.0 representing a pipeline with a series of pumps.

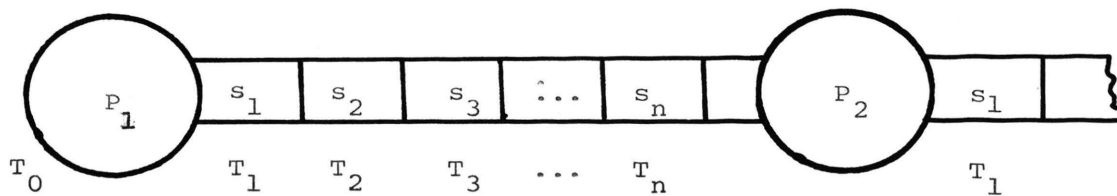


Fig. 7.0. Pipeline Schematic.

Water enters pump P<sub>1</sub> at mass flow rate  $\dot{m}$  lbm/hr. The energy added across the pump would be:

$$h'_w = h_w + \frac{HP}{\dot{m}} \quad (17)$$

where

$h_w$  = internal energy of the water before entering pump P<sub>1</sub>

HP = power output of the pump (BTU/hr)

$h'_w$  = internal energy of the water after the pump

Immediately following the pump  $P_1$ , energy will begin to flow across the wall of the pipe if the ambient temperature is different from that of the water in the pipe (this will be the case in most circumstances). As the water moves downstream from the pump heat will transfer out or into the pipe, as a result of this heat flow the temperature of the water will be a different value from one instant to the next. This fact will in turn effect the rate of heat transfer in or out of the pipe, because the rate of heat transfer is determined by the temperature difference across the pipe. It is possible to approximate the actual case by assuming the temperature of the water to be essentially constant for very small subsections ( $S_n$ ) of the distance between the pumps (L).

These calculations would be carried out by first determining the rate of heat loss per unit length for a constant temperature difference.

Consider Fig. 8.0 which is a cross sectional representation of an insulated pipe buried in the ground. The steady state heat transfer per unit length is given by: [5]

$$Q_a = \frac{2\pi(T_i - T_G)}{\frac{1}{h_1 r_1} + \frac{\ln(r_2 - r_1)}{k_p} + \frac{\ln(r_3 - r_2)}{K_I} + \frac{\ln(r_4 - r_3)}{K_g}} \quad (18)$$

where

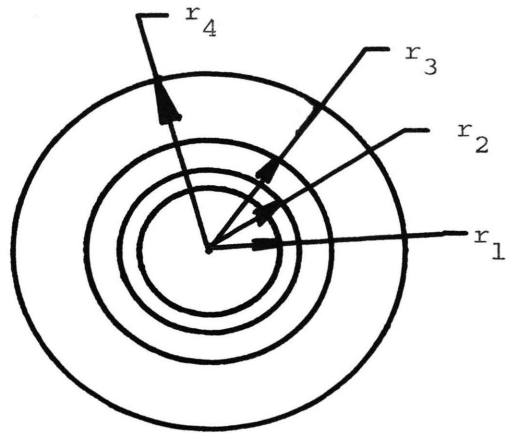


Fig. 8.0. Cross Section of an Insulated Buried Pipe.

$$h_1 = \frac{(NU_d)(k_w)}{2r_1} = \text{the film coefficient} \quad (19)$$

and

$NU_d$  = Nusselt number

$$= .023(Re_d)^{.8} (Pr)^B$$

$B = .4$  for heating the water

$B = .3$  for cooling the water

$Re_d$  = Reynolds number

$$= \frac{V 2r_1}{v_k}$$

$Pr$  = Prandtl number

$V$  = water velocity

$v_k$  = kinematic viscosity of the water

$k_w$  = thermal conductivity of the water

$T_i$  = temperature of the water

$T_G$  = temperature of the ground the pipe is buried in

$r_1$  = inner radius of the pipe

- $r_3$  = outer radius of the insulation  
 $r_4$  = outer radius of the soil around the pipe  
 $k_p$  = thermal conductivity of the pipe (BTU/hr-ft-°F)  
 $k_I$  = thermal conductivity of the insulation  
 $k_g$  = thermal conductivity of the ground  
 $Q_a$  = heat transfer per unit length (BTU/hr-ft)

The sequence of events used in determining the heat transfer in each section would be:

For heat transfer in section  $s_1$  Fig. 7.0:

1. Determine the pump energy addition to the water by using equation (17) and find  $h'_w$ .
2. From the steam tables determine the temperature  $T_2$  (Fig. 7.0) from the value  $h'_w$ .
3. Given the ground temperature  $T_G$  (Fig. 8.0) and having calculated the water temperature  $T_1 = T_i$  use equation (18) to determine the heat transferred per unit length.
4. Determine the film coefficient  $h_1$  by equation (19).
5. Determine the heat transferred through section  $s_1$  of the pipe  $Q_a$ .
6. Determine the new enthalpy of the water by:

$$h''_w = h'_w + \frac{Q_a}{\dot{m}}$$

7. Knowing  $h''$  determine the corresponding temperature  $T_2 = T_i$  from the thermodynamic tables and use this as the constant temperature for section  $s_2$ .

8. Repeat steps 1 through 7 for all sections through  $s_n$  until the next pump or the load center is reached.

### III.C. Energy Available at the Load Center

In section III.A and III.B, the technique for determining the temperature at any point in the pipeline was discussed. Now the actual amount of energy available at the load center may be determined.

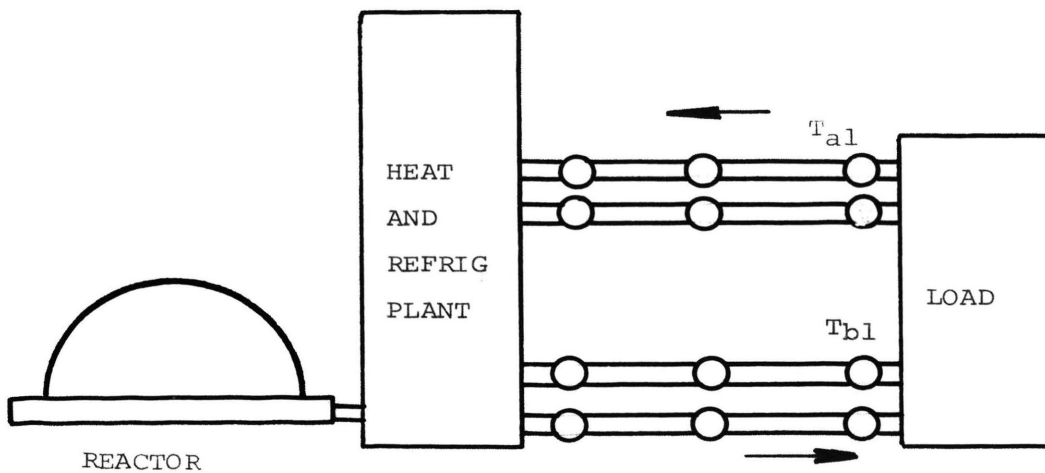


Fig. 9.0. Schematic of Pipeline Delivery System.

The three important factors involved in this analysis are:

1. Determination of the temperature before the load
2. Determination of the temperature after the load
3. Determination of the mass rate of flow

The temperature before the load was calculated by the technique

outlined in the previous sections and  $\dot{m}$  is known. The temperature after the load, is in most instances variable, dependent on the weather conditions effecting the local requirements. For purposes of this analysis a maximum temperature differential across the load is specified.

The temperature increase across the load for the air conditioning service never exceeds 12°F. Temperature increases greater than 12°F would make humidity control difficult. The temperature change across the load for heating was chosen to be 35°F. Temperature drops greater than 35°F are possible; however, the lower the temperature entering the load center the greater the heat exchanger surfaces required to deliver an equivalent amount of energy. Since the temperature change across the load will be a function of the temperature of the water entering the load center; the temperature change across the load must also be a function of the distance from the load center.

#### Assumptions

$$T_{al} = 55^{\circ}\text{F for the air conditioning service}$$

$$T_{al} = 150^{\circ}\text{F for the heating service}$$

where

$$T_{al} = \text{temperature after the load}$$

The energy left at the load would be:



$$Q_1 = \dot{m}h_{b1} - \dot{m}h_{a1}$$

where

$Q_1$  = energy removed from, or added to the load center (BTU/hr)

$h_{b1}$  = enthalpy of the water before the load (BTU/lbm)

$h_{a1}$  = enthalpy of the water after the load (BTU/lbm)

### III.D. Demonstration of Method

A computer program HOTNCOLD (subroutine TECH) was developed to utilize the type of analysis outlined in the above sections. The following input to the program was used for the systems analyzed in this investigation.

#### III.D.1. Program input

Temperature drop across the load = 20°F to 35°F (heating)

Temperature rise across the load = less than 12°F (cooling)

Number of pipes = 2 in each direction \*\*

Water mass rate of flow = variable  $.8 \times 10^8$  lbm/hr to

$.3 \times 10^8$  lbm/hr

Pump size = 7000 horsepower

Thermal conductivity of the water = .338 BTU/hr-ft°F

Thermal conductivity of the pipe = 25.0 BTU/hr-ft°F

---

\*\* two pipes were selected because there is sufficient water available to the system at full load to accommodate a two pipe system

Thermal conductivity of the insulation	= .13 BTU/hr-ft°F
Thermal conductivity of the soil	= 1.0 BTU/hr-ft°F
Friction factor (Moody determination)	= .015
Maximum distance to the load centre	= 110 miles
Pipe diameter	= 30 to 60 inches
Kinematic viscosity of the water	= function of temperature in tabular form
Prandtl Number	= function of temperature in tabular form
Months of heating service	= 4 months (full load)
Months of cooling service	= 3 months (full load)

### III.E. Results

The following figures are the results of the calculations done in subroutine TECH in the program HOTNCOLD.

The graphs illustrate the refrigeration or heat available at a given distance PER PIPE. For example it is seen from Fig. 16.0 that 51820.0 tons of refrigeration is available per delivery pipe at a distance of 100.0 miles with a 60 inch pipe and a mass rate of flow of  $56.0 \times 10^6$  lbm/hr of chilled water.

At the same distance from Fig. 10.0,  $1.91 \times 10^9$  BTU/hr is available to a heating load with the same mass rate of flow of water. It is known from sections II.C.2 and II.B that  $1.21 \times 10^8$  lbm of chilled water and  $.910 \times 10^8$  lbm/hr of heated water are actually available to the pipeline. Obviously what this means is that two pipes may be used to deliver at maximum load. When the season does not require a

strictly heating or air conditioning service, hot water may be shipped in one pipe and cold in the other.

The following symbols key the mass rates of flow on Figures 10.0 through 17.0.

$$m1 = 57 \times 10^6 \text{ lbm/hr}$$

$$m2 = 56 \times 10^6 \text{ lbm/hr}$$

$$m3 = 55 \times 10^6 \text{ lbm/hr}$$

$$m4 = 54 \times 10^6 \text{ lbm/hr}$$

$$m5 = 53 \times 10^6 \text{ lbm/hr}$$

$$m6 = 52 \times 10^6 \text{ lbm/hr}$$

$$m7 = 51 \times 10^6 \text{ lbm/hr}$$

$$m8 = 50 \times 10^6 \text{ lbm/hr}$$

$$m9 = 49 \times 10^6 \text{ lbm/hr}$$

$$m10 = 48 \times 10^6 \text{ lbm/hr}$$

$$m11 = 47 \times 10^6 \text{ lbm/hr}$$

$$m12 = 46 \times 10^6 \text{ lbm/hr}$$

$$m13 = 45 \times 10^6 \text{ lbm/hr}$$

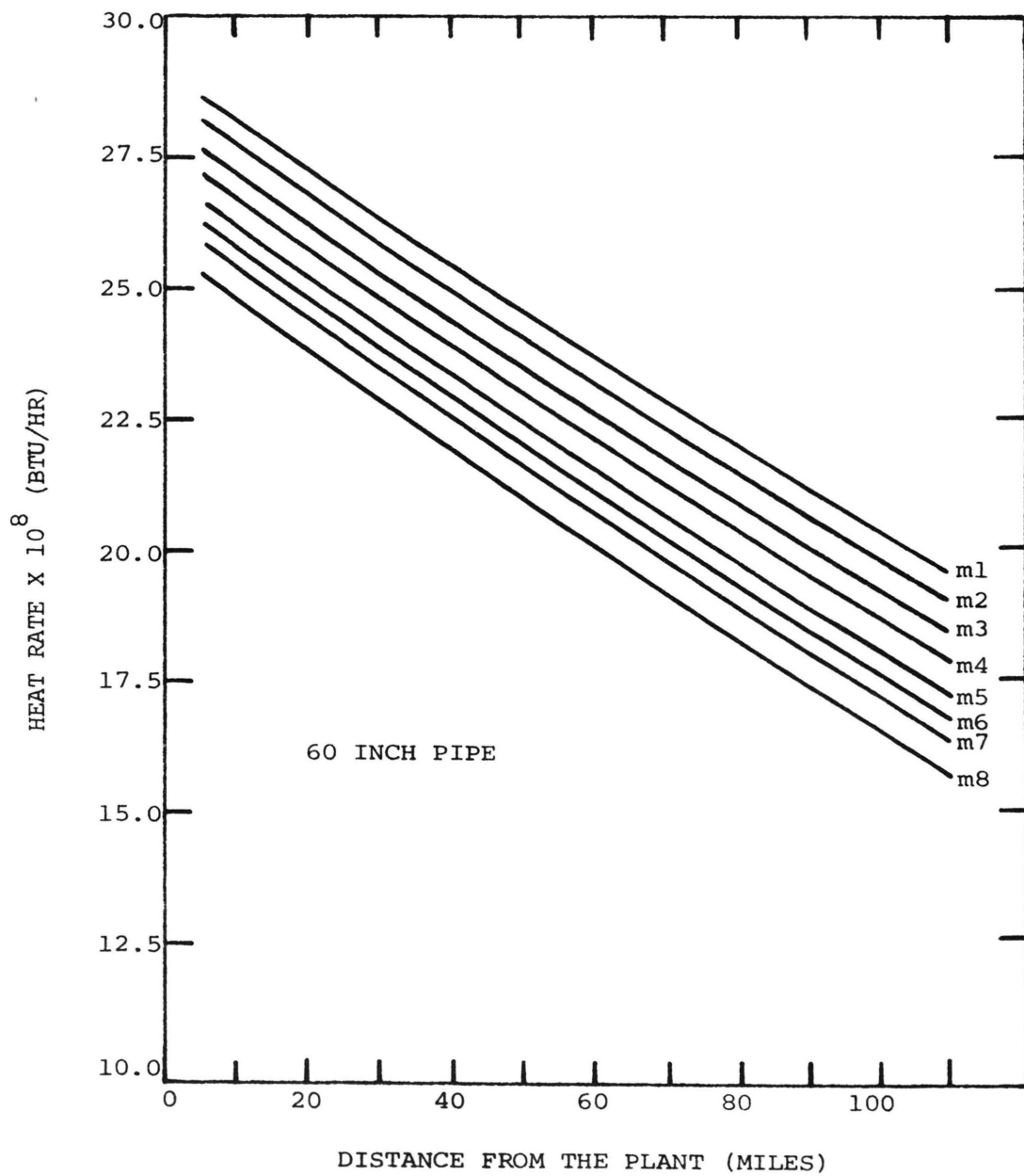


Fig. 10.0. Heat Rate vs. Distance. m1-m8

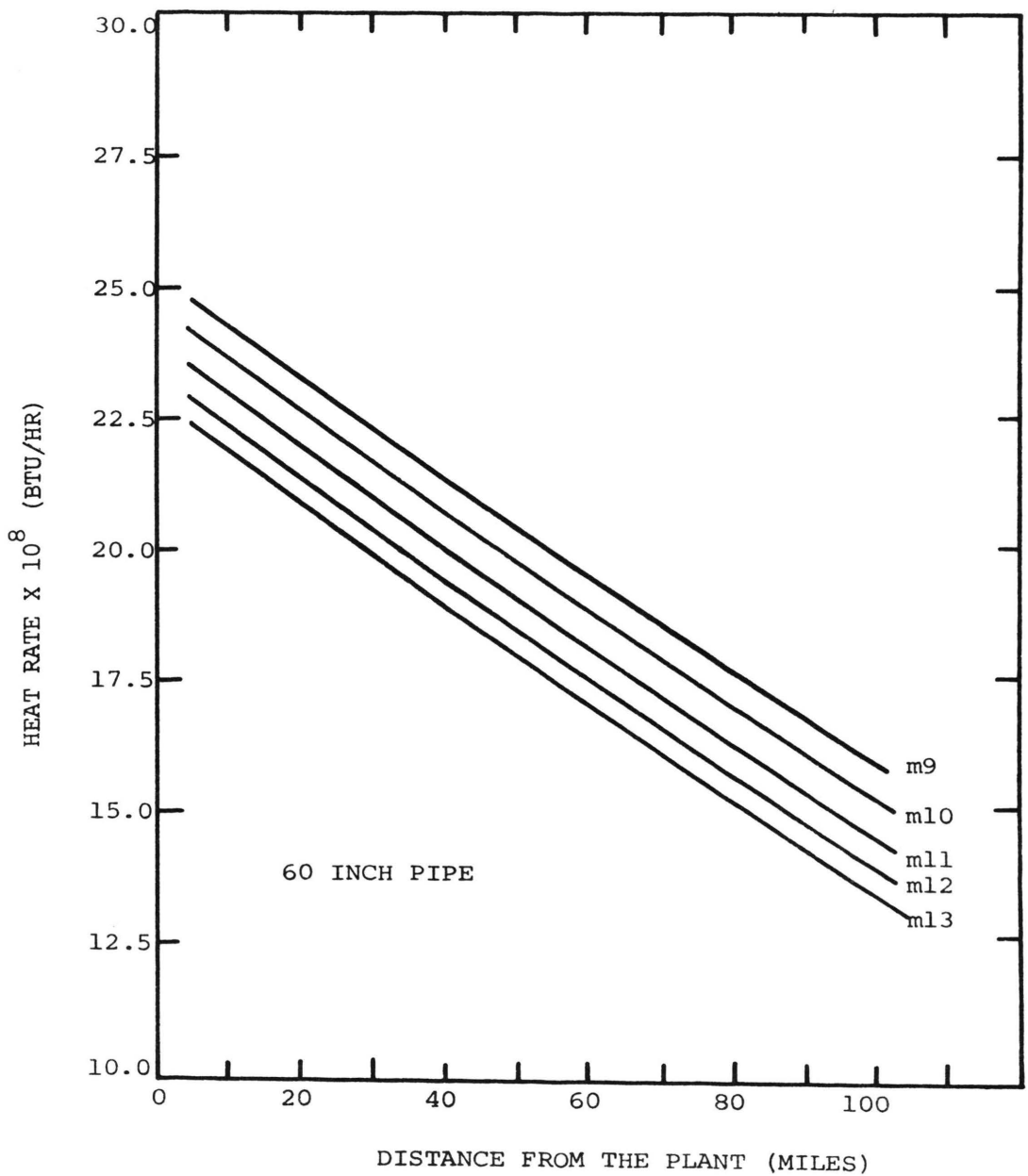


Fig. 11.0. Heat Rate vs. Distance. m9-m13

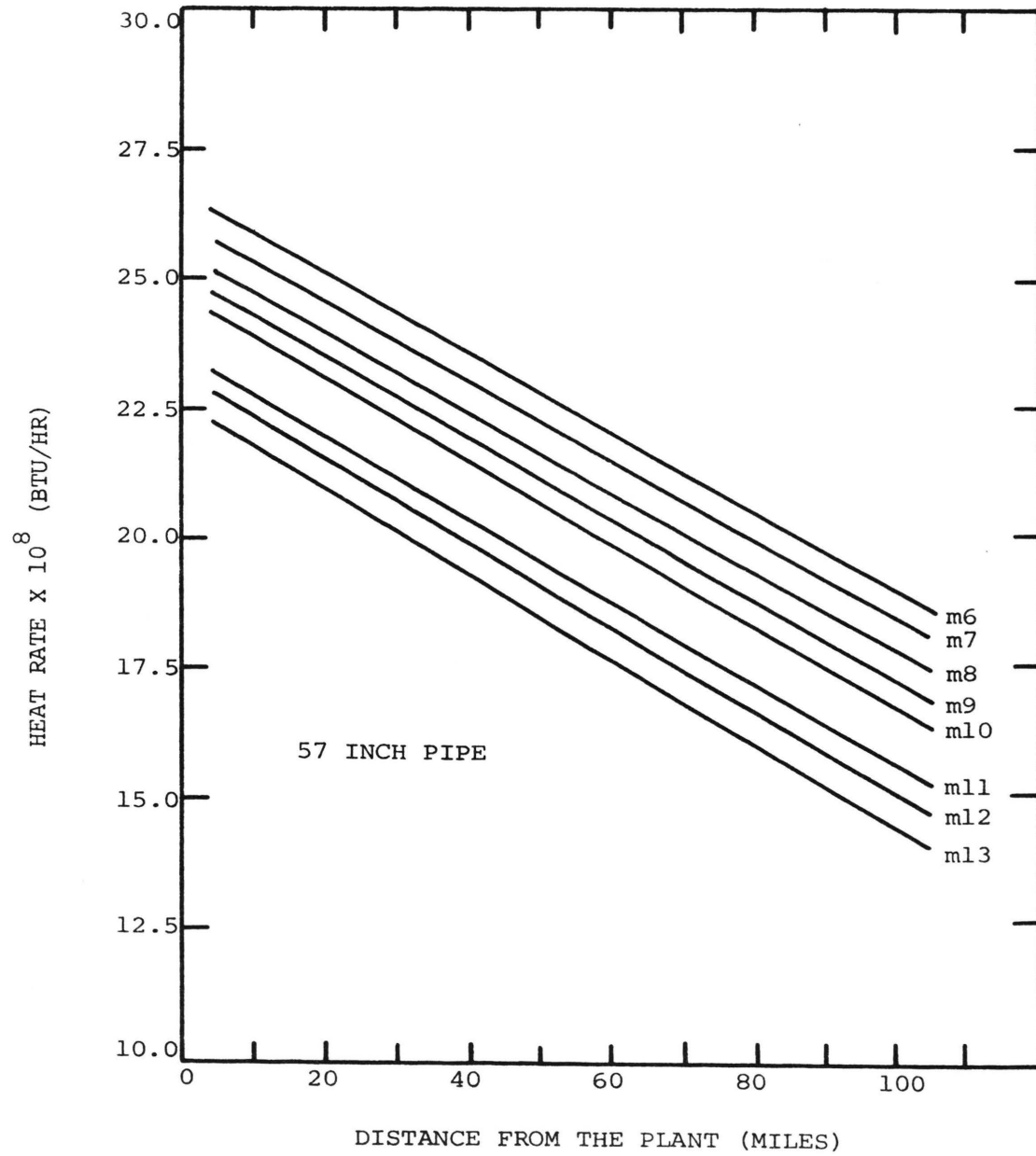


Fig. 12.0. Heat Rate vs. Distance. m6-m13

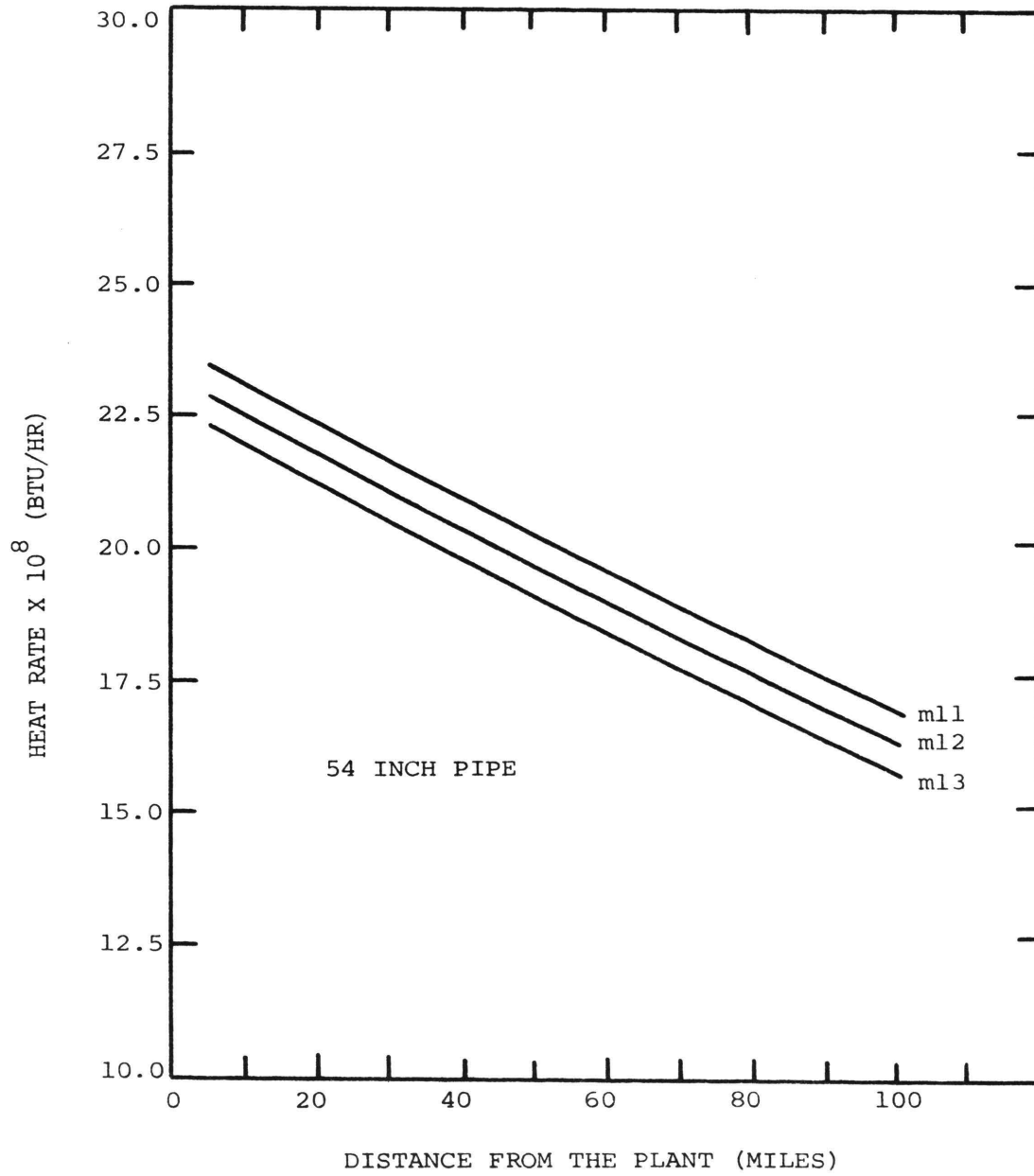


Fig. 13.0. Heat Rate vs. Distance. m11-m13

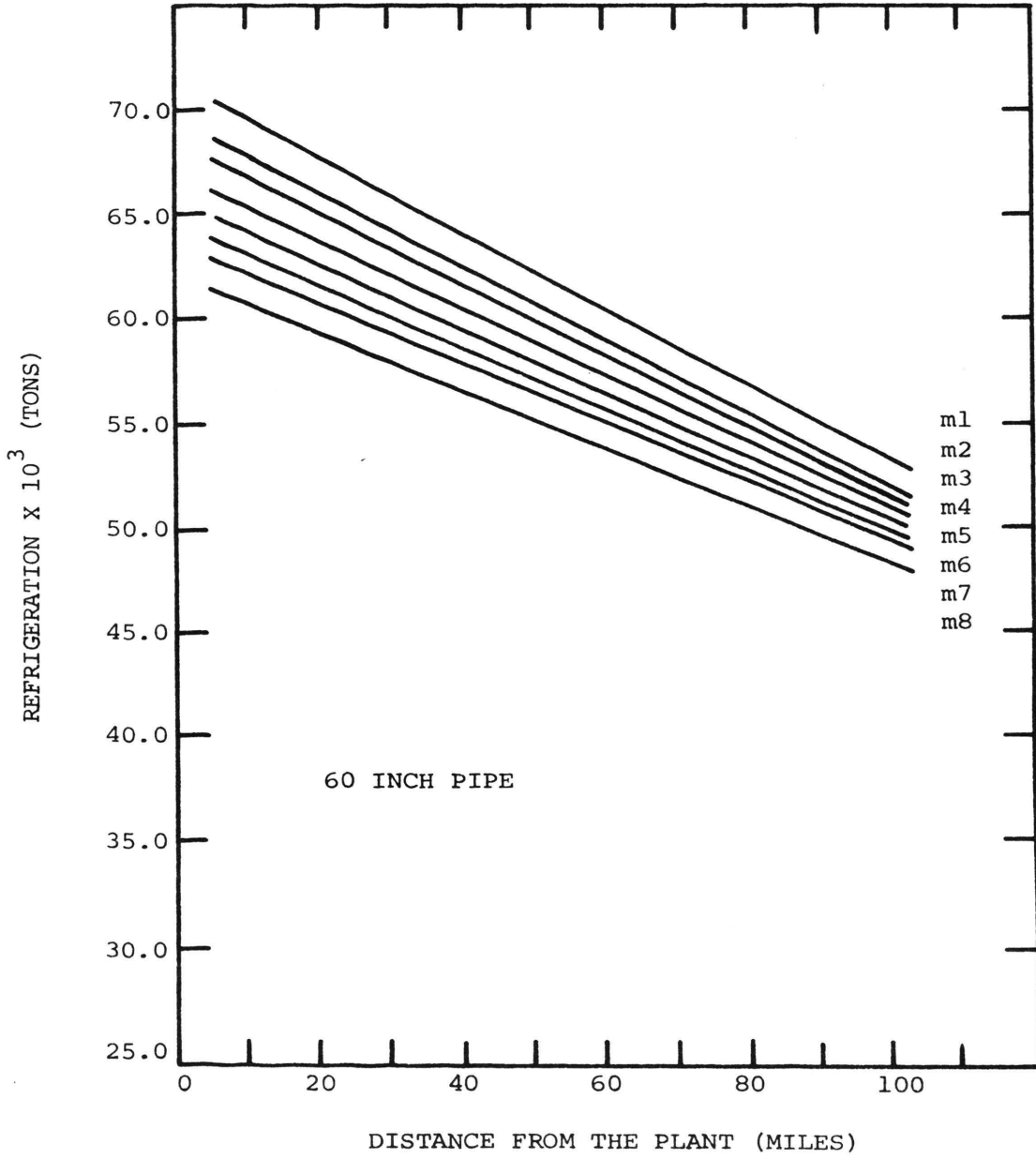


Fig. 14.0. Refrigeration vs. Distance from the Plant. m1-m8



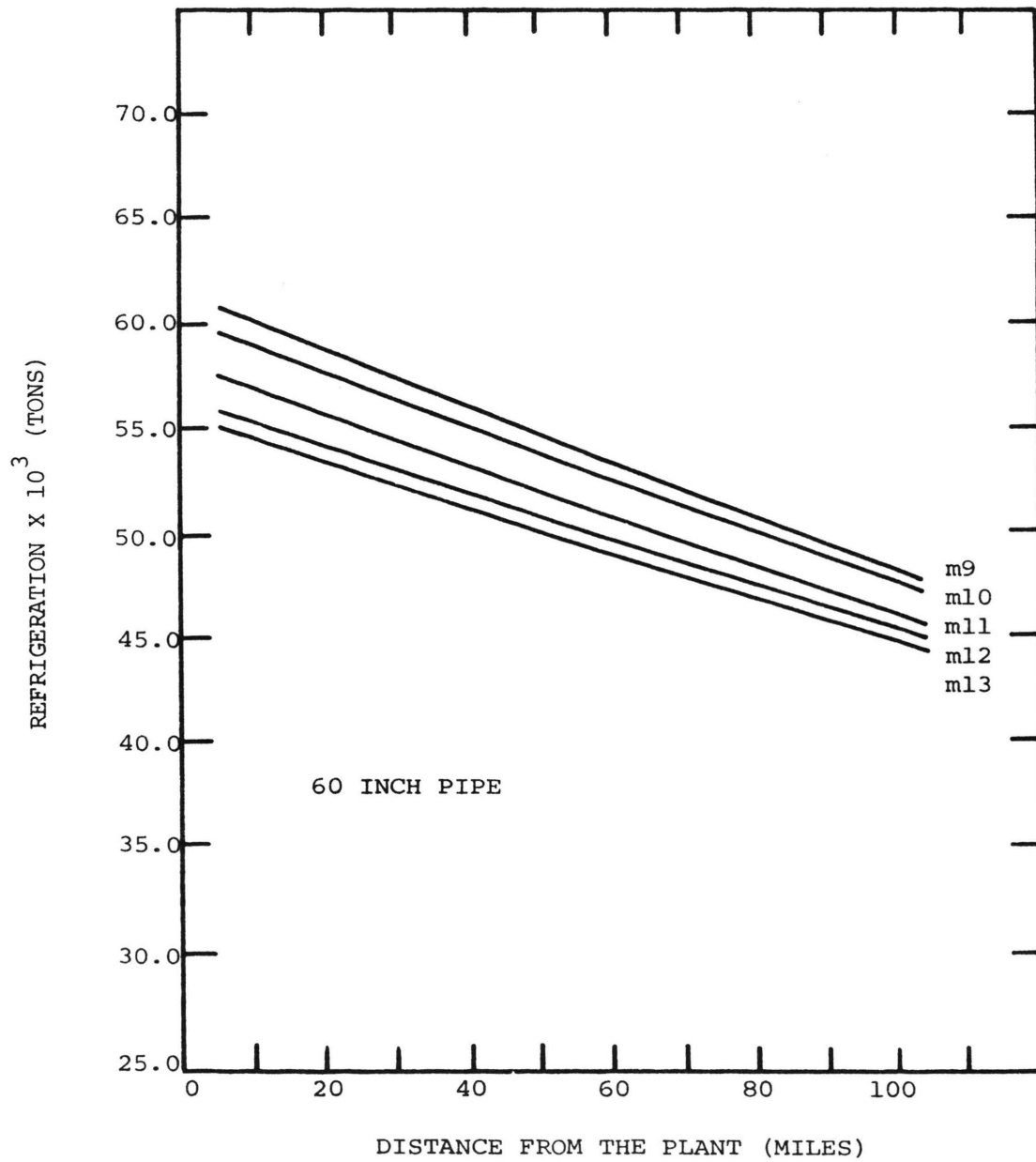


Fig. 15.0. Refrigeration vs. Distance from the Plant. m9-m13

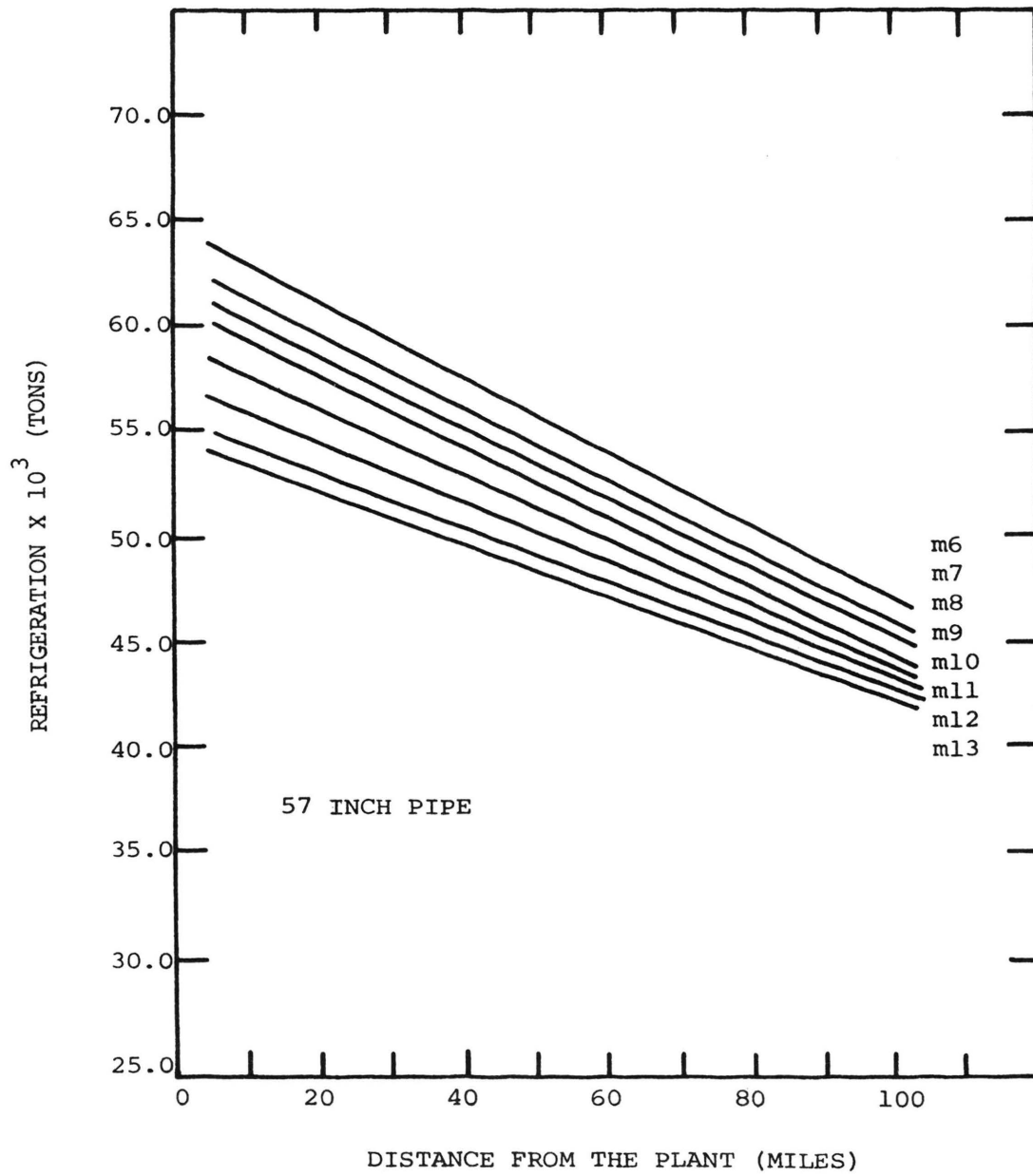


Fig. 16.0. Refrigeration vs. Distance from the Plant. m6-m13

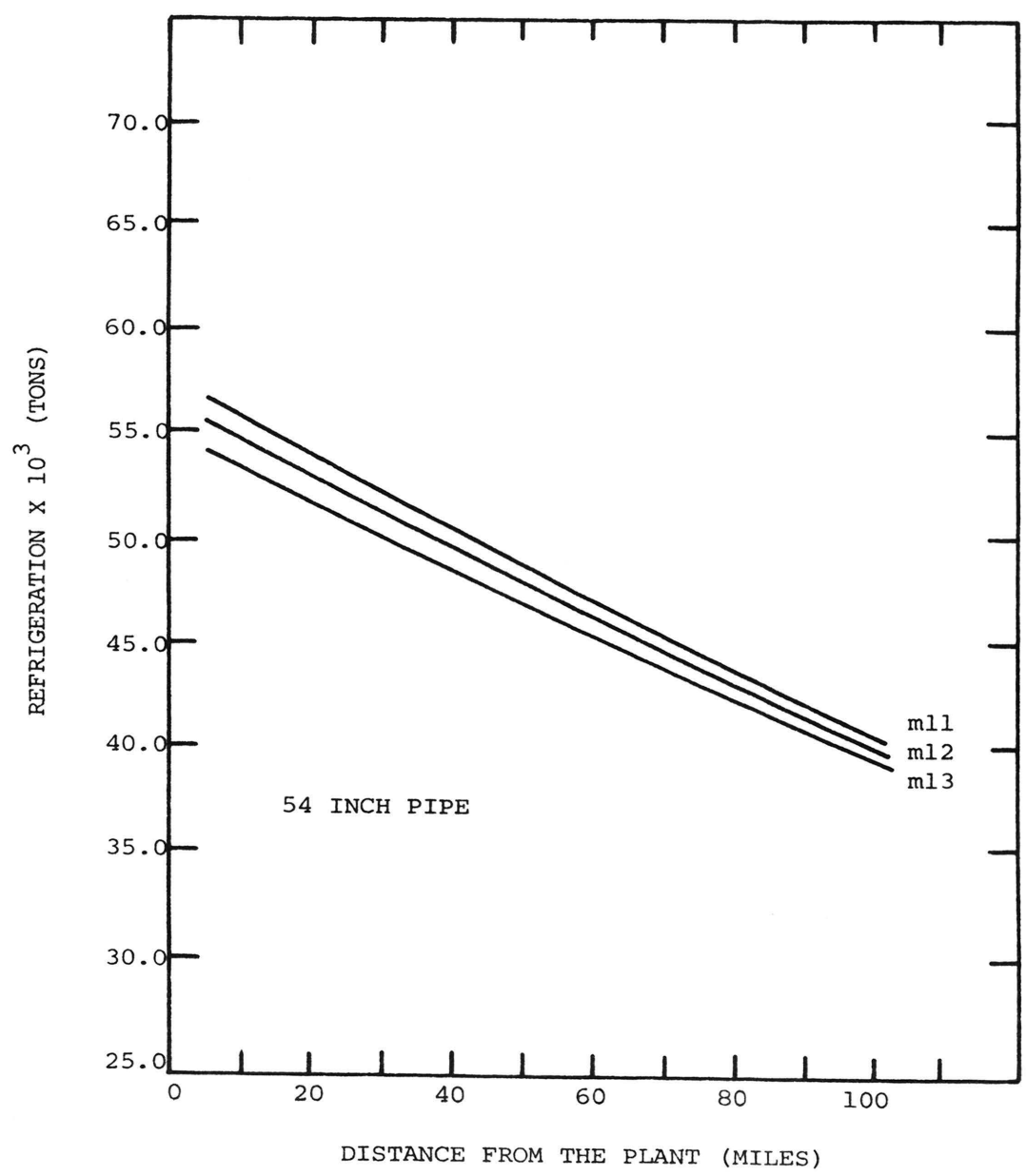


Fig. 17.0. Refrigeration vs. Distance from the Plant. m11-m13

#### IV. CASH FLOW ANALYSIS

A discounted cash flow analysis is conducted to yield an initial look at the economic desirability of undertaking the district heating and cooling project.

##### IV.A. Procedure

The following procedure was used to carry out the cash flow analysis:

1. These parameters are held at fixed levels:
  - a. The revenue rate for energy sold
  - b. The discounting rate
  - c. The cost and revenue escalation rate
  - d. Depreciation scheme for capital investments
2. Decide which parameters to vary as a function of the physical system:
  - a. The installed cost of the piping system
  - b. The maintenance cost of the system
  - c. Installed cost of the refrigeration system
  - d. Operating cost of the system
  - e. Tax costs
3. For each unique set of parameters carry out the following:
  - a. Establish a 30 year face value cash flow table with escalation (inflation) costs included
  - b. Discount the face value table to a single present worth cash in and cash out value

- c. Calculate the cumulative present worth table for the 30 year life of the project.

#### IV.A.1. Rates

Discounting interest rate	= 10%
Cost and revenue escalation (inflation)	= 4.5%
Tax rate (income)	= 50.0%
Bond rate of interest	= 7.0%
Preferred stock interest	= 7.0%
Common stock interest	= 14.0%
Cost of heat	= \$1.00/million BTU
Cost of refrigeration	= \$2.00/million BTU
Life	= 30 years
Property tax rate	= 2.0%
Installed cost of pumping stations	= \$275.00/horsepower
Installed costs of controls and communications	= \$1,000,000
Pump operating costs	= \$.01/KWh
Maintenance	= 2.0% of installed cost
Installed cost of piping	= Fig. 19.0

#### IV.A.2. Example cash flow

The following is an excerpt from Appendix D where a detailed development of this example is given. The following example situation was developed for cash flows in the years they occur for an initial investment of \$1000.00, maintenance expense of \$1000.00/year

and \$2000.00/year revenue.

Table 1.0. \$1000 Investment Cash Flow Table.

YEAR	CI	MAINT & OP	TAX	PRTX	FC	REV	EF
1	1000.0	1045.0	402.0	20.0	91.0	2090.0	1.045
2		1092.0	445.4	20.0	91.0	2184.0	1.092
3		1141.0	485.7	20.0	91.0	2282.2	1.141
4		1192.5	524.5	20.0	91.0	2385.0	1.192
5		1246.2	561.6	20.0	91.0	2492.4	1.246
6		1302.3	597.9	20.0	91.0	2604.5	1.302
7		1360.9	627.2	20.0	91.0	2721.7	1.360
8		1422.2	657.8	20.0	91.0	2844.2	1.422
9		1486.1	689.8	20.0	91.0	2972.2	1.486
10		1552.9	723.2	20.0	91.0	3105.9	1.552

where

CI = capital investment

FC = finance charges + dividends

$$= (.40 \times CI \times \text{BROI}) + (.30 \times CI \times \text{CROI}) + (.30 \times \text{PROI})$$

BROI = bond rate of interest

CROI = common rate of interest

PROI = preferred rate of interest

per cent bonds = 40%

per cent preferred = 30%

per cent common = 30%

$$\begin{aligned} \text{PRTX} &= \text{property taxes} \\ &= 2.0\% \times \text{CI} \\ \text{TAXES} &= \text{income taxes} \end{aligned}$$

#### IV.A.3. Depreciation scheme

The following method was used to calculate a dual declining balance depreciation scheme.

Year	Undepreciated balance	Depreciation
1	CI(1)	CI x 2.0 x SLR = dep(1)
2	CI(2) = CI(1) - dep(1)	CI(2) x 2.0 x SLR = dep(2)
3	CI(3) = CI(2) - dep(2)	CI(3) x 2.0 x SLR = dep(3)
.	.	.
.	.	.
.	.	.
N	CI(N) = CI(N-1) - dep(N-1)	CI(N) x 2.0 x SLR = dep(N)

where

$$\begin{aligned} \text{SLR} &= \text{straight line depreciation rate} \\ &= \frac{1}{\text{Project life (years)}} \end{aligned} \quad (21)$$

In this scheme we switch to a straight line depreciation scheme when the undepreciated balance divided by the number of years remaining in the life of the project is greater than the dual declining balance depreciation value.

#### IV.A.4. Income tax calculations

Knowing the depreciation schedule, the income tax calculations

may now be carried out. A tax rate of 50% of net income is used.

$$\begin{aligned} \text{Taxes}(N) = & [(R(N) - (OP(N) + \text{MAINT}(N) + \text{DEP}(N) + \text{PT}(N) \\ & + \text{Bond interest}(N))] \times .50 \quad (22) \end{aligned}$$

where

N = any one year in the project life from 1 through 30  
inclusive

R(N) = revenue in any one year  
=  $R(1 + k)^N$

FC(N) = finance charges for any one year

OP(N) = operating expenses in any one year  
=  $OP(1 + k)^N$

MAINT(N) = maintenance expenses in any one year  
=  $\text{MAINT}(1 + k)^N$

DEP(N) = depreciation expense (outlined in section IV.A.3)

PT(N) = property tax in any one year

Bond Interest = interest paid on the bonds only to finance  
part of the project

#### IV.A.5. Net cash flow

The face value net cash flow may now be determined.

$$\begin{aligned} \text{NCF}(N) = & [R(N) - (OP(N) + \text{MAINT}(N) + \text{INCOME TAXES}(N) + \text{PT}(N) \\ & + \text{FC}(N) + \text{CR})] \quad (23) \end{aligned}$$

where



NCF(N) = net cash flow for any one year

CR = capital recovery

and

$$PW_{\circ}(N) = \frac{NCF(N)}{(1+i)^N} \quad (24)$$

where

$PW_{\circ}(N)$  = the present worth at time zero for any one year (N).

thus

$$PVI = PW_{\circ}(1) + PW_{\circ}(2) + PW_{\circ}(3) + \cdots + PW_{\circ}(30) \quad (25)$$

where

PVI = cumulative present value of income at  $i\%$  for  
a project life of 30 years.

This type of cash flow analysis was conducted for the systems represented in figures 20 through 25. The computer program HOTNCOLD subroutine CASH was developed using the technique outlined in the above sections to process the cash flow calculations and prepare the plots therefrom.

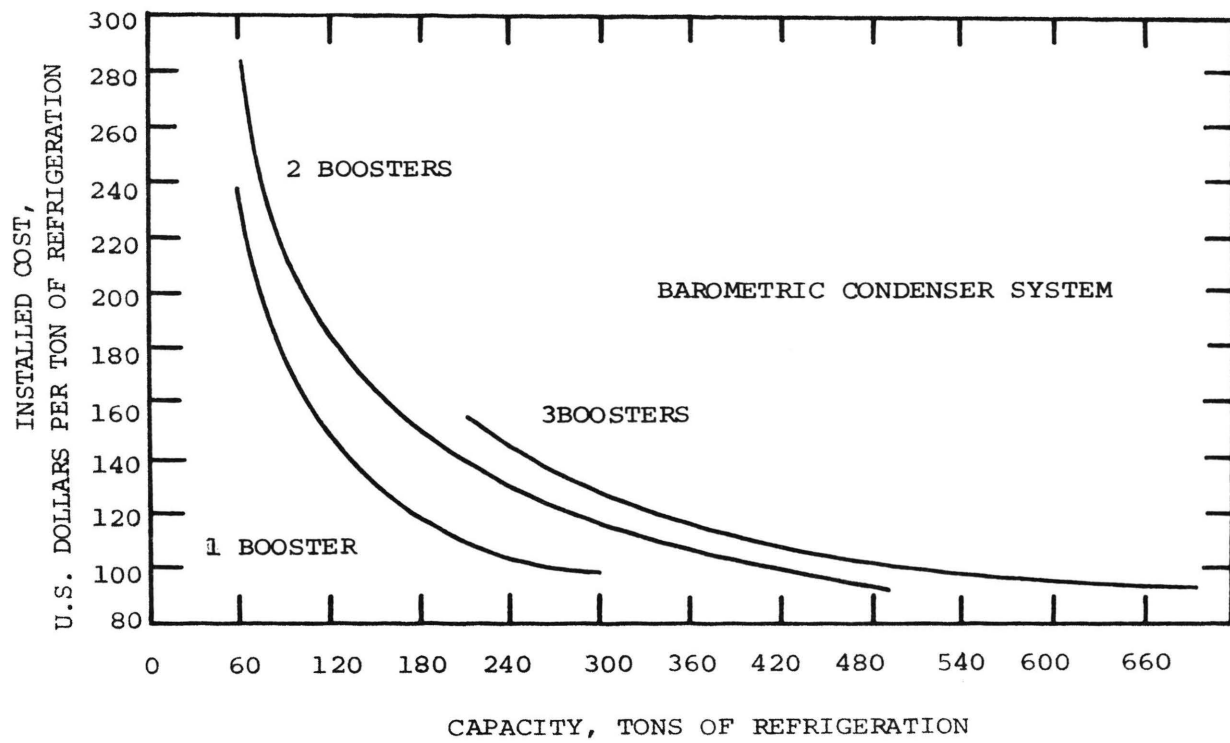


Fig. 18.0 Installed Cost of Refrigeration Systems vs. Refrigeration Capacity.

The following figure (Fig. 19.0) was developed from cost projections from pipeline data given for the years 1951 through 1967. These data were projected to the year 1974 to give the curve represented in Fig. 19.0. These data were published by the Federal Power Commission in the March 1969 issue of Pipeline Engineer. With the shortage of fabricated steel pipe there is no accurate way of determining the actual price of the pipe in March 1974. Although the graph does most probably represent the range in which the pipe costs would fall if pipe were available.

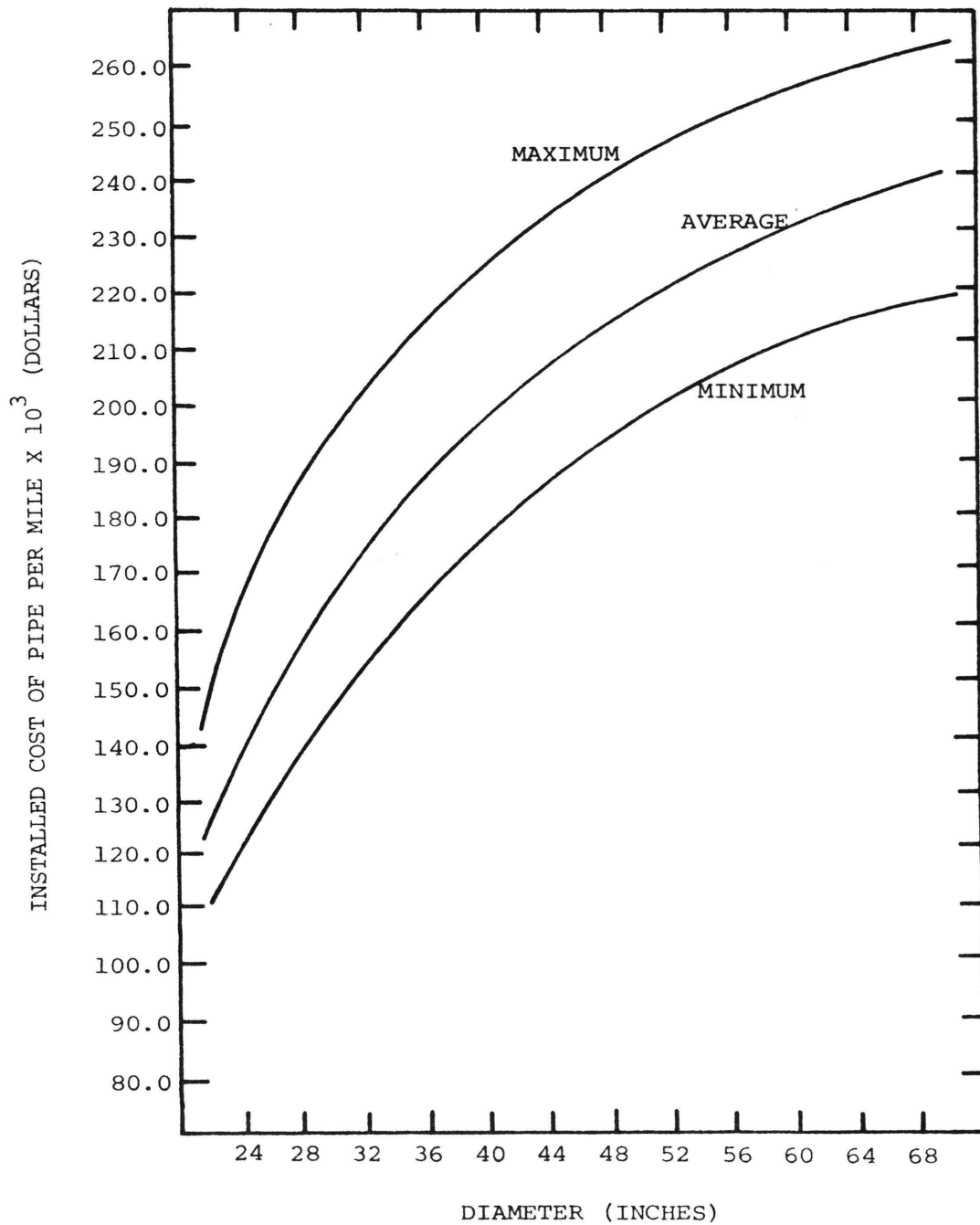


Fig. 19.0. Installed Cost of Pipe vs. Diameter.

#### IV.B. Results of the Cash Flow Analysis

The following figures are the results of the calculations done in subroutine CASH in the program HOTNCOLD. The graphs illustrate the present value net cumulative cash flow for a two pipe (two in each direction) hot water and cold water delivery system. For example, it is seen from figure 20.0 that the 10% cumulative present worth of the net cash flow for a 50 mile installation at a mass rate of flow of  $56 \times 10^6$  lbm/hr (m2) is \$52,000,000. At the distance where the line crosses the 0.0 point the system would have an internal rate of return of 10.0%. Above the dashed line represents money earned above 10.0%, below the dashed line represents money short of 10.0% internal rate of return.

The following symbols key the mass rates of flow on figures 20 through 25.

$$\begin{aligned}
 m1 &= 57 \times 10^6 \text{ lbm/hr} \\
 m2 &= 56 \times 10^6 \text{ lbm/hr} \\
 m3 &= 55 \times 10^6 \text{ lbm/hr} \\
 m4 &= 54 \times 10^6 \text{ lbm/hr} \\
 m5 &= 53 \times 10^6 \text{ lbm/hr} \\
 m6 &= 52 \times 10^6 \text{ lbm/hr} \\
 m7 &= 51 \times 10^6 \text{ lbm/hr} \\
 m8 &= 50 \times 10^6 \text{ lbm/hr} \\
 m9 &= 48 \times 10^6 \text{ lbm/hr} \\
 m10 &= 48 \times 10^6 \text{ lbm/hr}
 \end{aligned}$$

$$m_{11} = 47 \times 10^6 \text{ lbm/hr}$$

$$m_{12} = 46 \times 10^6 \text{ lbm/hr}$$

$$m_{13} = 45 \times 10^6 \text{ lbm/hr}$$

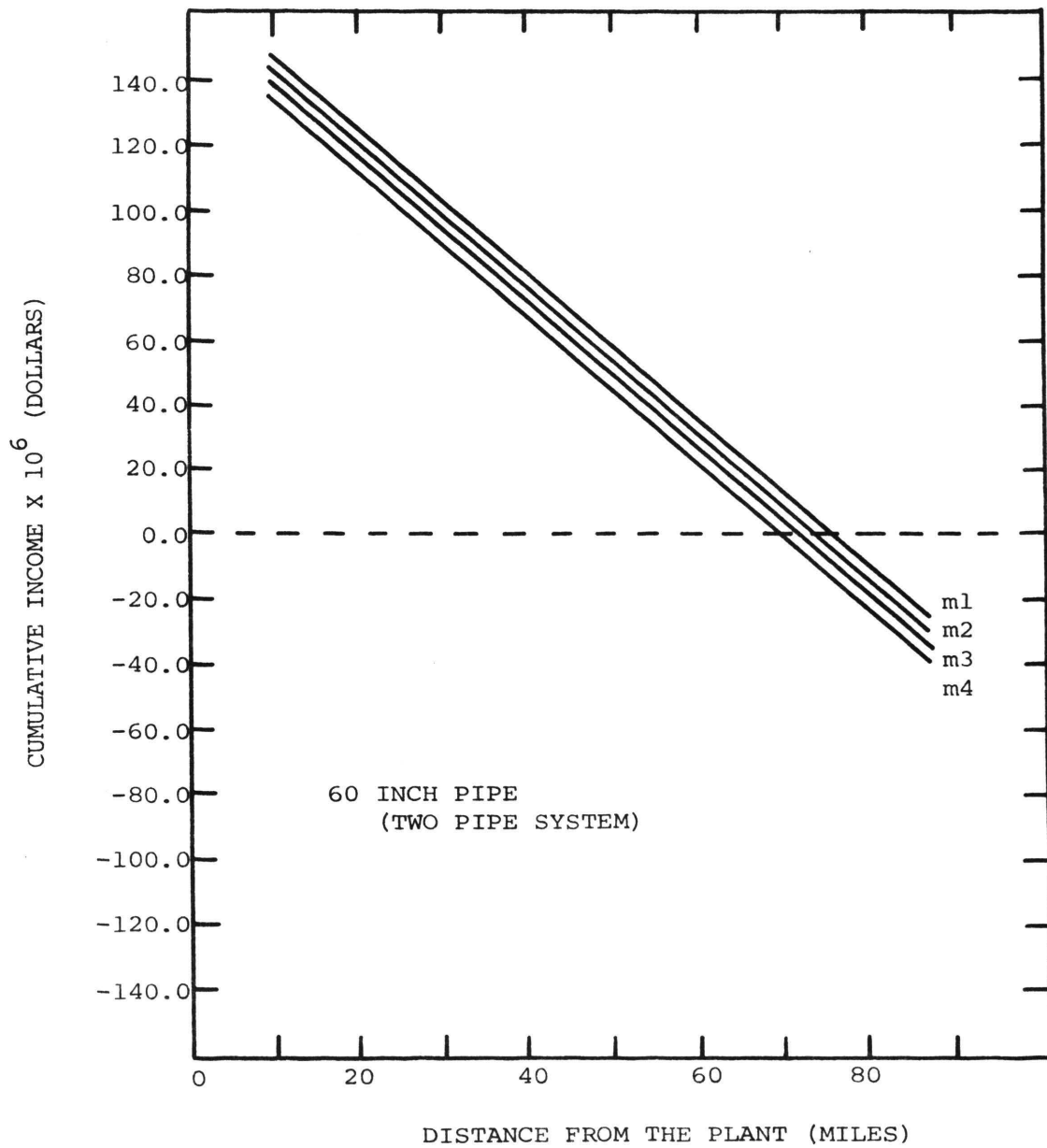


Fig. 20.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years. m1-m4

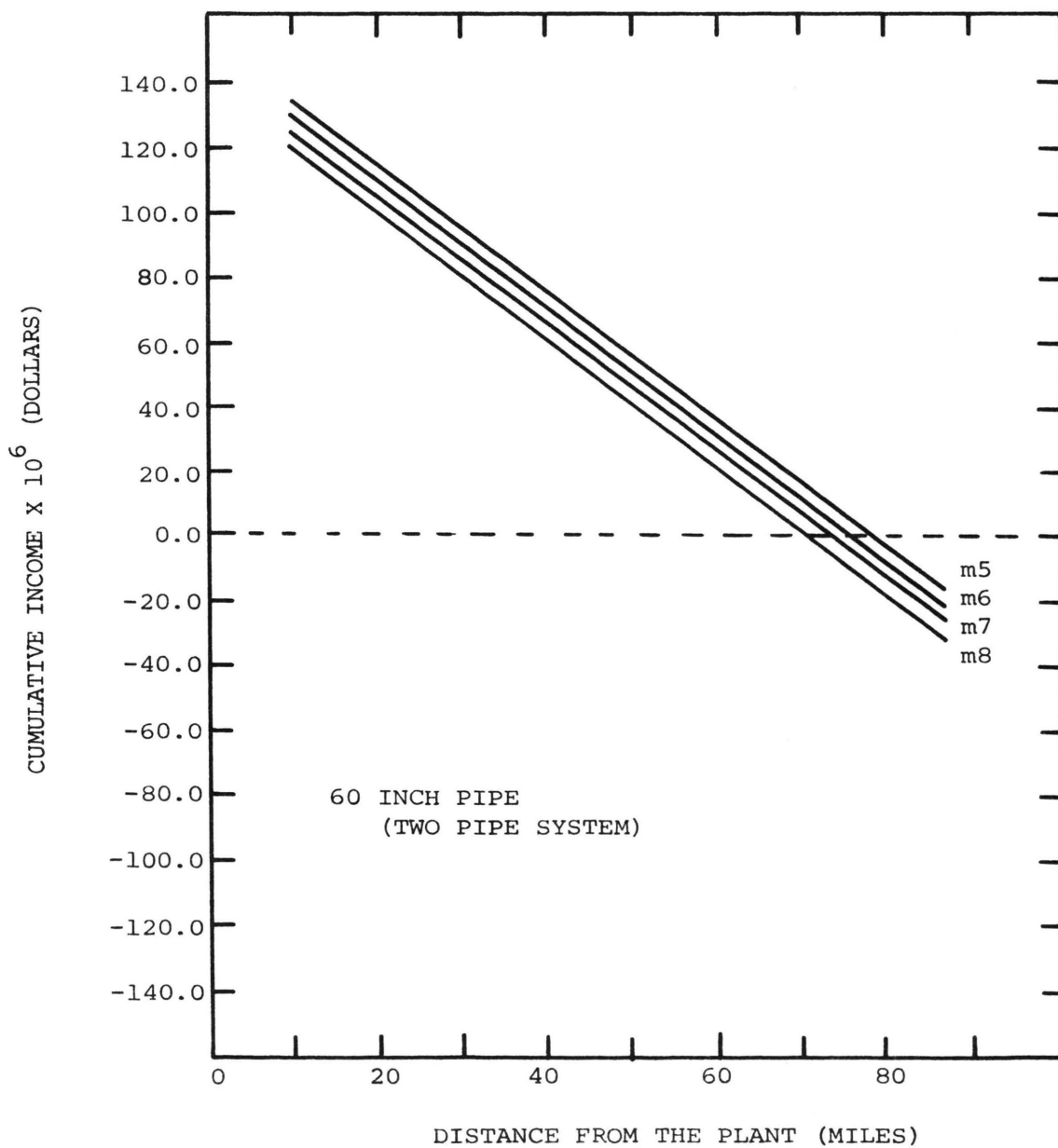


Fig. 21.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years. m5-m8



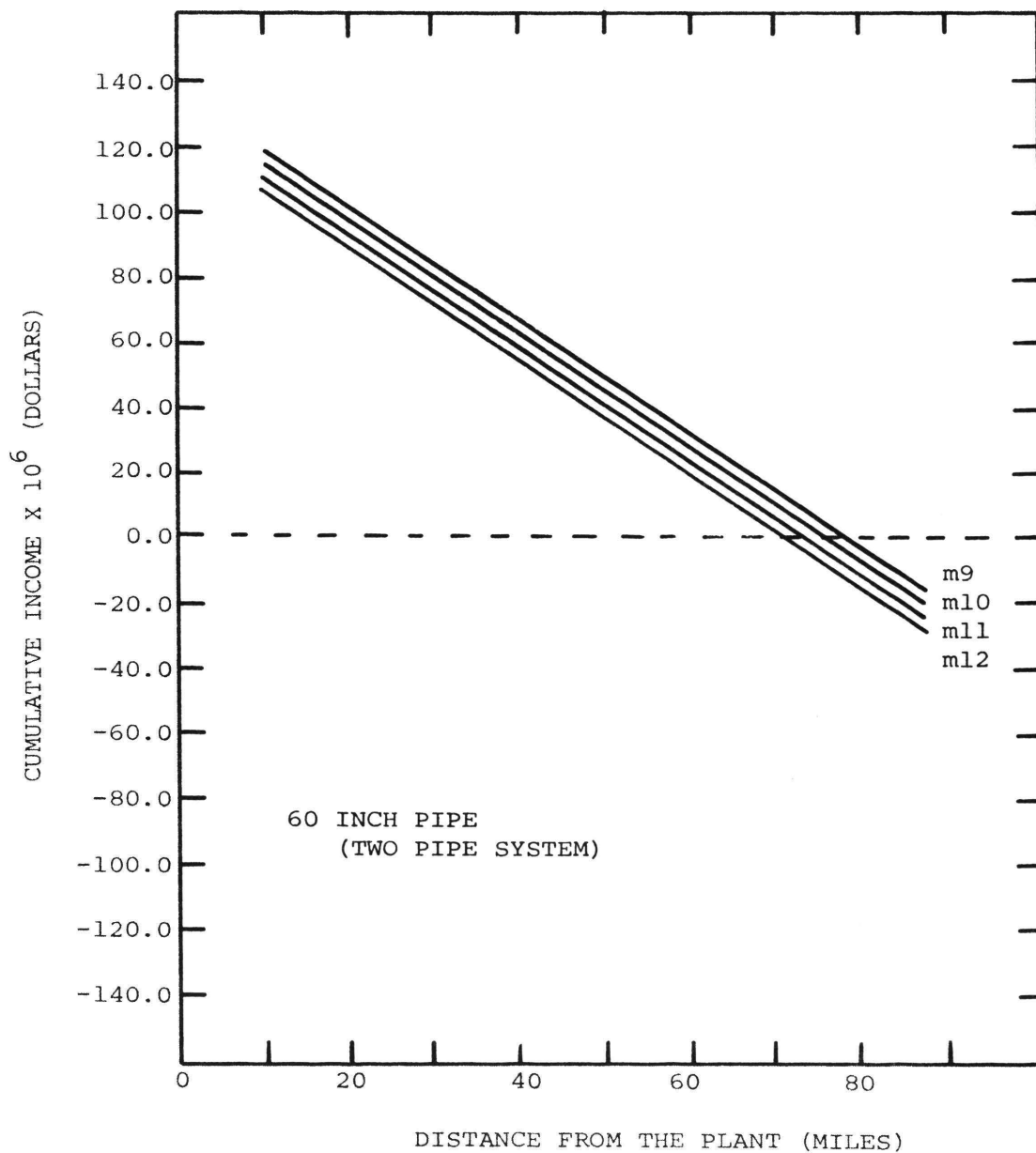


Fig. 22.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years. m9-m12

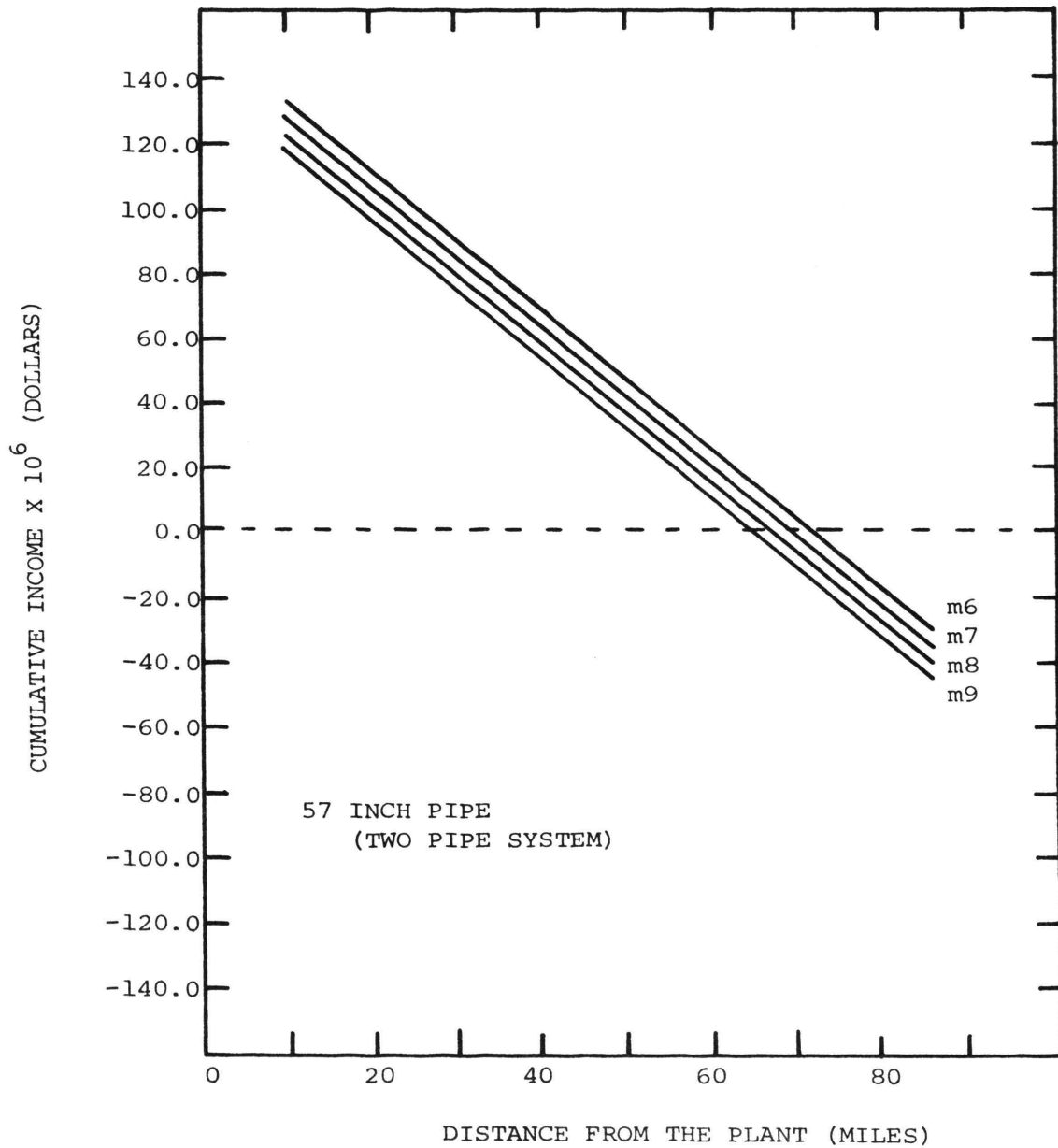


Fig. 23.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years. m6-m9

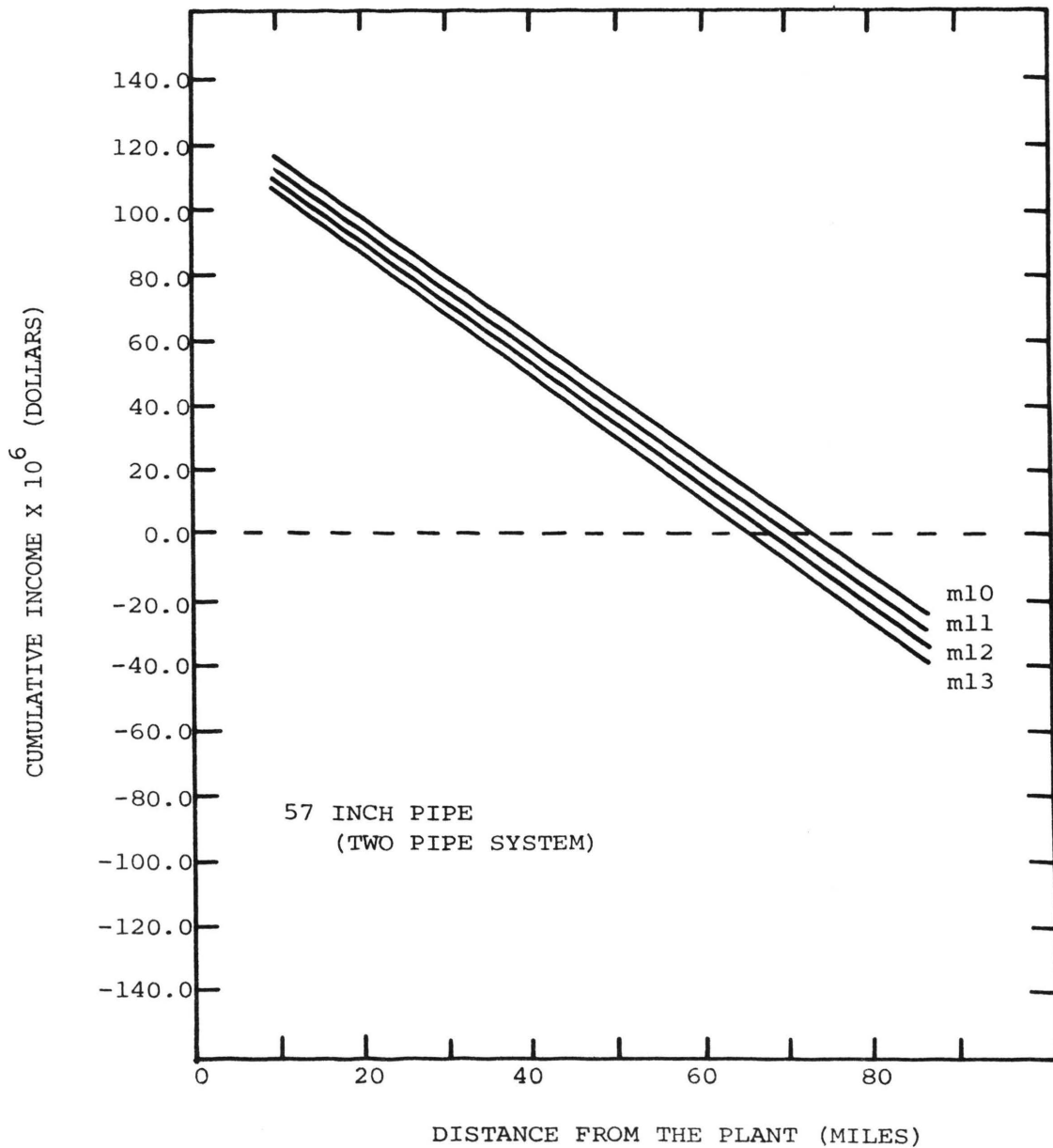


Fig. 24.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years. m10-m13

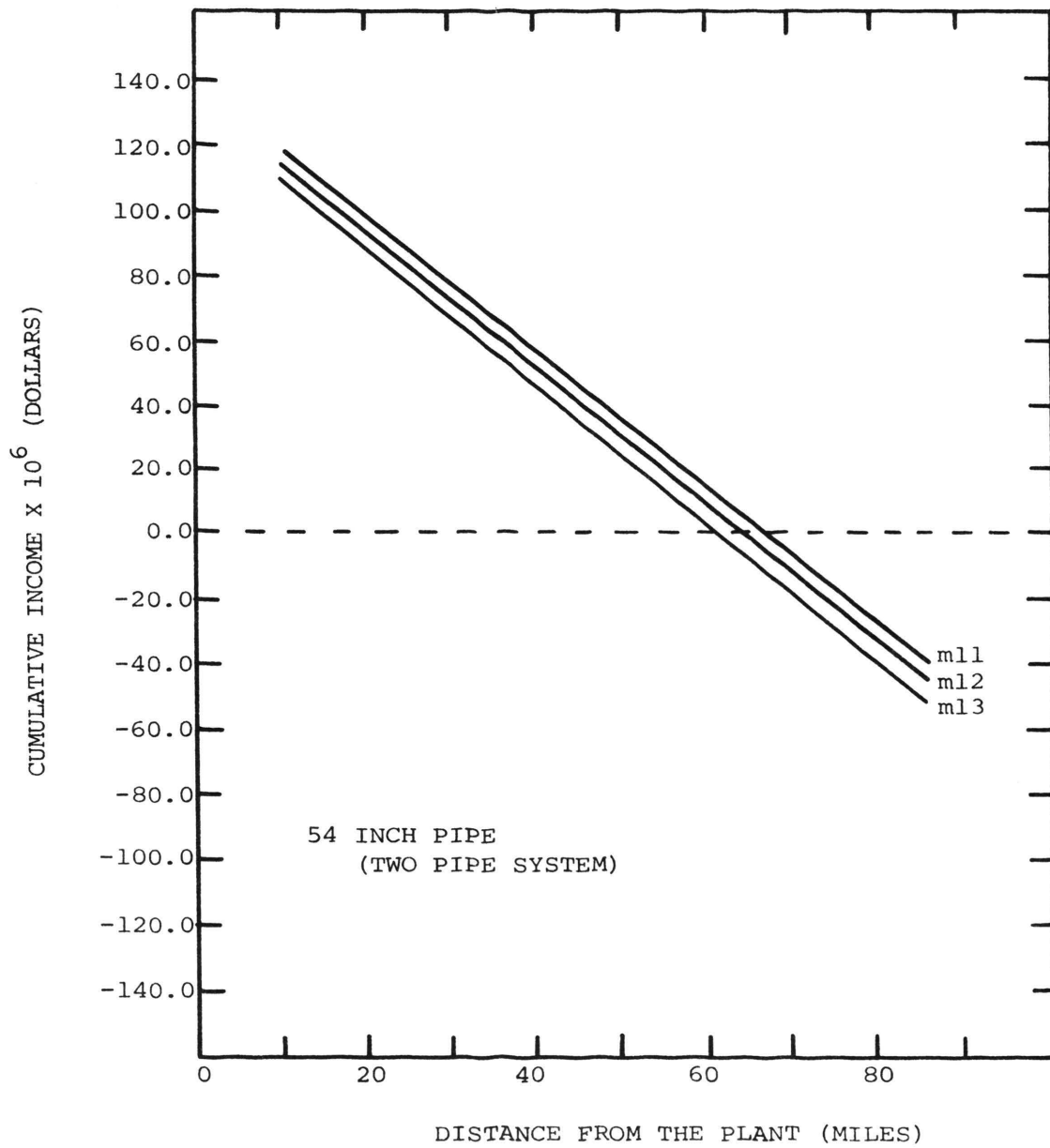


Fig. 25.0. Present Value of Cumulative Income at 10% for a 30 Year Life vs. Years. m11-m13

## V. DISCUSSION OF RESULTS

Depending on the mass rate of flow and pipe diameter, it is possible to realize at least a 10% internal rate of return at distances from the load center between 50 and 75 miles. At distances greater than this range internal rates of return less than 10% would be realized. At distances less than this range internal rates of return greater than 10% would be realized.

It must be remembered that the most significant assumption made in this investigation was the fact that the system would operate at full load capacity for the heating period of four months and a cooling period of three months. Hence, these systems are being presented as supplemental in nature to existing heating and refrigeration systems. The heating and cooling network is designed to handle a major portion of the steady load season, which is usually in the middle of the summer and winter seasons. If the systems were to be applied on a year round basis, the load requirements for the local area would have to be determined and the water flow rate adjusted according to the varying load requirements, in variable seasons as the spring and fall. However, even if these systems were used as suggested herein, that is, as supplemental systems, the energy savings and economic benefit would still be quite high.

The efficient utilization of energy from high temperature gas cooled reactors not only has the attractive point of utilizing much of the energy that would be otherwise wasted; but, also the

added advantage of conserving fossil fuel resources, that would ordinarily have been required to supply the heating and air conditioning service during high load periods.

The fossil fuel savings would of course be equivalent to the energy consumed by the load center during operation of the waste heat systems. For example, if the load required  $3 \times 10^9$  BTU/hr for a heating season of 4 months and 100,000 tons of refrigeration for a 3 month cooling season, a savings would be realized for any one of the following sources of energy:

Natural gas

HEATING

$$3.0 \times 10^9 \frac{\text{BTU}}{\text{hr}} \times 2880 \text{ hrs} \times \frac{\text{ft}^3}{(1000 \text{ BTU}) (.8)} = 10.8 \times 10^9 \text{ ft}^3$$

COOLING

$$100000 \text{ tons} \times \frac{12000 \text{ BTU}}{\text{HR} - \text{ton}} \times 2160 \text{ hrs} \times \frac{\text{ft}^3}{(1000 \text{ BTU}) (.5)} = 5.18 \times 10^9 \text{ ft}^3$$

Total =  $15.98 \times 10^9 \text{ ft}^3$  natural gas

No. 2 Fuel oil

Using  $19110.0 \frac{\text{BTU}}{\text{lbm}}$

Savings = 1,749,800 barrels

Electric

Savings = 3,280,000 megawatt-hours

It is clearly seen that considerable quantities of fossile fuels can

be conserved, in addition, a profit can be realized by the installation of such a system.

As a suggestion for further study, an investigation into the load following characteristics and the subsequent impact on the economic development would be of considerable interest. In addition the investigation of the utilization of this energy in agricultural and industrial processes (for example, grain drying operations) would merit further study.

## VI. CONCLUSIONS

It is possible to service a district heating and cooling network by utilizing the rejected heat from a direct cycle high temperature gas cooled reactor as designed by the General Atomic Company.

The objective of this thesis was to investigate the feasibility of utilizing the rejected energy from the direct cycle HTGR to serve a district heating and cooling network. The objective has been accomplished, insomuch as the results clearly indicate that with the advent of the direct cycle HTGR, waste heat utilization will approach a more realistic solution. New technological advancements such as the direct cycle HTGR will provide the opportunity of increasing our energy utilization efficiency.

Since that which moves the technological society is inventiveness, magnified and implemented by an energy base, it is the techno-sociological responsibility of energy system designers to efficiently and equitably utilize our energy resources. In so doing, an optimized system of environmental, technological and sociological benefits will be realized.

The results of this investigation indicate that the state of the art in reactor design is reaching a point where the maximum energy utilization efficiency may be realized.



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## VITA

John J. Blase was born February 13, 1947 in Girardville, Pennsylvania. He was raised in Girardville which is located in the Anthracite coal mining region. After completing his high school education at Cardinal Brennan High School, he attended the Academy of Aeronautics in New York City where he earned his Associate in Applied Science Degree in aircraft design. He also attended Parks College - St. Louis University where he received his B.S. in Aerospace Engineering.

Mr. Blase worked in the capacity of liaison engineer for Grumman Aircraft Engineering Company on the Apollo Project Lunar Module for a period of two years. He also held the position of Mechanical Engineer with the Environmental Protection Agency for two years.

He is President of the UMR Chapter of the American Nuclear Society, Vice President of the Nuclear Engineering and Science Honor Society, and an associate member of the National Society of Professional Engineers. Mr. Blase is married to the former Karen Wolf of St. Louis, Missouri.

## APPENDIX A

## REVIEW OF LITERATURE

The utilization of low temperature waste heat from steam-electric power plants has always been a difficult task. The temperature of the rejected heat is relatively low (around 105°F), thus making the utilization of this energy quite difficult. There have been significant efforts, however, involved in utilizing waste energy. An entire range of heating<sup>[3][18]</sup> and agricultural<sup>[4]</sup> uses have been proposed. Some have met with success and many have not.

A unique approach to the use of this low value energy has been made by W. Martinovsky<sup>[13][14]</sup> of the Odessa Technical Institute in the Soviet Union. In 1953 Martinovsky proposed<sup>[13]</sup> the rejection of low value waste heat to a steam jet refrigeration cycle. In his proposal the steam jet cycle did not use water as a refrigerant as is the usual case, instead it was suggested that a freon or similar refrigerant be utilized in the steam jet refrigerating process. The low condenser temperatures of the steam jet cycle limited the use of such a system because of the large heat exchanger surfaces required at the condenser end of the cycle. The utilization of waste energy from steam-electric cycles is indeed worthy of future investigation when one considers the number of such plants in existence.

The advent of high temperature gas cooled reactors as designed by General Atomic, has added a new dimension to the possibilities

of utilizing the heat rejected from the nuclear-electric energy cycle. The only helium cooled nuclear reactor in operation in the United States at this time is the 330 MWe unit operated by Public Service Company of Colorado. This unit utilizes a conventional steam-electric cycle, coupled to a helium-water steam generator. A new design under consideration at this time by General Atomic is the direct cycle high temperature gas (helium) cooled reactor<sup>[11]</sup>. In this machine, the helium is heated in the reactor core and then expanded directly through a gas turbine which consequently turns the electric generator<sup>[11]</sup>. The attractive feature of this cycle is the temperature at which the waste heat is rejected. Rejection temperatures across the precooler stage of the cycle is from 470°F to 105°F<sup>[11]</sup>. Immediately it can be seen that this high value waste heat has many utilization possibilities. In fact, much research into the effective utilization of this energy is underway at the General Atomic facility in San Diego, California.

Rejection temperatures in this range could provide sufficiently high temperature input to generate low energy steam which may in turn power a water cycle series of steam jet refrigeration units.<sup>[8]</sup> This chilled water could in turn be used either in industrial processes or it could provide for a district refrigeration service (air conditioning). Chilled and heated water district heating and cooling systems have been in existence for many years<sup>[1]</sup>, and, therefore, this technological consideration is neither surprising

nor new. However, the great distance of nuclear power plants from load centers<sup>[18]</sup> increases the difficulty involved in transporting heated and chilled water to the load center. The pipeline technology required to move large quantities of water has been available to the oil and natural gas industries for many years<sup>[9][17]</sup>.

The object of this investigation is the determination of the technical and economic feasibility of transporting large quantities of heated and chilled water to a concentrated load center by using the rejected heat from the high temperature gas cooled reactor as the energy source.

APPENDIX B

FORTRAN IV COMPUTER PROGRAM LISTING

0001

SUBROUTINE TECH

```

C
C***** TECH DOES ALL PRESSURE DROP AND HEAT TRANSFER CALCULATIONS *****
C

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0002 REAL K1
0003 REAL K2
0004 REAL K3
0005 REAL MLIQ
0006 DIMENSION E(180),T(180)
0007 DIMENSION T1A(100),T2A(100),JBA(100),DISA(100)
0008 DIMENSION T3A(100),T4A(100),HEATA(100)
0009 COMMON AT(18),PR(18),KV(18)
0010 J=1
0011 I=3
0012 DO 1001 L=1,100
0013 T1A(L)=0.0
0014 T2A(L)=0.0
0015 JBA(L)=0.0
0016 DISA(L)=0.0
0017 T3A(L)=0.0
0018 T4A(L)=0.0
0019 HEATA(L)=0.0
0020 1001 CONTINUE
0021 ADIS=0.0
0022 ENTHY=117.95
0023 ENTHW=166.09
0024 P1=3.14115927
0025 I=3
0026 J=1
0027 READ(J,7000)AMHP
0028 READ(J,7003)AA,AE
0029 READ(J,7001)AINC,Z,FF,SV,ENTH1,ENTH3
0030 READ(J,7004)AKK,ANUW,ANPR,K1,K2,K3,N,DA
0031 E=AE
0032 F=0.0
0033 Q=199270.0
0034 DO 20 I=1,6
0035 READ(J,1010)AT(I),PR(I),KV(I)
0036 20 CONTINUE
0037 DO 20 II=1,N
0038 READ(J,8000)E(II),T(II)
0039 20 CONTINUE
0040 MLIQ=48.0E+06
0041 WRITE(I,8999)
0042 WRITE(I,9000)ENTH1,ENTH3,K1,K2,K3,AKK,ANUW,ANPR,Q,X,FF
0043 GO TO 7
0044 9 CONTINUE
0045 DO 820 IC=1,1A
0046 WRITE(I,9004)T1A(IC),T2A(IC),JBA(IC),T3A(IC),T4A(IC),HEATA(IC),DIS
-A(IC)
WRITE(I,9007)QBA(IC),HEATA(IC),DISA(IC)
0047 820 CONTINUE
0048 IF(D.LT.60.10)GO TO 3
0049 7 MLIQ=MLIQ-0.50E+06
0050 IF(MLIQ.LT.10.00E+06) GO TO 100
0051 D=63.0
0052

```



```

0053      3 D=D-3.0
0054      IF(D.LT.40.0)GO TO 7
0055      L=0.
0056      DD=D/12.0
0057      AREA=(PI*D**2.)/(4.0*144.0)
0058      VEL=MLIQ/(AREA*62.4)
0059      AVEL=VEL/3600.
0060      CALL PRESS(AREA,FF,MLIQ,D,S,Y,DELPI)
0061      CALL HOKSE(DELPI,MLIQ,AMHP,HP,PLUC,ENTHP)
0062      IF(PLUC.LT.10.0)GO TO 7
0063      DIS=0.0
0064      ENTHZ=0.0
0065      ENTHX=0.0
0066      ENTH2=0.0
0067      ENTH4=0.0
0068      ENTHX=ENTH1+ENTHX+ENTHP
0069      ENTHZ=ENTH1+ENTHZ+ENTHP
0070      ENTH2=ENTH1+ENTH2+ENTHP
0071      ENTH4=ENTH3+ENTH4+ENTHP
0072      120 DIS=DIS+AINC
0073      IF(DIS.GT.AA) GO TO 9
0074      ZZ=0.0
0075      CALL TEMP(E,T,ENTH2,J,N,TIN1)
0076      CALL TEMP(E,T,ENTH4,J,N,TIN2)
0077      CALL TEMP(E,T,ENTHX,J,N,TIN4)
0078      CALL TEMP(E,T,ENTHZ,J,N,TIN3)
0079      QB=(ENTH3-ENTH2)*MLIQ
0080      QB=QB/12000.0
0081      HEAT=(ENTHX-ENTHY)*MLIQ
0082      IF(QB.LT.9000.0) GO TO 3
0083      IF(DIS.GT.AINC) GO TO 170
0084      WRITE(I,8998)
0085      WRITE(I,9001)
0086      WRITE(I,9002)MLIQ,DELPI,D,AVEL,THK
0087      WRITE(I,9003)HP,PLUC
0088      WRITE(7,9006)MLIQ,D,PLUC
0089      IF(DIS.GT.AINC) GO TO 170
0090      WRITE(I,9005)
0091      IA=0
0092      170 CONTINUE
0093      IA=IA+1
0094      T3A(IA)=TINA
0095      T4A(IA)=TINB
0096      HEATA(IA)=HEAT
0097      T1A(IA)=TIN1
0098      DISA(IA)=DIS
0099      QBA(IA)=QB
0100      T2A(IA)=TIN2
0101      L=L+1
0102      IF(L.GT.52) GO TO 40
0103      GO TO 50
0104      40 WRITE(I,8998)
0105      L=0
0106      50 CONTINUE
0107      130 CALL TEMP(E,T,ENTH2,J,N, TIN1)
0108      CALL TEMP(E,T,ENTH4,J,N, TIN2)

```

```

0109 CALL TEMP(E,T,ENTHX,J,N,TINA)
0110 CALL TEMP(E,T,ENTHZ,J,N,TINB)
0111 C=0.0
0112 B=.3
0113 CALL HTRAN(TIN2,K1,K2,K3,VEL,DD,ANUW,ANPR,B,AKW,C,HT2,R1,R2,R3,THK
-)
0114 CALL HTRAN(TINA,<K1,K2,K3,VEL,DD,ANUW,ANPR,B,AKW,C,HTA,R1,R2,R3,THK
-)
0115 B=.4
0116 C=EE
0117 CALL HTRAN(TINI,K1,K2,K3,VEL,DD,ANUW,ANPR,B,AKW,C,HT1,R1,R2,R3,THK
-)
0118 CALL HTRAN(TINB,K1,K2,K3,VEL,DD,ANUW,ANPR,B,AKW,C,HTB,R1,R2,R3,THK
-)
0119 HTA=HTA*AINC*5280.0/Z
0120 HTB=HTB*AINC*5280.0/Z
0121 HT1=HT1*AINC*5280.0/Z
0122 HT2=HT2*AINC*5280.0/Z
0123 THK=THK*12.0
0124 ENTH2=-(HT1/MLIQ)+ENTH2
0125 ENTH4=-(HT2/MLIQ)+ENTH4
0126 ENTHX=-(HTA/MLIQ)+ENTHX
0127 ENTHZ=-(HTB/MLIQ)+ENTHZ
0128 ADIS=ADIS+AINC/Z
0129 IF(ADIS-(PLOC-.1)) 400,140,1+0
0130 140 ENTH2=ENTH2+ENTHP
0131 ENTH4=ENTH4+ENTHP
0132 ENTHX=ENTHX+ENTHP
0133 ENTHZ=ENTHZ+ENTHP
0134 ADIS=0.0
0135 400 ZZ=ZZ+1.0
0136 IF(ZZ.GE.Z) GO TO 120
0137 GO TO 130
0138 1010 FORMAT(3F10.5)
0139 7000 FORMAT(F12.3)
0140 7001 FORMAT(6F12.5)
0141 7003 FORMAT(2F12.5)
0142 7004 FORMAT(6F8.5,13,F6.2)
0143 3000 FORMAT(2F10.3)
0144 8998 FORMAT(1H1,////)
0145 8999 FORMAT(1H1,////////////////////////////////////)
0146 9000 FORMAT('PLANT OUTLET ENTHALPY =',F9.6, ' BTU/L3M',///,'LOAD OUTLET
-ENTHALPY =',F9.6, ' BTU/L3M',///,'THERMAL CONDUCTIVITY OF:',F9.2,
-0X,'PIPE =',F8.5, ' BTU/HR-FT-DEGF',/,20X,'INSULATION =',F8.5,
-, ' BTU/HR-FT-DEGF',/,20X,'SOIL =',F8.5, ' BTU/HR-FT-DEGF',/
-,20X,'WATER =',F8.5, ' BTU/HR-FT-DEGF',///,'KINEMATIC VISCOSI
-TY OF THE WATER =',F8.5, ' FT SQ/HR',///,'PRANDTL NUMBER =',F4.2,/
-//,'REFRIGERATION AVAILABLE AT THE PLANT =',F7.0, ' TONS',///,'NUMB
-ER OF PIPES IN ONE DIRECTION =',F3.0,///,'PIPE FRICTION FACTOR (MO
-DULY DETERMINATION) =',F5.3)
0147 9001 FORMAT(' MASS RATE PRESSURE LOSS PIPE DIA. VELOCITY INSULATION
-',/, ' OF FLOW PER MILE (INCHES) (FT/SEC) THICKNESS(IN.)'
-)
0148 9002 FORMAT(E12.6,2X,E9.3,4X,F5.2,4X,F8.3,4X,F6.3)
0149 9003 FORMAT(/, ' HP/PIPE/MILE =',F3.2, ' DIS BETWEEN PUMPS =',F5.1,/)
0150 9004 FORMAT(4X,F6.2,7X,F6.2,6X,F9.2,6X,F6.2,6X,F6.2,6X,E12.6,6X,F8.4)

```

```

0151            9005 FORMAT(' TEMP LEAVING TEMP LEAVING REFRIGERATION TEMP LEAVING TEM
              -P LEAVING HEAT DISTANCE FROM ' ,/, ' REF PLANT REF
              - LOAD AVAILABLE HEAT PLANT HEAT LOAD AVAILABLE
              -THE LOAD CENTER ' ,/, ' (DEG F) (DEG F) (DEG F) (DEG F) (TONS)
              - (DEG F) (DEG F) (BTU/HR) (MILES) ')
0152            9006 FORMAT(E13.6,F5.2,F5.1)
0153            9007 FORMAT(F9.2,E14.6,F6.1)
0154            100 RETURN
0155            END
    
```

```

0001            SUBROUTINE PRKV(T,PRAN,KINV)
              C ***** PRKV DOES A TABLE LOOK UP FOR PRANDTL NUMBER AND KINEMATIC VIS *****
              C
0002            COMMON AT(10),PR(10),KV(10)
0003            DO 10 I=1,6
0004            IF((T.GE.AT(I)).AND.(T.LT.AT(I+1))) GO TO 40
0005            10 CONTINUE
0006            40 A=AT(I+1)
0007            B=AT(I)
0008            PA=PR(I+1)
0009            PB=PR(I)
0010            KA=KV(I+1)
0011            KB=KV(I)
0012            PRAN =((T-B)/(A-B))*(PA-PB)+PB
0013            KINV=((T-B)/(A-B))*(KA-KB)+KB
0014            RETURN
0015            END
    
```

```

0001            SUBROUTINE PRESS(AREA,FF,MLIQ,D,SV,DELP)
              C ***** PRESS CALCULATES PRESSURE DROP PER MILE *****
              C
0002            REAL MLIQ
0003            G=MLIQ/AREA
0004            DELP=((FF*5280.)/D)*SV*((G/100000.0)**2)
0005            RETURN
0006            END
    
```

0001

SUBROUTINE TEMP(E,T,ENTH,J,N,TR)

```
C
C***** TEMP IS A TABLE LOOK UP FOR TEMPERATURE GIVEN ENTHALPY *****
C
```

0002

DIMENSION E(180),T(180)

0003

NN=N-1

0004

DO 30 I=1,NN

0005

IF((ENTH.GE.E(I)).AND.(ENTH.LT.E(I+1))) GO TO 40

0006

30 CONTINUE

0007

40 TIN=T(I)

0008

EN=E(I)

0009

ENN=E(I+1)

0010

B=T(I+1)

0011

TR=((EN-ENTH)/(EN-ENN))\*(B-TIN)+TIN

0012

RETURN

0013

END

0001  
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0053

```

SUBROUTINE HCPL0T
C***** HCPL0T PLOTS THE DATA FROM THE TECH ROUTINE *****
C
DIMENSION H(50),R(50),DI(50)
CALL PENPOS('BLASE',5,0)
ZA=25.0
ZB=0.0
A)=30.0
B)=63.0
1 G)=GD-3.0
IF(GD.LT.AD)GO TO 300
REWIND 8
L=200
LA=15
30 READ(8)Q,DIA,PL0C
IF(Q.LT.5.0)GO TO 100
DO 20 I=1,44
READ(8)A,B,DI(I)
H(I)=B*1.0E-07
20 CONTINUE
AW=GD+0.5
AZ=GD-0.5
IF((DIA.GT.AW).OR.(DIA.LT.AZ))GO TO 30
L=L+1
WRITE(3,25)DIA
IF(L.LT.LA)GO TO 50
IF(L.EQ.LA)CALL ENDPLT
L=0
CALL NEWPLT(0.5,2.0,6.0)
CALL ORIGIN(0.0,100.0)
CALL XSCALE(0.0,120.0,4.5)
CALL YSCALE(ZA,300.0,6.0)
CALL XAXIS(10.0)
CALL YAXIS(25.0)
30 CALL XYPLT(DI,H,44,1,-1)
GO TO 30
100 IF(L.LT.LA) CALL ENDPLT
REWIND 8
L=200
40 READ(8)Q,DIA,PL0C
IF(Q.LT.5.0)GO TO 200
DO 120 I=1,44
READ(8)A,B,DI(I)
R(I)=A*1.0E-03
120 CONTINUE
IF((DIA.GT.AW).OR.(DIA.LT.AZ))GO TO 40
L=L+1
IF(L.LT.LA) GO TO 150
IF(L.EQ.LA)CALL ENDPLT
L=0
CALL NEWPLT(0.5,2.0,6.0)
CALL ORIGIN(0.0,25.0)
CALL XSCALE(0.0,120.0,4.5)
CALL YSCALE(ZB,75.0,6.0)
CALL XAXIS(10.0)

```

```
0054      CALL YAXIS(5.0)
0055      15) CALL XYPLT(DI,R,44,1,-1)
0056          G) T) 40
0057      20) IF(L.LT.LA) CALL ENDPLT
0058          G) T) 1
0059      30) CONTINUE
0060          25) F) 3) AT(F6.2)
0061          RETJPN
0062          END
```

```

0001      SUBROUTINE CASH
          C ***** CASH DOES THE DISCOUNTED CASH FLOW ANALYSIS *****
          C
0002      REAL MAINT
0003      REAL MLIQ
0004      DIMENSION CASINA(50),CASQUA(50),CASINR(50),CASQUR(50),CASINC(50),
          -CASJUC(50),CASINE(50),CASQUE(50),CASINF(50),CASQJF(50)
0005      DIMENSION PEF(100),HEAT(100),DIS(100),COSMA(100),COSMV(100),COSMI(
          -100)
0006      DIMENSION COSA(50),COSB(50),COSC(50),COSE(50),COSF(50),MAINT(50)
0007      DIMENSION D1(50),C1(50),C2(50),C3(50),CF(50)
0008      NA=7
0009      REWIND NA
0010      REWIND 8
0011      COSR=10000000.0
0012      AN=4.0
0013      BN=AN/2.0
0014      A=1.000
0015      AA=2.0
0016      CF(4)=AA
0017      CF(10)=AA
0018      CF(20)=AA
0019      CF(30)=AA
0020      CF(40)=AA
0021      DO 301 I=1,50
0022      COSA(I)=0.0
0023      COSB(I)=0.0
0024      COSC(I)=0.0
0025      COSE(I)=0.0
0026      COSF(I)=0.0
0027      MAINT(I)=0.0
0028      301 CONTINUE
0029      DO 305 I=1,100
0030      REF(I)=0.0
0031      HEAT(I)=0.0
0032      DIS(I)=0.0
0033      COSMA(I)=0.0
0034      COSMV(I)=0.0
0035      COSMI(I)=0.0
0036      305 CONTINUE
0037      READ(1,452)Q,QZ
0038      READ(1,450)PCB,RORB,PCC,RORC,PCP,ROPP
0039      READ(1,451)N,T,APCT,BPCT
0040      READ(1,103)HH,CC
0041      READ(1,100)AMHP,A1N,ADIN,PUMCOS
0042      DO 504 I=1,23
0043      READ(1,102)D1(I),C1(I),C2(I),C3(I)
0044      504 CONTINUE
0045      1000 READ(1,101,END=110)MLIQ,DIA,PLCC
0046      WRITE(8)MLIQ,DIA,PLCC
0047      IF(QZ.LT.10.0)GO TO 2000
0048      WRITE(3,104)
0049      2000 CONTINUE
0050      IF(MLIQ.LT.100.0) GO TO 8
0051      DO 500 I=1,44

```

```

0052 READ(1,105)REF(I),HEAT(I),DIS(I)
0053 WRITE(8)REF(I),HEAT(I),DIS(I)
0054 600 CONTINUE
0055 CALL ZIP(D1,C1,C2,C3,DIA,COST1,COST2,COST3)
0056 77 602 I=1,44
0057 CJSMAX=COST1*DIS(I)
0058 CJSAVG=COST2*DIS(I)
0059 CJSMIN=COST3*DIS(I)
0060 PND=DIS(I)/PLOC
0061 IX=PND
0062 X2=IX
0063 X3=X2+1.0
0064 CJS PJM=X3*PJMCCS*AMHP
0065 CJSMA(I)=AN*(CJS PUM+CJS MAX)+COSR
0066 CJS MV(I)=AN*(CJS PUM+CJS AVG)+COSR
0067 CJS MI(I)=AN*(CJS PUM+CJS MIN)+COSR
0068 MAINT(I)=(CJS PJM*.02)+(X3*27.0*(HH+CC))*AN+0.02*CJS MV(I)
0069 602 CONTINUE
0070 REV=HH*HEAT(4)*A*BN/1000000.0
0071 RREV=CC*REF(4)*CF(4)*A*RN*12000.0/1000000.0
0072 J=4
0073 CALL EXACT(PCB,RORB,PCC,RORC,PCP,RORP,N,COSMV(J),AIN,ADIN,REV,
- RREV,MAINT(J),CASINA,CASQUA)
0074 REV=HH*HEAT(10)*A*BN/1000000.0
0075 RREV=CC*REF(10)*CF(10)*A*RN*12000.0/1000000.0
0076 J=10
0077 CALL EXACT(PCB,RORB,PCC,RORC,PCP,RORP,N,COSMV(J),AIN,ADIN,REV,
- RREV,MAINT(J),CASINB,CASQUB)
0078 REV=HH*HEAT(20)*A*BN/1000000.0
0079 RREV=CC*REF(20)*CF(20)*A*RN*12000.0/1000000.0
0080 J=20
0081 CALL EXACT(PCB,RORB,PCC,RORC,PCP,RORP,N,COSMV(J),AIN,ADIN,REV,
- RREV,MAINT(J),CASINC,CASQUC)
0082 REV=HH*HEAT(30)*A*BN/1000000.0
0083 RREV=CC*REF(30)*CF(30)*A*RN*12000.0/1000000.0
0084 J=30
0085 CALL EXACT(PCB,RORB,PCC,RORC,PCP,RORP,N,COSMV(J),AIN,ADIN,REV,
- RREV,MAINT(J),CASINF,CASQUE)
0086 REV=HH*HEAT(40)*A*BN/1000000.0
0087 RREV=CC*REF(40)*CF(40)*A*RN*12000.0/1000000.0
0088 J=40
0089 CALL EXACT(PCB,RORB,PCC,RORC,PCP,RORP,N,COSMV(J),AIN,ADIN,REV,
- RREV,MAINT(J),CASINF,CASQUE)
0090 IF(QZ.LT.10.0)GO TO 2001
0091 WRITE(3,805)
0092 WRITE(3,800)
0093 WRITE(3,801)MLIQ,DIA,PLOC
0094 WRITE(NA)MLIQ,DIA,PLOC
0095 WRITE(3,802)
0096 WRITE(3,803)
0097 WRITE(3,804)
0098 2001 CONTINUE
0099 YA=CASINA(N)-CASQUA(N)
0100 YB=CASINB(N)-CASQUB(N)
0101 YC=CASINC(N)-CASQUC(N)
0102 YE=CASINE(N)-CASQUE(N)

```



```

0103       YF=CASINF(N)-CASQUF(N)
0104       IYEAR =0
0105       DO 506 I=1,N
0106       IYEAR=IYEAR+1
0107       IF(OZ.LT.10.0)GO TO 2002
0108       WRITE(3,911)IYEAR,CASQUA(I),CASINA(I),CASQUB(I),CASINB(I),CASQUC(I)
          -),CASINC(I),CASQUE(I),CASINE(I),CASQUF(I),CASINF(I)
0109 2002 CONTINUE
0110       WRITE(N4) IYEAR,CASQUA(I),CASINA(I),CASQUB(I),CASINB(I),CASQUC(I)
          -),CASINC(I),CASQUE(I),CASINE(I),CASQUF(I),CASINF(I)
0111 506 CONTINUE
0112       WRITE(3,805)
0113       ALIN=ADIN*100.0
0114       WRITE(3,10)ALIN,N
0115       WRITE(3,1)YA,YR,YC,YF,YF
0116       DO TO 1000
0117 110 MLIQ=0.0
0118       DIA=0.0
0119       PLOC=0.0
0120       WRITE(N4)MLIQ,DIA,PLOC
0121       CALL CFLOT(N)
0122       1 FORMAT(17X,1PE12.5,4(12X,1PE12.5))
0123       2 FORMAT(////)
0124       10 FORMAT(14X,'PRESENT VALUE OF INCOME AT ',F4.1,' PER CENT AND A LIFE
          -E OF ',I3,' YEARS',/)
0125       100 FORMAT(F7.1,2F6.4,F5.1)
0126       101 FORMAT(F13.6,FF.2,F5.2)
0127       102 FORMAT(F9.2,3F10.2)
0128       103 FORMAT(2F7.1)
0129       104 FORMAT(1H1)
0130       105 FORMAT(F6.2,1X,E13.6,F6.1)
0131       450 FORMAT(6F6.4)
0132       451 FORMAT(14,3F6.4)
0133       452 FORMAT(2F6.2)
0134       800 FORMAT(1X,'MASS RATE OF FLOW',20X,'PIPE DIAMETER',15X,'DISTANCE B
          -ETWEEN PUMPS',/,6X,'(LBM/HR)',26X,'(INCHES)',26X,'(MILES)',/)
0135       801 FORMAT(1X,F13.6,28X,F5.2,28X,F5.2,////)
0136       802 FORMAT(10(8X,'CASH'))
0137       803 FORMAT(8X,'OUT',10X,'IN',4(9X,'CUT',IN'))
0138       804 FORMAT(2X,'YEAR (10 MI) (10 MI)',5X,'(25 MI) (25 MI)',5X,
          -'(50 MI) (50 MI)',5X,'(75 MI) (75MI)',5X,
          -'(100 MI) (100 MI)')
0139       805 FORMAT(////)
0140       911 FORMAT(15,10(1PE12.5))
0141       9 RETURN
0142       END

```

```

0001      SUBROUTINE EXACT(PCB,RORB,PCC,RORC,PCP,PORP,N,CI,AIN,ADIN,REV,
          -RREV,MAINT,CASIN,CASOUT)
C
C***** EXACT DOES THE DEPRECIATION SCHEME, TAX CALCULATIONS AND DISCOUNTING
C CALCULATIONS INCLUDING INFLATION FACTORS *****
C
0002      DIMENSION CASOUT(50),CASIN(50),YEAR(50)
0003      REAL MAINT
0004      CRF=ADIN*((1.0+ADIN)**N)/((1.0+ADIN)**N)-1.0
0005      ADEP=CRF*CI
0006      TR=0.5
0007      ASJM=0.0
0008      BSJM=0.0
0009      PTP=.02
0010      YRST=N
0011      BDEP=CI/YRST
0012      PCT=(BDEP/CI)*2.0
0013      RRB=PCB*RORB*CI
0014      RJC=PCC*RORC*CI
0015      RJP=PCP*ROFP*CI
0016      TRD=RRB+RJC+RJP
0017      TAXOUT=CI*PTP
0018      CA=CI
0019      DO 10 I=1,N
0020      YEAR(I)=PCT*CA
0021      IF(REV.GT.10000.)GO TO 40
0022      WRITE(3,101)YEAR(I)
0023      +0 CONTINUE
0024      CA=CA-YEAR(I)
0025      M=I
0026      IF((CA/(N-I)-YEAR(I)))/12,200,200
0027      12 CONTINUE
0028      10 CONTINUE
0029      200 CONTINUE
0030      X=M
0031      RBD=CA/X
0032      L=M+1
0033      DO 20 I=M,N
0034      YEAR(I)=RBD
0035      IF(REV.GT.10000.)GO TO 50
0036      WRITE(3,101)YEAR(I)
0037      50 CONTINUE
0038      20 CONTINUE
0039      DO 30 I=1,N
0040      ES=(1.0+AIN)**I
0041      PWF=1.0/((1.0+ADIN)**I)
0042      CALL PWRTH(REV,RFEV,I,AIN,ADIN,MAINT,CASIN,BMAINT)
0043      FTAX=TR*((REV+RFEV)*ES)-(MAINT*ES+YEAR(I)+RCB+TAXOUT)
0044      FEDTAX=FTAX*PWF
0045      PRTX=TAXOUT*PWF
0046      DTR=TRD*PWF
0047      CASIN(I)=FEDTAX+PRTX+BMAINT+DTR+ADEP
0048      IF(REV.GT.10000.)GO TO 60
0049      WRITE(3,100)CASIN(I),FEDTAX,PRTX,BMAINT,DTR,ADEP
0050      60 CONTINUE
0051      ASJM=ASJM+CASIN(I)

```

```

0001      SJBROUTINE ZIP(D,C1,C2,C3,DIA,COSTA,COSTB,COSTC)
C
C***** ZIP DOES A TABLE LOOK UP FOR PIPE COSTS *****
C
0002      DIMENSION C1(50),C2(50),C3(50),D(50)
0003      DO 20 I=1,22
0004      IF((DIA.GE.D(I)).AND.(DIA.LT. D(I+1)))G3 TO 30
0005      20 CONTINUE
0006      30 A=C1(I)
0007      B=C2(I)
0008      C=C3(I)
0009      DD=C1(I+1)
0010      E=C2(I+1)
0011      F=C3(I+1)
0012      G=D(I)
0013      H=D(I+1)
0014      CJSTA=(A+(((DD-A)/(H-G))*(DIA-G)))*1000.0
0015      CJSTB=(B+(((E-B)/(H-G))*(DIA-G)))*1000.0
0016      CJSTC=(C+(((F-C)/(H-G))*(DIA-G)))*1000.0
0017      RETJRN
0018      END

```

```

0052      BSUM=BSUM+CASI
0053      CASOUT(I)=ASUM
0054      CASIN(I)=BSUM
0055      30 CONTINUE
0056      100 FJRMAT(5X,6F10.2)
0057      101 FJRMAT(5X,F10.2)
0058      RETURN
0059      END

```

```

0001      SJBROUTINE AWRTH(K,AAIN,RR,ARR)
C
C***** AWRTH IS A ROUTINE THAT DOES THE PRESENT WORTH CALCULATIONS *****
C
0002      YEARS=K
0003      PWF=1.0/((1.0+AAIN)**YEARS)
0004      ARR=RR*PWF
0005      RETURN
0006      END

```

```

0001      SUBROUTINE CPL0T(N)
C
C***** CPL0T PLOTS THE DATA FROM CASH *****
C
0002      DIMENSION A(20),R(20),C(20)
0003      DIMENSION IYEAR(50),COSA(50),ATOTAL(50),COSB(50),BTOTAL(50),
- C)JSC(50),CTOTAL(50),COSE(50),ETOTAL(50),COSF(50),FTOTAL(50)
0004      DIMENSION YEAR(50),AD(50)
0005      REAL MLIQ
0006      CALL PENPJS('BLASE',5,0)
0007      IA=7
0008      Z)=39.0
0009      DG=63.0
0010      21 REWIND NA
0011      L=0
0012      K=0
0013      M=10
0014      DJ=DG-3.0
0015      AJ=DG+0.5
0016      BJ=DG-0.5
0017      +3 READ(NA)MLIQ,DIA,PLOC
0018      IF(MLIQ.LT.1.0) GO TO 50
0019      DO 10 I=1,N
0020      READ(NA)IYEAR(I),CCSA(I),ATOTAL(I),COSB(I),BTOTAL(I),COSC(I),
- CTOTAL(I),COSE(I),ETOTAL(I),COSF(I),FTOTAL(I)
0021      CCSA(I)=COSA(I)*1.0E-06
0022      COSB(I)=COSB(I)*1.0E-06
0023      C)JSC(I)=C)JSC(I)*1.0E-06
0024      COSE(I)=COSE(I)*1.0E-06
0025      COSF(I)=COSF(I)*1.0E-06
0026      ATOTAL(I)=ATOTAL(I)*1.0E-06
0027      BTOTAL(I)=BTOTAL(I)*1.0E-06
0028      CTOTAL(I)=CTOTAL(I)*1.0E-06
0029      ETOTAL(I)=ETOTAL(I)*1.0E-06
0030      FTOTAL(I)=FTOTAL(I)*1.0E-06
0031      YEAR(I)=IYEAR(I)
0032      10 CONTINUE
0033      IF((DIA.GT.AJ).OR.(DIA.LT.BJ))GO TO 40
0034      WRITE(3,27)DIA
0035      IF(M.GT.1)GO TO 30
0036      CALL NEWPLT(0.5,2.0,6.0)
0037      CALL ORIGIN(0.0,0.0)
0038      CALL YSCALE(0.0,710.0,4.5)
0039      X=N
0040      CALL XSCALE(0.0,X,4.5)
0041      CALL XAXIS(5.0)
0042      CALL YAXIS(25.0)
0043      CALL XYPLT(YEAR,CCSA,N,1,1)
0044      CALL XYPLT(YEAR,COSB,N,1,2)
0045      CALL XYPLT(YEAR,C)JSC,N,1,3)
0046      CALL XYPLT(YEAR,COSE,N,1,4)
0047      CALL XYPLT(YEAR,COSF,N,1,5)
0048      CALL XYPLT(YEAR,ATOTAL,N,1,6)
0049      CALL XYPLT(YEAR,BTOTAL,N,1,7)
0050      CALL XYPLT(YEAR,CTOTAL,N,1,8)
0051      CALL XYPLT(YEAR,ETOTAL,N,1,11)

```

```
0052     CALL XYPLT(YEAR,FTOTAL,N,1,12)
0053     CALL ENDPLT
0054 30  CALL FINAL(COSA(N),ATOTAL(N),COSB(N),BTOTAL(N),COSC(N)
-      ,CTOTAL(N),COSE(N),FTOTAL(N),COSE(N),FTOTAL(N),A,B,C)
0055     ) ) 32 I=1,5
0056     A(I)=C(I)-B(I)
0057 32  CONTINUE
0058     KSET=1
0059     K=K+1
0060     IF (L.LT.1)GO TO 20
0061     IF (K.LT.10)GO TO 70
0062     IF (K.GE.10)CALL ENDPLT
0063     KSET=2
0064     K=0
0065 20  CONTINUE
0066     L=L+1
0067     CALL NEWPLT(0.5,5.5,6.0)
0068     CALL ORIGIN(0.0,0.0)
0069     CALL XSCALE(0.0,101.0,4.5)
0070     CALL YSCALE(-160.0,160.0,6.0)
0071     CALL XAXIS(10.0)
0072     CALL YAXIS(20.0)
0073     J=5
0074     NN=K
0075     NK=K
0076 70  CONTINUE
0077     CALL XYPLT(A,AD,J,1,NN)
0078     ) ) TO 40
0079 50  CONTINUE
0080     IF (KSET.EQ.2)GO TO 80
0081     CALL ENDPLT
0082 80  CONTINUE
0083     IF (DG-Z)28,21,21
0084 23  CONTINUE
0085     CALL LSTPLT
0086 27  FORMAT(F5.2)
0087     RETURN
0088     END
```

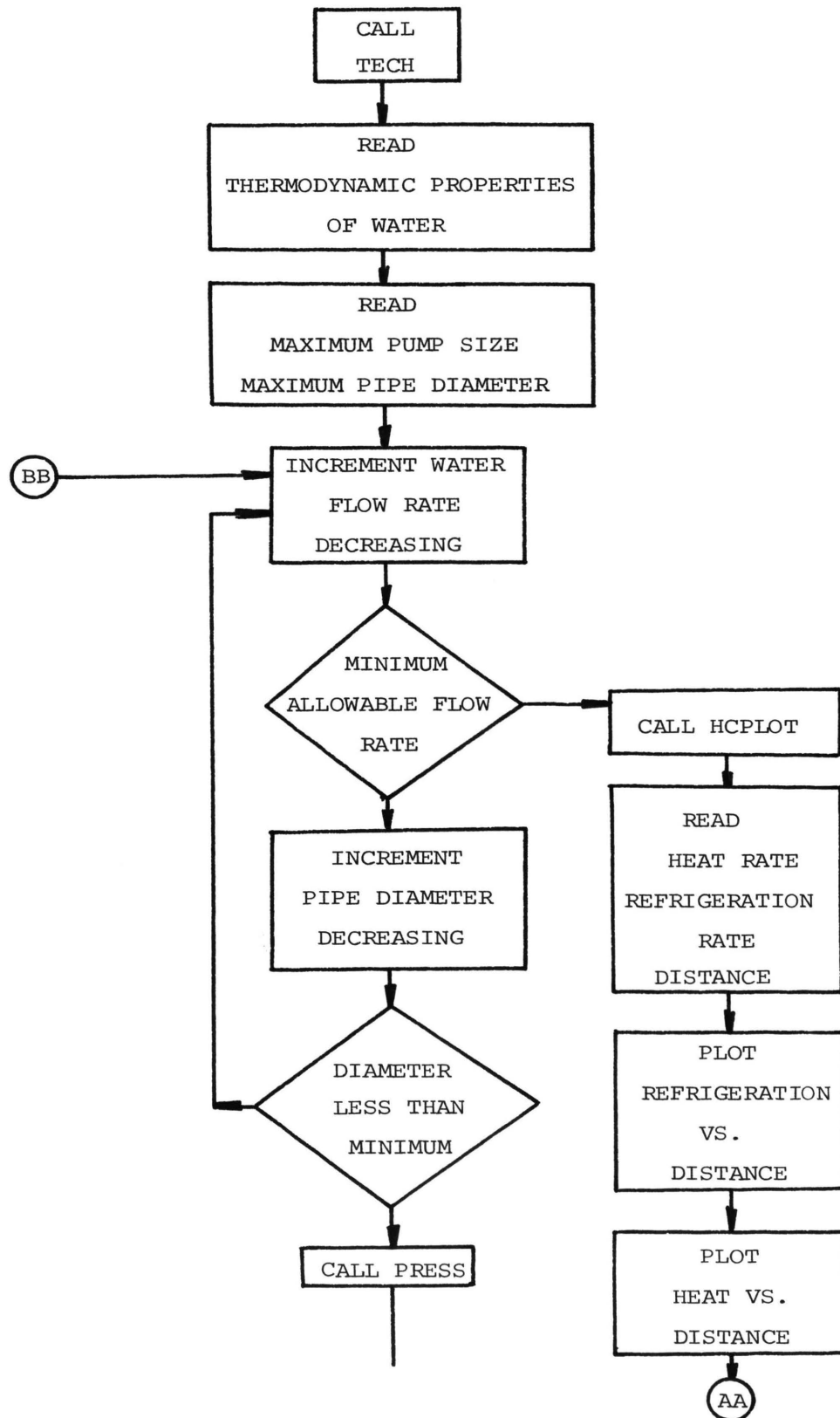
```

0001      SUBROUTINE FINAL(COSA,ATOTAL,COSE,BTOTAL,COSE,CTOTAL,COSE,FTOTAL
- ,COSF,FTOTAL,DIS,COST,TOTAL)
C ***** FINAL ARRANGES SCALARS INTO VECTOR FORMS FOR THE PLOTTER *****
C
0002      DIMENSION DIS(20),COST(20),TOTAL(20)
0003      J=0
0004      J=J+1
0005      DIS(J)=10.0
0006      COST(J)=COSA
0007      TOTAL(J)=ATOTAL
0008      J=J+1
0009      DIS(J)=25.0
0010      COST(J)=COSB
0011      TOTAL(J)=BTOTAL
0012      J=J+1
0013      DIS(J)=50.0
0014      COST(J)=COSC
0015      TOTAL(J)=CTOTAL
0016      J=J+1
0017      DIS(J)=75.0
0018      COST(J)=COSE
0019      TOTAL(J)=ETOTAL
0020      J=J+1
0021      DIS(J)=100.0
0022      COST(J)=COSF
0023      TOTAL(J)=FTOTAL
0024      RETURN
0025      END
    
```

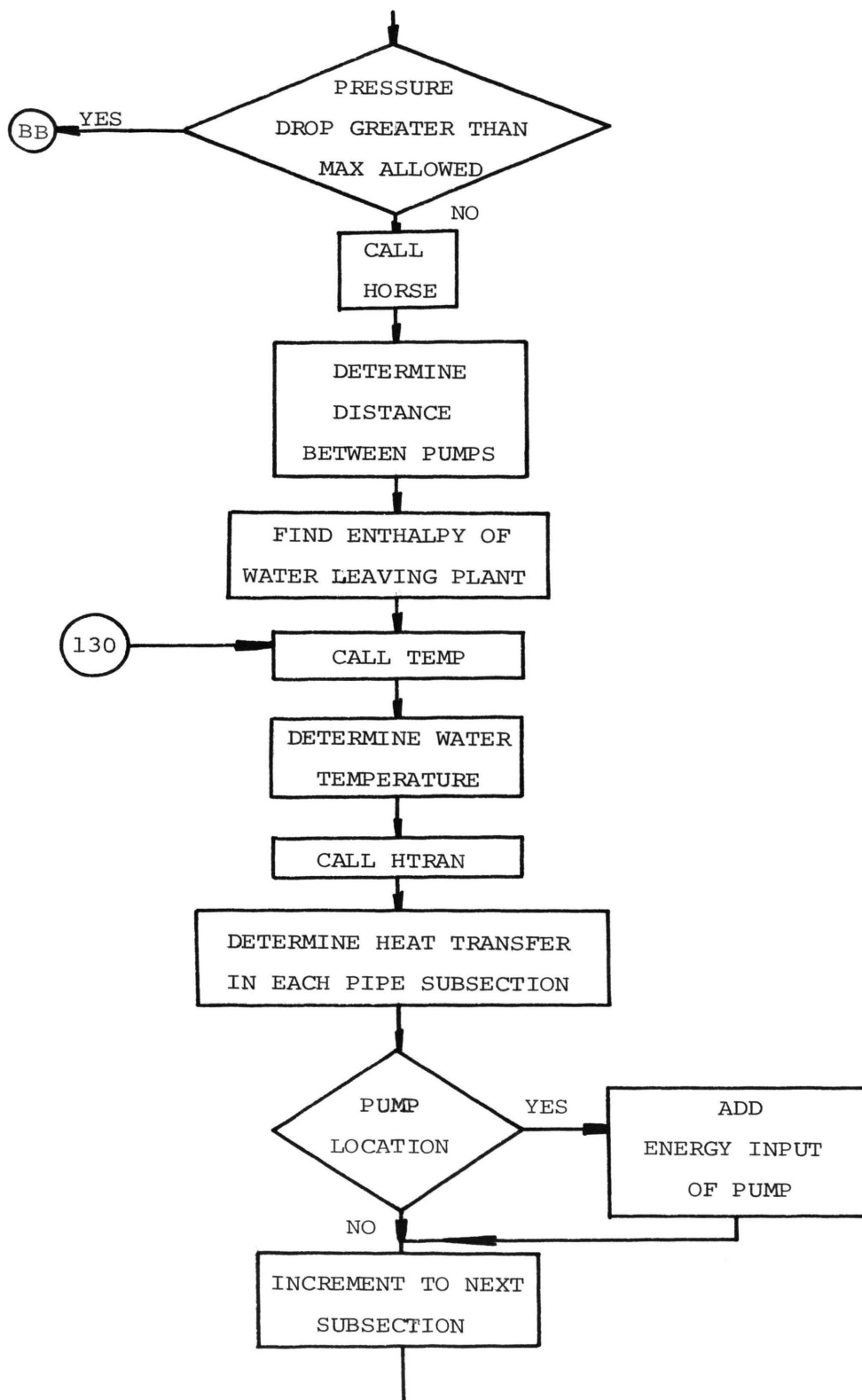
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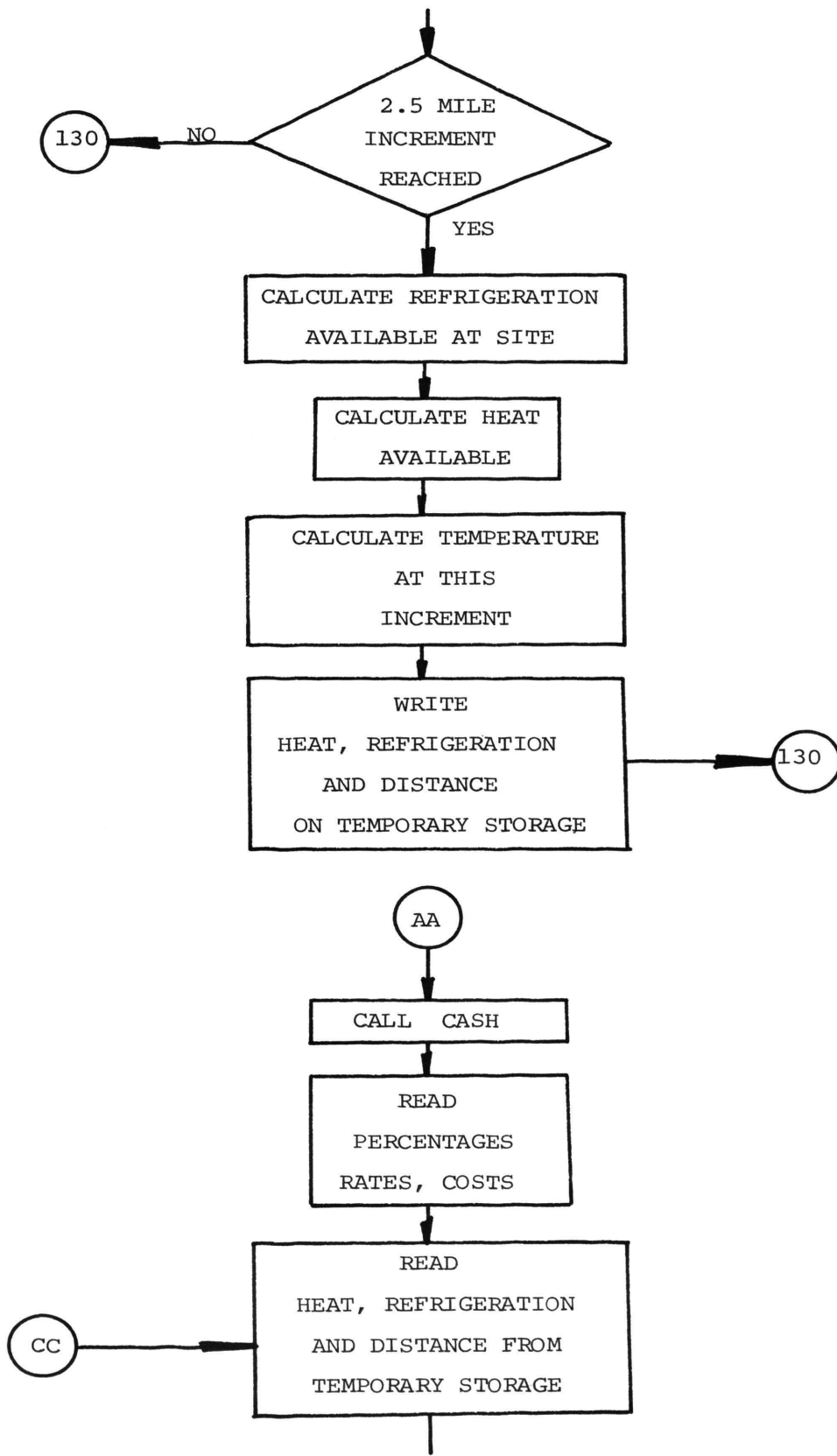
0001      SUBROUTINE PWRTH(REV,RREV, K ,AIN,ADIN,MAINT,DZ,DM)
C ***** PWRTH DOES PRESENT WORTH AND COMPOUND AMOUNT CALCULATIONS *****
C
0002      REAL MAINT
0003      PWF=1.0/((1+ADIN)**K)
0004      CAF=(1.0+AIN)**K
0005      DDVH=REV*CAF*PWF
0006      DDVR=RREV*CAF*PWF
0007      D4=MAINT*CAF*PWF
0008      DZ=DDVH+DDVR
0009      RETURN
0010      END
    
```

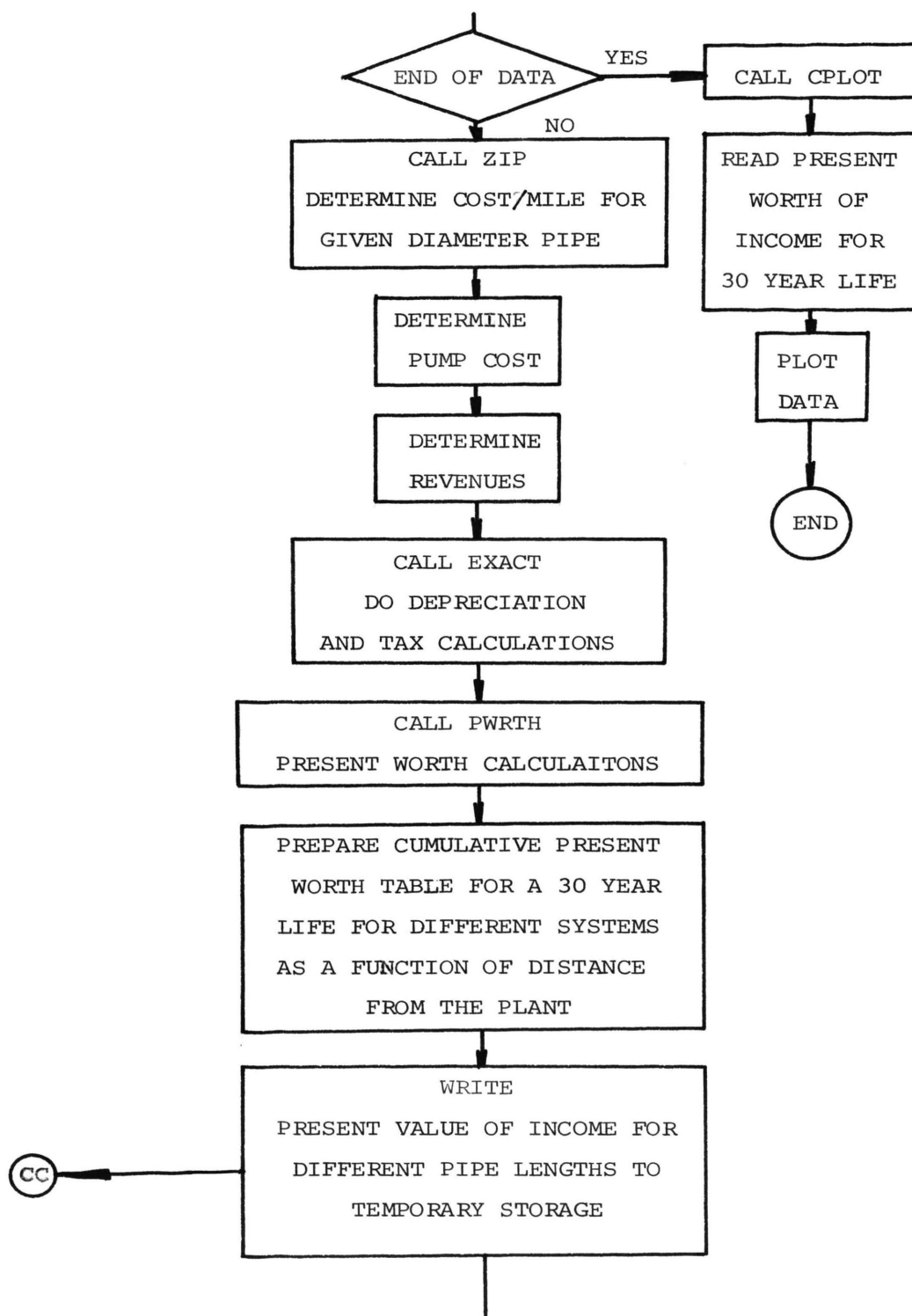
APPENDIX C  
COMPUTER PROGRAM FLOW CHART











APPENDIX D  
SAMPLE CASH FLOW PROBLEM

The following is a sample problem demonstrating the technique used in the discounted cash flow analysis in the economics section of this investigation.

Given:

Capital investment	= \$1000.00
Revenue	= \$2000.00/year
Maintenance & Operating costs	= \$1000.00/year
Inflation factor	= 4.5%
Discount factor	= 10%
Tax rate	= 50%
Property tax rate	= 2%

Find:

The present value net cumulative profit at 10% for a 10 year life.

Straight line depreciation rate:

$$\begin{aligned} \text{DR} &= \frac{1}{10 \text{ years}} \\ &= 10\% \end{aligned}$$

Dual declining balance rate:

$$\begin{aligned} \text{DDR} &= 2.0 \times \text{DR} \\ &= 20\% \end{aligned}$$

The following table is a dual declining balance depreciation scheme which will be used for the tax calculations.

$$\text{DDB} = \text{DDR} \times \text{Undepreciated balance}$$

where

DDB = Depreciation expense

$$\text{DDB}(1) = (.2)(1000.0) = 200.00$$

$$\text{DDB}(2) = (.2)(1000.0 - 200.0) = 160.00$$

$$\text{DDB}(3) = (.2)(800.00 - 160.0) = 128.00$$

$$\text{DDB}(4) = (.2)(640.00 - 128.0) = 102.40$$

$$\text{DDB}(5) = (.2)(512.00 - 102.4) = 81.92$$

SWITCH TO STRAIGHT LINE SCHEME

$$\text{DDB}(6) = \frac{409.60 - 81.92}{5 \text{ years}} = 65.54$$

$$\text{DDB}(7) = 65.54$$

$$\text{DDB}(8) = 65.54$$

$$\text{DDB}(9) = 65.54$$

$$\text{DDB}(10) = 65.54$$

FINANCING EXPENSES/\$1000.00 Capital Investment

The project will be financed by:

30% Bonds @ 7% interest

30% Common @ 14% interest

40% Preferred @ 7% interest

Return on Bonds

$$\text{ROB} = \text{Per cent bonds} \times \text{interest rate} \times \text{capital investment}$$

$$= .30 \times .07 \times 1000.00$$

$$= 21.00/\text{year}$$

## Return on Common

$$\begin{aligned} \text{ROC} &= \text{Per cent common} \times \text{interest rate} \times \text{capital investment} \\ &= .30 \times .14 \times 1000.00 \\ &= 42.00/\text{year} \end{aligned}$$

## Return on Preferred

$$\begin{aligned} \text{ROP} &= \text{Per cent preferred} \times \text{interest rate} \times \text{capital investment} \\ &= .40 \times .07 \times 1000.00 \\ &= 28.00/\text{year} \end{aligned}$$

## Total return/\$1000.00 Capital Investment

$$\begin{aligned} \text{TRO} &= \text{ROB} + \text{ROC} + \text{ROP} \\ &= 91.00 \end{aligned}$$

## Property tax/\$1000.00 Capital Investment

$$\begin{aligned} \text{PRTX} &= \text{Tax rate} \times \text{capital investment} \\ &= .02 \times 1000.00 \\ &= 20.00/\text{year} \end{aligned}$$

Table D1.0. Schedule for Tax Calculations.

YEAR	SPCA (1 + i) <sup>n</sup>	MAINT + OP (escalated)	REVENUE (escalated)	DDB	BOND Interest
1	1.045	1045.00	2090.00	200.00	21.00
2	1.092	1092.00	2184.00	160.00	21.00
3	1.141	1141.00	2282.00	128.00	21.00
4	1.192	1192.00	2384.04	102.40	21.00
5	1.246	1246.00	2492.36	81.92	21.00
6	1.302	1302.00	2604.52	65.54	21.00
7	1.360	1360.00	2721.72	65.54	21.00
8	1.422	1422.00	2844.30	65.54	21.00
9	1.486	1486.00	2972.18	65.54	21.00
10	1.552	1552.97	3105.94	65.54	21.00

Where

SPCA = single payment compound amount factor

escalated = adjusted by SPCA for a 4.5% inflation

Income tax

$$\text{TAX}(N) = \text{Tax rate} (\text{revenue} - \text{bond interest} - \text{property tax} \\ - \text{maintenance and operating} - \text{depreciation})$$

Example

$$\begin{aligned} \text{Tax}(1) &= .50(2090.00 - 21.00 - 1045.00 - 200.00) \\ &= 402.00 \end{aligned}$$

Table D2.0. Yearly Tax.

YEAR	TAX
1	402.00
2	445.37
3	485.67
4	524.54
5	561.54
6	597.85
7	627.15
8	657.78
9	689.77
10	723.21

Capital recovery

$$\begin{aligned}
 \text{CR} &= \text{Capital investment} \left( \frac{i(1+i)^n}{(1+i)^{n-1}} \right) \\
 &= 1000.00 \times .16275 \\
 &= 162.75
 \end{aligned}$$



Table D3.0. Face Value Cash.

YEAR	REVENUE	TAX	TOTAL INTEREST + DIVIDENDS	PROP. TAX	MAINT OP	SPCA
1	2090.00	402.00	91.00	20.00	1045.00	1.045
2	2184.00	445.37	91.00	20.00	1092.00	1.092
3	2282.20	485.67	91.00	20.00	1141.66	1.141
4	2385.04	524.54	91.00	20.00	1192.52	1.192
5	2492.36	561.63	91.00	20.00	1246.18	1.246
6	2604.52	597.85	91.00	20.00	1302.26	1.302
7	2721.72	627.15	91.00	20.00	1360.86	1.360
8	2844.20	657.78	91.00	20.00	1422.10	1.422
9	2972.18	689.77	91.00	20.00	1486.09	1.486
10	3105.94	723.24	91.00	20.00	1552.97	1.552

Table D4.0. Present Worth at Time 0. Discounted at 10%.

YEAR	REVENUE	TAX	INTEREST + DIVIDENDS	PROP. TAX	MAINT OP
1	1900.00	365.45	82.73	18.18	950.01
2	1804.06	368.05	75.21	16.53	902.64
3	1714.47	364.89	68.37	15.03	851.73
4	1628.98	358.25	62.15	13.66	814.49
5	1547.51	348.71	56.50	12.42	773.75
6	1470.25	337.48	51.37	11.29	735.13
7	1396.79	321.85	46.70	10.26	698.39
8	1326.82	306.85	42.45	9.33	663.11
9	1260.50	292.53	38.59	8.48	630.25
10	1197.33	278.80	35.08	7.71	601.26

Cash in = Revenue

Cash out = Income tax + interest + dividends + property tax  
 + maintenance + operating + capital recovery

Table D5.0. Cumulative Cash Flow.

YEAR	CASH IN	CASH OUT
1	1900.02	1564.32
2	3704.88	3061.24
3	5419.35	4483.53
4	7048.33	5837.23
5	8595.84	7129.65
6	10066.09	8356.80
7	11462.88	9517.52
8	12789.70	10615.17
9	14050.20	11654.04
10	15247.53	12639.71

$$\begin{aligned} NP &= 15247.53 - 12639.71 \\ &= 2607.82 \end{aligned}$$

Where

NP = Present value net cumulative profit  
 at 10% for a life of 10 years.