

01 May 2018

Search for Tensor, Vector, and Scalar Polarizations in the Stochastic Gravitational-Wave Background

Benjamin P. Abbott

Marco Cavaglia

Missouri University of Science and Technology, cavagliam@mst.edu

For full list of authors, see publisher's website.

Follow this and additional works at: https://scholarsmine.mst.edu/phys_facwork



Part of the [Physics Commons](#)

Recommended Citation


B. P. Abbott et al., "Search for Tensor, Vector, and Scalar Polarizations in the Stochastic Gravitational-Wave Background," *Physical Review Letters*, vol. 120, no. 20, American Physical Society (APS), May 2018. The definitive version is available at <https://doi.org/10.1103/PhysRevLett.120.201102>

This Article - Journal is brought to you for free and open access by Scholars' Mine. It has been accepted for inclusion in Physics Faculty Research & Creative Works by an authorized administrator of Scholars' Mine. This work is protected by U. S. Copyright Law. Unauthorized use including reproduction for redistribution requires the permission of the copyright holder. For more information, please contact scholarsmine@mst.edu.

Search for Tensor, Vector, and Scalar Polarizations in the Stochastic Gravitational-Wave Background

B. P. Abbott *et al.**

(LIGO Scientific Collaboration and Virgo Collaboration)

 (Received 1 March 2018; revised manuscript received 30 March 2018; published 16 May 2018)

The detection of gravitational waves with Advanced LIGO and Advanced Virgo has enabled novel tests of general relativity, including direct study of the polarization of gravitational waves. While general relativity allows for only two tensor gravitational-wave polarizations, general metric theories can additionally predict two vector and two scalar polarizations. The polarization of gravitational waves is encoded in the spectral shape of the stochastic gravitational-wave background, formed by the superposition of cosmological and individually unresolved astrophysical sources. Using data recorded by Advanced LIGO during its first observing run, we search for a stochastic background of generically polarized gravitational waves. We find no evidence for a background of any polarization, and place the first direct bounds on the contributions of vector and scalar polarizations to the stochastic background. Under log-uniform priors for the energy in each polarization, we limit the energy densities of tensor, vector, and scalar modes at 95% credibility to $\Omega_0^T < 5.58 \times 10^{-8}$, $\Omega_0^V < 6.35 \times 10^{-8}$, and $\Omega_0^S < 1.08 \times 10^{-7}$ at a reference frequency $f_0 = 25$ Hz.

DOI: [10.1103/PhysRevLett.120.201102](https://doi.org/10.1103/PhysRevLett.120.201102)

Introduction.—The direct detection of gravitational waves offers novel opportunities to test general relativity in previously unexplored regimes. Already, the compact binary mergers [1–5] observed by Advanced LIGO (the Laser Interferometer Gravitational Wave Observatory) [6,7] and Advanced Virgo [8] have enabled improved limits on the graviton mass, experimental measurements of post-Newtonian parameters, and inference of the speed of gravitational waves, among other tests [3,9–11].

Another central prediction of general relativity is the existence of only two gravitational-wave polarizations: the tensor plus and cross modes, with spatial strain tensors

$$\hat{e}_+ = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \hat{e}_\times = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad (1)$$

(assuming waves propagating in the $+\hat{z}$ direction). Generic metric theories of gravity, however, can allow for up to four additional polarizations: the x and y vector modes and the breathing and longitudinal scalar modes, with basis strain tensors [12–14]

$$\hat{e}_x = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} \quad \hat{e}_y = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \\ \hat{e}_b = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \hat{e}_l = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}. \quad (2)$$

The observation of vector or scalar modes would be in direct conflict with general relativity, and so the direct measurement of gravitational-wave polarizations offers a promising avenue by which to test theories of gravity [14].

Recently, the Advanced LIGO-Virgo network has succeeded in making the first direct statement about the polarization of gravitational waves. The gravitational-wave signal GW170814, observed by both the Advanced LIGO and Virgo detectors, significantly favored a model assuming pure tensor polarization over models with pure vector or scalar polarizations [4,15]. In general, however, the ability of the Advanced LIGO-Virgo network to study the polarization of gravitational-wave transients is limited by several factors. First, the LIGO-Hanford and LIGO-Livingston detectors are nearly co-oriented, preventing Advanced LIGO from sensitively measuring more than a single polarization mode [4,9,10,15]. Second, at least five detectors are needed to fully characterize the five polarization degrees of freedom accessible to quadrupole detectors. Quadrupole detectors (those measuring differential arm motion) have degenerate responses to breathing and

*Full author list given at the end of the article.

longitudinal modes, and can therefore measure only a single linear combination of scalar breathing and longitudinal polarizations [14–17].

Beyond compact binary mergers, another target for Advanced LIGO and Virgo is the stochastic gravitational-wave background. An astrophysical stochastic background is expected to arise from the population of distant compact binary mergers [18–23], core-collapse supernovae [24–26], and rapidly rotating neutron stars [27–29]. In particular, the astrophysical background from compact binary mergers is likely to be detected by LIGO and Virgo at their design sensitivities [23]. A background of cosmological origin may also be present, due to cosmic strings [30,31], inflation [32–35], and phase transitions in the early Universe [32,33,36–38].

Long duration gravitational-wave sources, like the stochastic background [39–42] or persistent signals from rotating neutron stars [43–45], offer a viable means of searching for nonstandard gravitational-wave polarizations. Unlike gravitational-wave transients, which sample only a single point on the LIGO/Virgo antenna response patterns, long-duration signals contain information about many points on the antenna patterns. Long-duration signals, therefore, enable the direct measurement of gravitational-wave polarizations using the current generation of gravitational-wave detectors, without the need for additional detectors or an independent electromagnetic counterpart. The stochastic background is thus a valuable laboratory for polarization-based tests of general relativity [42].

In this Letter, we present the first direct search for vector and scalar polarizations in the stochastic gravitational-wave background. We analyze data recorded during Advanced LIGO’s first observing run (O1), which has previously been searched for both isotropic and anisotropic backgrounds of standard tensor polarizations [46,47]. First, we describe the O1 data set and its initial processing. We then discuss the stochastic analysis, including the construction of Bayesian odds that indicate the nondetection of a generically polarized stochastic background in our data. Finally, we present upper limits on the joint contributions of tensor, vector, and scalar polarizations to the stochastic gravitational-wave background. Additional details and results are presented in the Supplemental Material [48], available online.

Data.—We search Advanced LIGO data for evidence of a stochastic background, analyzing data recorded between September 18, 2015 15:00 UTC and January 12, 2016 16:00 UTC during LIGO’s O1 observing run. We do not include several days of O1 data recorded prior to September 18, but this has negligible impact on our results. We exclude times containing the binary black hole signals GW150914 and GW151226, as well as the signal candidate LVT151012.

The initial data processing proceeds as in previous analyses [46,49]. Time-domain strain measurements from the LIGO-Hanford and LIGO-Livingston detectors are

down-sampled from 16 384 Hz to 4096 Hz and divided into half-overlapping 192 s segments. Each time segment is then Hann-windowed, Fourier transformed, and high-pass filtered using a 16th order Butterworth filter with a knee frequency of 11 Hz. Finally, the strain data are coarse-grained to a frequency resolution of 0.03 125 Hz and restricted to a frequency band from 20–1726 Hz. Within each segment, we compute the LIGO-Hanford and LIGO-Livingston strain auto-power spectral densities using Welch’s method [50].

Standard data quality cuts are performed in both the time and frequency domains to mitigate the effects of non-Gaussian instrumental and environmental noise [46,47,51]. In the time domain, 35% of data is discarded due to nonstationary detector noise, leaving 29.85 days of coincident observing time. In the frequency domain, an additional 21% of data is discarded to remove correlated narrow-band features between LIGO-Hanford and LIGO-Livingston [46,47,51]. These narrow-band correlations are due to a variety of sources, including injected calibration signals, power mains, and GPS timing systems. To estimate possible contamination due to terrestrial Schumann resonances [52–54], we additionally monitored coherences between magnetometers installed at both detectors. Schumann resonances were found to contribute negligibly to the stochastic measurement [46,51].

We assume conservative 4.8% and 5.4% calibration uncertainties on the strain amplitude measured by LIGO-Hanford and LIGO-Livingston, respectively [55]. Phase calibration is a much smaller source of uncertainty and is therefore neglected [46,56]. All results below are obtained after marginalization over amplitude uncertainties; see the Supplemental Material [48] for details.

Method.—To search for a generically polarized stochastic background, we will apply the methodology presented in Ref. [42]. This method is summarized below, and additional details are discussed in the Supplemental Material [48].

The stochastic background may be detected in the form of a correlated signal between pairs of gravitational-wave detectors. We will assume that the stochastic background is stationary, isotropic, and Gaussian. For simplicity, we also assume that the background is uncorrelated between polarization modes. Finally, we assume that the tensor and vector contributions to the background are individually unpolarized (with equal contributions, for instance, from the tensor plus and cross modes). Certain theories may violate one or more of these assumptions. For example, the stochastic background is unlikely to remain strictly unpolarized in the presence of gravitational-wave birefringence, as in Chern-Simons gravity [57–59], while theories violating Lorentz invariance may yield a departure from isotropy [60,61]. The violation of one or more of our assumptions would likely reduce our search’s sensitivity to the stochastic background.

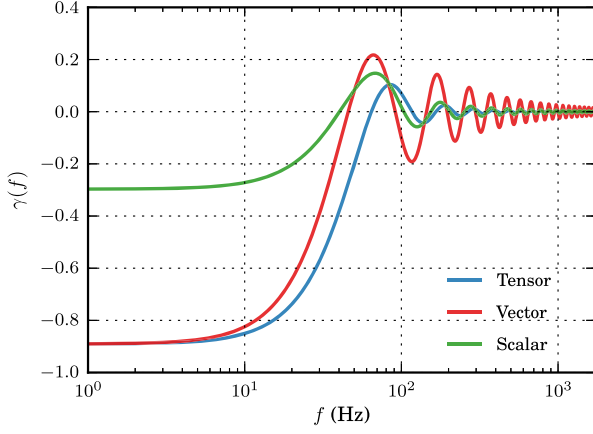


FIG. 1. Overlap reduction functions representing the Advanced LIGO network's sensitivity to stochastic backgrounds of tensor (blue), vector (red), and scalar-polarized (green) gravitational waves.

Given the above assumptions, the expected cross-correlation between two detectors in the presence of a stochastic background is of the form [39–41,62]

$$\langle \tilde{s}_1(f) \tilde{s}_2^*(f') \rangle = \frac{1}{2} \delta(f - f') \sum_A \Gamma_A(f) S_h^A(f). \quad (3)$$

Here, $S_h^A(f)$ is the one-sided gravitational-wave strain power spectral density of the net tensor ($A = T$), vector (V), and scalar (S) contributions to the stochastic background. The detectors' geometry is encoded in the overlap reduction functions $\Gamma_A(f)$, defined [39,42,62,63]

$$\Gamma_A(f) = \frac{1}{8\pi} \sum_{a \in A} \int d\hat{n} F_1^a(\hat{n}) F_2^a(\hat{n}) e^{2\pi i f \hat{n} \cdot \Delta x / c}. \quad (4)$$

$F_I^a(\hat{n})$ is the antenna response function of detector I to signals of polarization a , Δx is the separation vector between detectors, and c is the speed of light. The integral is taken over all sky directions \hat{n} .

We will work not directly with $\Gamma_A(f)$, but rather with the *normalized* overlap reduction functions $\gamma_A(f) \propto \Gamma_A(f)/\Gamma_0$, where the constant Γ_0 is chosen such that $\gamma_T(f) = 1$ for co-located and co-oriented detectors. For Advanced LIGO, $\Gamma_0 = 1/5$, but in general its value will vary for other experiments like LISA and pulsar timing arrays [64]. The normalized overlap reduction functions for LIGO's Hanford-Livingston baseline are shown in Fig. 1. Because tensor, vector, and scalar modes each have distinct overlap reduction functions, the shape of a measured cross-correlation spectrum [Eq. (3)] will reflect the polarization content of the stochastic background [39,42]. Of the three curves in Fig. 1, the scalar overlap reduction function is smallest in magnitude. This reflects the fact that the Advanced LIGO detectors have weaker geometrical

responses to scalar-polarized gravitational waves than to tensor- and vector-polarized signals.

Conventionally, gravitational-wave backgrounds are parameterized by their energy-density spectra [62,64]

$$\Omega(f) = \frac{1}{\rho_c} \frac{d\rho_{\text{GW}}}{d \ln f}, \quad (5)$$

where $d\rho_{\text{GW}}$ is the energy density in gravitational waves per logarithmic frequency interval $d \ln f$. We normalize Eq. (5) by $\rho_c = 3H_0^2 c^2 / 8\pi G$, the closure energy density of the Universe. Here, G is Newton's constant and H_0 is the Hubble constant; we take $H_0 = 68 \text{ kms}^{-1} \text{ Mpc}^{-1}$ [65]. The precise relationship between $\Omega(f)$ and $S_h(f)$ is theory dependent. Under any theory obeying Isaacson's formula for the stress-energy of gravitational waves [66], the energy-density spectrum is related to $S_h(f)$ by [42,62,67]

$$\Omega(f) = \frac{2\pi^2}{3H_0^2} f^3 S_h(f). \quad (6)$$

Equation (6) does not hold in general, however [67]. For ease of comparison with previous studies, we will instead take Eq. (6) as the *definition* of the canonical energy-density spectra $\Omega^A(f)$. The canonical energy-density spectra can be directly identified with true energy densities under any theory obeying Isaacson's formula. For other theories, $\Omega^A(f)$ can instead be understood simply as a function of the detector-frame observable $S_h^A(f)$.

Within each 192 s time segment (indexed by i), we form an estimator of the visible cross power between LIGO-Hanford and LIGO-Livingston:

$$\hat{C}_i(f) = \frac{1}{\Delta T} \frac{20\pi^2}{3H_0^2} f^3 \tilde{s}_{1,i}^*(f) \tilde{s}_{2,i}(f), \quad (7)$$

normalized such that the estimator's mean and variance are [42]

$$\langle \hat{C}_i(f) \rangle = \sum_A \gamma_A(f) \Omega^A(f) \quad (8)$$

and

$$\sigma_i^2(f) = \frac{1}{2\Delta T df} \left(\frac{10\pi^2}{3H_0^2} \right)^2 f^6 P_{1,i}(f) P_{2,i}(f), \quad (9)$$

respectively. Within Eqs. (7) and (9), ΔT is the segment duration, df the frequency bin width, and $P_{I,i}(f)$ is the one-sided auto-power spectral density of detector I in time segment i , defined by

$$\langle \tilde{s}_{I,i}^*(f) \tilde{s}_{I,i}(f') \rangle = \frac{1}{2} \delta(f - f') P_{I,i}(f). \quad (10)$$

The normalization of $\hat{C}(f)$ is chosen such that the contribution from each polarization appears symmetrically in Eq. (8); this choice differs by a factor of $\gamma_T(f)$ from the point estimate $\hat{Y}(f)$ typically used in stochastic analyses [42,46,49]. Finally, the cross-power estimators from each segment are optimally combined via a weighted sum to form a single cross-power spectrum for the O1 observing run,

$$\hat{C}(f) = \frac{\sum_i \hat{C}_i(f) \sigma_i^{-2}(f)}{\sum_i \sigma_i^{-2}(f)}, \quad (11)$$

with the corresponding variance

$$\sigma^{-2}(f) = \sum_i \sigma_i^{-2}(f). \quad (12)$$

Note that, unlike transient gravitational-wave searches, searches for the stochastic background are well described by Gaussian statistics due to the large number of time segments contributing to the final cross-power spectrum [68].

Given the measured cross-power spectrum $\hat{C}(f)$, we compute Bayesian evidence for various hypotheses describing the presence and polarization of a possible stochastic signal within our data. Evidence is computed using PYMULTINEST [69], a Python interface to the nested sampling code MULTINEST [70–74]. We consider several different hypotheses: (i) Gaussian noise (N): No stochastic signal is present in our data, and the measured cross power is due entirely to Gaussian noise. (ii) Signal (SIG): A stochastic background of any polarization(s) is present. (iii) Tensor-polarized (GR): The data contains a purely tensor-polarized stochastic signal, consistent with general relativity. (iv) Nonstandard polarizations (NGR): The data contains a stochastic signal with vector and/or scalar contributions. These evidences are combined to form two Bayesian odds [42]: (1) Odds $\mathcal{O}_N^{\text{SIG}}$ for the presence of a stochastic signal relative to pure noise, and (2) odds $\mathcal{O}_{\text{GR}}^{\text{NGR}}$ for the presence of nonstandard polarizations versus ordinary tensor modes. $\mathcal{O}_N^{\text{SIG}}$ quantifies evidence for the *detection* of a generically polarized stochastic background, and generally depends only on a background’s total power, not its polarization content. $\mathcal{O}_{\text{GR}}^{\text{NGR}}$ indicates if the background’s polarization is inconsistent with general relativity. In particular, the sensitivity of $\mathcal{O}_{\text{GR}}^{\text{NGR}}$ to nonstandard polarizations is not significantly affected by the strength of any tensor polarization which may also be present [42]. See the Supplemental Material [48] for further details about our hypotheses and odds ratio construction, including the priors placed on these hypotheses and their parameters.

Results.—Using the cross power measured between LIGO-Hanford and LIGO-Livingston during Advanced LIGO’s O1 observing run, we obtain odds $\ln \mathcal{O}_N^{\text{SIG}} = -0.53$ between signal and Gaussian noise hypotheses,

indicating a nondetection of the stochastic gravitational-wave background. Additionally, we find $\ln \mathcal{O}_{\text{GR}}^{\text{NGR}} = -0.25$, consistent with values expected in the presence of Gaussian noise [42]. (We will use \ln and \log to denote base- e and base-10 logarithms, respectively).

Given our nondetection, we place upper limits on the presence of tensor, vector, and scalar contributions to the stochastic background. To simultaneously constrain the properties of each polarization, we will restrict our analysis to a model assuming the presence of tensor, vector, and scalar-polarized signals (this is the TVS hypothesis in the notation of the Supplemental Material [48]). Under this hypothesis, we model the total canonical energy density of the stochastic background as a sum of power laws:

$$\Omega(f) = \Omega_0^T \left(\frac{f}{f_0}\right)^{\alpha_T} + \Omega_0^V \left(\frac{f}{f_0}\right)^{\alpha_V} + \Omega_0^S \left(\frac{f}{f_0}\right)^{\alpha_S}. \quad (13)$$

Here, Ω_0^A is the amplitude of polarization A at a reference frequency f_0 , and α_A is the corresponding spectral index. We take $f_0 = 25$ Hz [46]. Standard tensor-polarized stochastic backgrounds are predicted to be well described by power laws in the Advanced LIGO band. The expected astrophysical background from compact binary mergers, for instance, is well modeled by a power law with $\alpha_T = 2/3$ [18–20,75].

We will consider two different prior distributions for the background amplitudes: a log-uniform prior between $10^{-13} \leq \Omega_0^A \leq 10^{-5}$ and a uniform prior between $0 \leq \Omega_0^A \leq 10^{-5}$. The former (log-uniform) corresponds to the prior adopted in Ref. [42]. The latter (uniform) implicitly reproduces the maximum likelihood analysis used in previous studies, and is included to allow direct comparison to previous stochastic results [46,49]. The upper amplitude bound (10^{-5}) is consistent with limits placed by Initial LIGO and Virgo [49]. In order to be normalizable, the log-uniform prior requires a nonzero lower bound; although parameter estimation results will depend on the specific choice of lower bound, in general this dependence is weak [44]. Our lower bound (10^{-13}) is chosen to encompass small energy densities well below the reach of LIGO and Virgo at design sensitivity [23,46].

Following Ref. [42], we take our spectral index priors to be $p(\alpha_A) \propto 1 - |\alpha_A|/\alpha_{\text{MAX}}$ for $|\alpha_A| \leq \alpha_{\text{MAX}}$ and $p(\alpha_A) = 0$ elsewhere. This prior preferentially weights flat energy-density spectra, penalizing spectra which are more steeply positively or negatively sloped in the Advanced LIGO band. We conservatively choose $\alpha_{\text{MAX}} = 8$, allowing for energy-density spectra significantly steeper than backgrounds predicted from known astrophysical sources (like compact binary mergers).

We perform parameter estimation using posterior samples obtained by PYMULTINEST. Figure 2 shows posteriors on the tensor, vector, and scalar background amplitudes, under each choice of amplitude prior. The dashed and dot-dashed

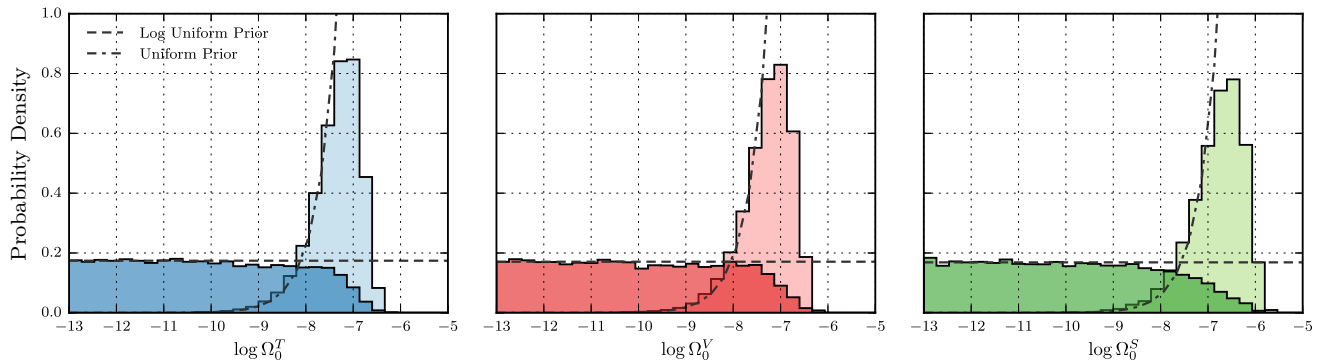


FIG. 2. Posteriors on the tensor (left), vector (center), and scalar (right) stochastic background amplitudes at reference frequency $f_0 = 25$ Hz. Within each subplot, dark posteriors show results obtained assuming log-uniform priors (dashed curves) on Ω_0^A , while light posteriors show results corresponding to uniform amplitude priors (dot-dashed curves). The prior curves shown here have been renormalized by constant factors to illustrate consistency with the posteriors below our measured upper limits. These posteriors correspond to the 95% credible upper limits listed in Table I. Relative to the log-uniform priors, the uniform amplitude priors preferentially weight loud stochastic signals and therefore yield more conservative upper limits.

curves are proportional to the log-uniform and uniform amplitude priors, respectively; each prior curve has been renormalized by a constant factor to illustrate consistency between our priors and posteriors at small Ω_0^A . We can now place upper limits on the amplitude of each component at $f_0 = 25$ Hz. The 95% credible upper limits on the amplitude of each polarization are listed in Table I for each choice of prior (for convenience, we list limits in terms of both $\log \Omega_0^A$ and Ω_0^A). As no signal was detected, our posteriors on the spectral indices α_A are dominated by our prior. Full parameter estimation results, including posteriors on α_A , are given in the Supplemental Material [48].

Care should be taken when comparing these upper limits to those obtained in previous analyses (e.g., Table I of Ref. [46]). Three important distinctions should be kept in mind. First, the amplitude posteriors in Fig. 2 (and hence the limits in Table I) are obtained after marginalization over spectral index. Previous analyses, on the other hand, typically assume specific fixed spectral indices or present exclusion curves in the $\Omega_0^T - \alpha_T$ plane [46]. Second, Bayesian upper limits may be strongly influenced by one’s adopted prior. Uniform amplitude priors, for instance, preferentially weight larger signals and hence yield larger upper limits, while log-uniform priors support smaller

signal amplitudes, giving tighter limits. Finally, our results are obtained under a specific signal hypothesis allowing simultaneously for tensor, vector, and scalar polarizations. These limits are not generically identical to those that would be obtained if we allowed for tensor modes alone. In the Supplemental Material [48], we have tabulated upper limits under a variety of signal hypotheses allowing for each unique combination of gravitational-wave polarizations (our results, though, do not vary considerably between hypotheses). We have additionally verified that, under the GR (tensor-only) hypothesis with delta-function priors on the background’s spectral index, we recover upper limits identical to results previously published in Ref. [46].

Conclusion.—The direct measurement of gravitational-wave polarizations may open the door to powerful new tests of gravity. Such measurements largely depend only on the geometry of a gravitational wave’s strain and its direction of propagation, not on the details of any specific theory of gravity. Recently, the Advanced LIGO-Virgo observation of the binary black hole merger GW170814 has enabled the first direct study of gravitational-wave polarizations [4,15]. While LIGO and Virgo are limited in their ability to discern the polarization of gravitational-wave transients, the future construction of additional detectors, like KAGRA [76,77]

TABLE I. 95% credible upper limits on the log amplitudes of tensor, vector, and scalar modes in the stochastic background at reference frequency $f_0 = 25$ Hz. We assume an energy-density spectrum in which all three modes are present, and present limits following marginalization over the spectral index of each component [see Eq. (13)]. We show results for two different amplitude priors: a log-uniform prior ($dp/d\log \Omega_0 \propto 1$; top row) and a uniform prior ($dp/d\Omega_0 \propto 1$; bottom row). Additional parameter estimation results are shown in the Supplemental Material [48].

Prior	$\log \Omega_0^T$	$\log \Omega_0^V$	$\log \Omega_0^S$	Ω_0^T	Ω_0^V	Ω_0^S
Log uniform	-7.25	-7.20	-6.96	5.58×10^{-8}	6.35×10^{-8}	1.08×10^{-7}
Uniform	-6.70	-6.59	-6.07	2.02×10^{-7}	2.54×10^{-7}	8.44×10^{-7}

and LIGO-India [78], will help to break existing degeneracies and allow for increasingly precise polarization measurements.

Long-duration signals offer further opportunities to study gravitational-wave polarizations. Detections of continuous sources like rotating neutron stars [44,45] and the stochastic background [42] will offer the ability to directly measure and/or constrain gravitational-wave polarizations, even in the absence of additional detectors. In this Letter, we have conducted a search for a generically polarized stochastic background of gravitational waves using data from Advanced LIGO's O1 observing run. Although we find no evidence for the presence of a background (of any polarization), we have succeeded in placing the first direct upper limits (listed in Table I) on the contributions of vector and scalar modes to the stochastic background.

The authors gratefully acknowledge the support of the United States National Science Foundation (NSF) for the construction and operation of the LIGO Laboratory and Advanced LIGO as well as the Science and Technology Facilities Council (STFC) of the United Kingdom, the Max-Planck-Society (MPS), and the State of Niedersachsen, Germany for support of the construction of Advanced LIGO and construction and operation of the GEO600 detector. Additional support for Advanced LIGO was provided by the Australian Research Council. The authors gratefully acknowledge the Italian Istituto Nazionale di Fisica Nucleare (INFN), the French Centre National de la Recherche Scientifique (CNRS) and the Foundation for Fundamental Research on Matter supported by the Netherlands Organisation for Scientific Research, for the construction and operation of the Virgo detector and the creation and support of the EGO consortium. The authors also gratefully acknowledge research support from these agencies as well as by the Council of Scientific and Industrial Research of India, the Department of Science and Technology, India, the Science & Engineering Research Board (SERB), India, the Ministry of Human Resource Development, India, the Spanish Agencia Estatal de Investigación, the Vicepresidència i Conselleria d'Innovació, Recerca i Turisme and the Conselleria d'Educació i Universitat del Govern de les Illes Balears, the Conselleria d'Educació, Investigació, Cultura i Esport de la Generalitat Valenciana, the National Science Centre of Poland, the Swiss National Science Foundation (SNSF), the Russian Foundation for Basic Research, the Russian Science Foundation, the European Commission, the European Regional Development Funds (ERDF), the Royal Society, the Scottish Funding Council, the Scottish Universities Physics Alliance, the Hungarian Scientific Research Fund (OTKA), the Lyon Institute of Origins (LIO), the Paris Île-de-France Region, the National Research, Development and Innovation Office Hungary (NKFI), the National Research Foundation of Korea, Industry Canada and the Province of Ontario through the Ministry of Economic Development and

Innovation, the Natural Sciences and Engineering Research Council Canada, the Canadian Institute for Advanced Research, the Brazilian Ministry of Science, Technology, Innovations, and Communications, the International Center for Theoretical Physics South American Institute for Fundamental Research (ICTP-SAIFR), the Research Grants Council of Hong Kong, the National Natural Science Foundation of China (NSFC), the Leverhulme Trust, the Research Corporation, the Ministry of Science and Technology (MOST), Taiwan and the Kavli Foundation. The authors gratefully acknowledge the support of the NSF, STFC, MPS, INFN, CNRS and the State of Niedersachsen, Germany for provision of computational resources.

-
- [1] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **116**, 061102 (2016).
 - [2] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **116**, 241103 (2016).
 - [3] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **118**, 221101 (2017).
 - [4] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **119**, 141101 (2017).
 - [5] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **119**, 161101 (2017).
 - [6] F. Acernese *et al.*, *Classical Quantum Gravity* **32**, 024001 (2015).
 - [7] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **116**, 131103 (2016).
 - [8] F. Acernese *et al.*, *Classical Quantum Gravity* **32**, 024001 (2015).
 - [9] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **116**, 221101 (2016).
 - [10] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. X* **6**, 041015 (2016).
 - [11] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Astrophys. J.* **848**, L13 (2017).
 - [12] D. M. Eardley, D. L. Lee, A. P. Lightman, R. V. Wagoner, and C. M. Will, *Phys. Rev. Lett.* **30**, 884 (1973).
 - [13] D. M. Eardley, D. L. Lee, and A. P. Lightman, *Phys. Rev. D* **8**, 3308 (1973).
 - [14] C. M. Will, *Living Rev. Relativity* **17**, 4 (2014).
 - [15] M. Isi and A. J. Weinstein, arXiv:1710.03794.
 - [16] K. Chatziioannou, N. Yunes, and N. Cornish, *Phys. Rev. D* **86**, 022004 (2012).
 - [17] E. Berti *et al.*, *Classical Quantum Gravity* **32**, 243001 (2015).
 - [18] P. A. Rosado, *Phys. Rev. D* **84**, 084004 (2011).
 - [19] X.-J. Zhu, E. Howell, T. Regimbau, D. Blair, and Z.-H. Zhu, *Astrophys. J.* **739**, 86 (2011).
 - [20] C. Wu, V. Mandic, and T. Regimbau, *Phys. Rev. D* **85**, 104024 (2012).
 - [21] X.-J. Zhu, E. J. Howell, D. G. Blair, and Z.-H. Zhu, *Mon. Not. R. Astron. Soc.* **431**, 882 (2013).
 - [22] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **116**, 131102 (2016).
 - [23] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **120**, 091101 (2018).

- [24] A. Buonanno, G. Sigl, G. G. Raffelt, H.-T. Janka, and E. Müller, *Phys. Rev. D* **72**, 084001 (2005).
- [25] X.-J. Zhu, E. Howell, and D. Blair, *Mon. Not. R. Astron. Soc. Lett.* **409**, L132 (2010).
- [26] K. Crocker, V. Mandic, T. Regimbau, K. Belczynski, W. Gladysz, K. Olive, T. Prestegard, and E. Vangioni, *Phys. Rev. D* **92**, 063005 (2015).
- [27] P. A. Rosado, *Phys. Rev. D* **86**, 104007 (2012).
- [28] C.-J. Wu, V. Mandic, and T. Regimbau, *Phys. Rev. D* **87**, 042002 (2013).
- [29] D. Talukder, E. Thrane, S. Bose, and T. Regimbau, *Phys. Rev. D* **89**, 123008 (2014).
- [30] S. Ölmez, V. Mandic, and X. Siemens, *Phys. Rev. D* **81**, 104028 (2010).
- [31] J. Aasi *et al.*, *Phys. Rev. Lett.* **112**, 131101 (2014).
- [32] M. Maggiore, *Phys. Rep.* **331**, 283 (2000).
- [33] J. T. Giblin and E. Thrane, *Phys. Rev. D* **90**, 107502 (2014).
- [34] R. Easther, J. T. Giblin, and E. A. Lim, *Phys. Rev. Lett.* **99**, 221301 (2007).
- [35] J. L. Cook and L. Sorbo, *Phys. Rev. D* **85**, 023534 (2012).
- [36] C. Caprini, R. Durrer, and G. Servant, *Phys. Rev. D* **77**, 124015 (2008).
- [37] C. Caprini, R. Durrer, and G. Servant, *J. Cosmol. Astropart. Phys.* **12** (2009) 024.
- [38] A. Lopez and K. Freese, *J. Cosmol. Astropart. Phys.* **1** (2015) 037.
- [39] A. Nishizawa, A. Taruya, K. Hayama, S. Kawamura, and M.-a. Sakagami, *Phys. Rev. D* **79**, 082002 (2009).
- [40] A. Nishizawa, A. Taruya, and S. Kawamura, *Phys. Rev. D* **81**, 104043 (2010).
- [41] A. Nishizawa and K. Hayama, *Phys. Rev. D* **88**, 064005 (2013).
- [42] T. Callister, A. S. Biscoveanu, N. Christensen, M. Isi, A. Matas, O. Minazzoli, T. Regimbau, M. Sakellariadou, J. Tasson, and E. Thrane, *Phys. Rev. X* **7**, 041058 (2017).
- [43] M. Isi, A. J. Weinstein, C. Mead, and M. Pitkin, *Phys. Rev. D* **91**, 082002 (2015).
- [44] M. Isi, M. Pitkin, and A. J. Weinstein, *Phys. Rev. D* **96**, 042001 (2017).
- [45] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **120**, 031104 (2018).
- [46] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **118**, 121101 (2017).
- [47] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **118**, 121102 (2017).
- [48] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevLett.120.201102> for an expanded discussion of hypothesis testing, calibration uncertainties, and complete parameter estimation results.
- [49] J. Aasi *et al.*, *Phys. Rev. Lett.* **113**, 231101 (2014).
- [50] P. D. Welch, *IEEE Trans. Audio Electroacoust.* **15**, 70 (1967).
- [51] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **118**, 121101 (2017).
- [52] E. Thrane, N. Christensen, and R. M. S. Schofield, *Phys. Rev. D* **87**, 123009 (2013).
- [53] E. Thrane, N. Christensen, R. M. S. Schofield, and A. Effler, *Phys. Rev. D* **90**, 023013 (2014).
- [54] Y. Himemoto and A. Taruya, *Phys. Rev. D* **96**, 022004 (2017).
- [55] C. Cahillane *et al.*, *Phys. Rev. D* **96**, 102001 (2017).
- [56] J. T. Whelan, E. L. Robinson, J. D. Romano, and E. H. Thrane, *J. Phys. Conf. Ser.* **484**, 012027 (2014).
- [57] R. Jackiw and S.-Y. Pi, *Phys. Rev. D* **68**, 104012 (2003).
- [58] S. Alexander, L. S. Finn, and N. Yunes, *Phys. Rev. D* **78**, 066005 (2008).
- [59] S. Alexander and N. Yunes, *Phys. Rep.* **480**, 1 (2009).
- [60] V. A. Kostelecký, *Phys. Rev. D* **69**, 105009 (2004).
- [61] V. A. Kostelecký and M. Mewes, *Phys. Lett. B* **757**, 510 (2016).
- [62] B. Allen and J. D. Romano, *Phys. Rev. D* **59**, 102001 (1999).
- [63] N. Christensen, *Phys. Rev. D* **46**, 5250 (1992).
- [64] J. D. Romano and N. J. Cornish, *Living Rev. Relativity* **20**, 2 (2017).
- [65] P. A. R. Ade *et al.*, *Astron. Astrophys.* **594**, A13 (2016).
- [66] R. A. Isaacson, *Phys. Rev.* **166**, 1272 (1968).
- [67] M. Isi and L. Stein, LIGO Document No. P1700234 (to be published).
- [68] D. Meacher, M. Coughlin, S. Morris, T. Regimbau, N. Christensen, S. Kandhasamy, V. Mandic, J. D. Romano, and E. Thrane, *Phys. Rev. D* **92**, 063002 (2015).
- [69] J. Buchner, A. Georgakakis, K. Nandra, L. Hsu, C. Rangel, M. Brightman, A. Merloni, M. Salvato, J. Donley, and D. Kocevski, *Astron. Astrophys.* **564**, A125 (2014).
- [70] F. Feroz and M. P. Hobson, *Mon. Not. R. Astron. Soc.* **384**, 449 (2008).
- [71] F. Feroz, M. P. Hobson, and M. Bridges, *Mon. Not. R. Astron. Soc.* **398**, 1601 (2009).
- [72] F. Feroz, M. P. Hobson, E. Cameron, and A. N. Pettitt, [arXiv:1306.2144](https://arxiv.org/abs/1306.2144).
- [73] J. Skilling, *AIP Conf. Proc.* **735**, 395 (2004).
- [74] J. Skilling, *Bayesian Analysis* **1**, 833 (2006).
- [75] T. Callister, L. Sammut, S. Qiu, I. Mandel, and E. Thrane, *Phys. Rev. X* **6**, 031018 (2016).
- [76] Y. Aso, Y. Michimura, K. Somiya, M. Ando, O. Miyakawa, T. Sekiguchi, D. Tatsumi, and H. Yamamoto, *Phys. Rev. D* **88**, 043007 (2013).
- [77] T. Akutsu *et al.*, *Prog. Theor. Exp. Phys.* **2018**, 013F01 (2018).
- [78] B. Iyer *et al.*, LIGO-India Tech. Report No. LIGO-M1100296 (2011), <https://dcc.ligo.org/LIGO-M1100296/public>.

B. P. Abbott,¹ R. Abbott,¹ T. D. Abbott,² F. Acernese,^{3,4} K. Ackley,^{5,6} C. Adams,⁷ T. Adams,⁸ P. Addesso,⁹ R. X. Adhikari,¹ V. B. Adya,¹⁰ C. Affeldt,¹⁰ M. Afrough,¹¹ B. Agarwal,¹² M. Agathos,¹³ K. Agatsuma,¹⁴ N. Aggarwal,¹⁵ O. D. Aguiar,¹⁶ L. Aiello,^{17,18} A. Ain,¹⁹ P. Ajith,²⁰ B. Allen,^{10,21,22} G. Allen,¹² A. Allocca,^{23,24} P. A. Altin,²⁵ A. Amato,²⁶ A. Ananyeva,¹

S. B. Anderson,¹ W. G. Anderson,²¹ S. V. Angelova,²⁷ S. Antier,²⁸ S. Appert,¹ K. Arai,¹ M. C. Araya,¹ J. S. Areeda,²⁹ N. Arnaud,^{28,30} S. Ascenzi,^{31,32} G. Ashton,¹⁰ M. Ast,³³ S. M. Aston,⁷ P. Astone,³⁴ D. V. Atallah,³⁵ P. Aufmuth,²² C. Aubert,¹⁰ K. AultO'Neal,³⁶ C. Austin,² A. Avila-Alvarez,²⁹ S. Babak,³⁷ P. Bacon,³⁸ M. K. M. Bader,¹⁴ S. Bae,³⁹ P. T. Baker,⁴⁰ F. Baldaccini,^{41,42} G. Ballardini,³⁰ S. W. Ballmer,⁴³ S. Banagiri,⁴⁴ J. C. Barayoga,¹ S. E. Barclay,⁴⁵ B. C. Barish,¹ D. Barker,⁴⁶ K. Barkett,⁴⁷ F. Barone,^{3,4} B. Barr,⁴⁵ L. Barsotti,¹⁵ M. Barsuglia,³⁸ D. Barta,⁴⁸ J. Bartlett,⁴⁶ I. Bartos,^{49,5} R. Bassiri,⁵⁰ A. Basti,^{23,24} J. C. Batch,⁴⁶ M. Bawaj,^{51,42} J. C. Bayley,⁴⁵ M. Bazzan,^{52,53} B. Bécsy,⁵⁴ C. Beer,¹⁰ M. Bejger,⁵⁵ I. Belahcene,²⁸ A. S. Bell,⁴⁵ B. K. Berger,¹ G. Bergmann,¹⁰ J. J. Bero,⁵⁶ C. P. L. Berry,⁵⁷ D. Bersanetti,⁵⁸ A. Bertolini,¹⁴ J. Betzwieser,⁷ S. Bhagwat,⁴³ R. Bhandare,⁵⁹ I. A. Bilenko,⁶⁰ G. Billingsley,¹ C. R. Billman,⁵ J. Birch,⁷ R. Birney,⁶¹ O. Birnholtz,¹⁰ S. Biscans,^{1,15} S. Biscoveanu,^{62,6} A. Bisht,²² M. Bitossi,^{30,24} C. Biwer,⁴³ M. A. Bizouard,²⁸ J. K. Blackburn,¹ J. Blackman,⁴⁷ C. D. Blair,^{1,63} D. G. Blair,⁶³ R. M. Blair,⁴⁶ S. Bloemen,⁶⁴ O. Bock,¹⁰ N. Bode,¹⁰ M. Boer,⁶⁵ G. Bogaert,⁶⁵ A. Bohe,³⁷ F. Bondu,⁶⁶ E. Bonilla,⁵⁰ R. Bonnand,⁸ B. A. Boom,¹⁴ R. Bork,¹ V. Boschi,^{30,24} S. Bose,^{67,19} K. Bossie,⁷ Y. Bouffanais,³⁸ A. Bozzi,³⁰ C. Bradaschia,²⁴ P. R. Brady,²¹ M. Branchesi,^{17,18} J. E. Brau,⁶⁸ T. Briant,⁶⁹ A. Brillat,⁶⁵ M. Brinkmann,¹⁰ V. Brisson,²⁸ P. Brockill,²¹ J. E. Broida,⁷⁰ A. F. Brooks,¹ D. A. Brown,⁴³ D. D. Brown,⁷¹ S. Brunett,¹ C. C. Buchanan,² A. Buikema,¹⁵ T. Bulik,⁷² H. J. Bulten,^{73,14} A. Buonanno,^{37,74} D. Buskulic,⁸ C. Buy,³⁸ R. L. Byer,⁵⁰ M. Cabero,¹⁰ L. Cadonati,⁷⁵ G. Cagnoli,^{26,76} C. Cahillane,¹ J. Calderón Bustillo,⁷⁵ T. A. Callister,¹ E. Calloni,^{77,4} J. B. Camp,⁷⁸ M. Canepa,^{79,58} P. Canizares,⁶⁴ K. C. Cannon,⁸⁰ H. Cao,⁷¹ J. Cao,⁸¹ C. D. Capano,¹⁰ E. Capocasa,³⁸ F. Carbognani,³⁰ S. Caride,⁸² M. F. Carney,⁸³ J. Casanueva Diaz,²⁸ C. Casentini,^{31,32} S. Caudill,^{21,14} M. Cavaglià,¹¹ F. Cavalier,²⁸ R. Cavalieri,³⁰ G. Cella,²⁴ C. B. Cepeda,¹ P. Cerdá-Durán,⁸⁴ G. Cerretani,^{23,24} E. Cesarini,^{85,32} S. J. Chamberlin,⁶² M. Chan,⁴⁵ S. Chao,⁸⁶ P. Charlton,⁸⁷ E. Chase,⁸⁸ E. Chassande-Mottin,³⁸ D. Chatterjee,²¹ B. D. Cheeseboro,⁴⁰ H. Y. Chen,⁸⁹ X. Chen,⁶³ Y. Chen,⁴⁷ H.-P. Cheng,⁵ H. Chia,⁵ A. Chincarini,⁵⁸ A. Chiummo,³⁰ T. Chmiel,⁸³ H. S. Cho,⁹⁰ M. Cho,⁷⁴ J. H. Chow,²⁵ N. Christensen,^{70,65} Q. Chu,⁶³ A. J. K. Chua,¹³ S. Chua,⁶⁹ A. K. W. Chung,⁹¹ S. Chung,⁶³ G. Ciani,^{5,52,53} R. Ciolfi,^{92,93} C. E. Cirelli,⁵⁰ A. Cirone,^{79,58} F. Clara,⁴⁶ J. A. Clark,⁷⁵ P. Clearwater,⁹⁴ F. Cleva,⁶⁵ C. Cocchieri,¹¹ E. Coccia,^{17,18} P.-F. Cohadon,⁶⁹ D. Cohen,²⁸ A. Colla,^{95,34} C. G. Collette,⁹⁶ L. R. Cominsky,⁹⁷ M. Constanicio Jr.,¹⁶ L. Conti,⁵³ S. J. Cooper,⁵⁷ P. Corban,⁷ T. R. Corbitt,² I. Cordero-Carrión,⁹⁸ K. R. Corley,⁴⁹ N. Cornish,⁹⁹ A. Corsi,⁸² S. Cortese,³⁰ C. A. Costa,¹⁶ E. Coughlin,⁷⁰ M. W. Coughlin,^{70,1} S. B. Coughlin,⁸⁸ J.-P. Coulon,⁶⁵ S. T. Countryman,⁴⁹ P. Couvares,¹ P. B. Covas,¹⁰⁰ E. E. Cowan,⁷⁵ D. M. Coward,⁶³ M. J. Cowart,⁷ D. C. Coyne,¹ R. Coyne,⁸² J. D. E. Creighton,²¹ T. D. Creighton,¹⁰¹ J. Cripe,² S. G. Crowder,¹⁰² T. J. Cullen,^{29,2} A. Cumming,⁴⁵ L. Cunningham,⁴⁵ E. Cuoco,³⁰ T. Dal Canton,⁷⁸ G. Dálya,⁵⁴ S. L. Danilishin,^{22,10} S. D'Antonio,³² K. Danzmann,^{22,10} A. Dasgupta,¹⁰³ C. F. Da Silva Costa,⁵ V. Dattilo,³⁰ I. Dave,⁵⁹ M. Davier,²⁸ D. Davis,⁴³ E. J. Daw,¹⁰⁴ B. Day,⁷⁵ S. De,⁴³ D. DeBra,⁵⁰ J. Degallaix,²⁶ M. De Laurentis,^{17,4} S. Deléglise,⁶⁹ W. Del Pozzo,^{57,23,24} N. Demos,¹⁵ T. Denker,¹⁰ T. Dent,¹⁰ R. De Pietri,^{105,106} V. Dergachev,³⁷ R. De Rosa,^{77,4} R. T. DeRosa,⁷ C. De Rossi,^{26,30} R. DeSalvo,¹⁰⁷ O. de Varona,¹⁰ J. Devenson,²⁷ S. Dhurandhar,¹⁹ M. C. Díaz,¹⁰¹ L. Di Fiore,⁴ M. Di Giovanni,^{108,93} T. Di Girolamo,^{49,77,4} A. Di Lieto,^{23,24} S. Di Pace,^{95,34} I. Di Palma,^{95,34} F. Di Renzo,^{23,24} Z. Doctor,⁸⁹ V. Dolique,²⁶ F. Donovan,¹⁵ K. L. Dooley,¹¹ S. Doravari,¹⁰ I. Dorrington,³⁵ R. Douglas,⁴⁵ M. Dovale Álvarez,⁵⁷ T. P. Downes,²¹ M. Drago,¹⁰ C. Dreissigacker,¹⁰ J. C. Driggers,⁴⁶ Z. Du,⁸¹ M. Ducrot,⁸ P. Dupej,⁴⁵ S. E. Dwyer,⁴⁶ T. B. Edo,¹⁰⁴ M. C. Edwards,⁷⁰ A. Effler,⁷ H.-B. Eggenstein,^{37,10} P. Ehrens,¹ J. Eichholz,¹ S. S. Eikenberry,⁵ R. A. Eisenstein,¹⁵ R. C. Essick,¹⁵ D. Estevez,⁸ Z. B. Etienne,⁴⁰ T. Etzel,¹ M. Evans,¹⁵ T. M. Evans,⁷ M. Factourovich,⁴⁹ V. Fafone,^{31,32,17} H. Fair,⁴³ S. Fairhurst,³⁵ X. Fan,⁸¹ S. Farinon,⁵⁸ B. Farr,⁸⁹ W. M. Farr,⁵⁷ E. J. Fauchon-Jones,³⁵ M. Favata,¹⁰⁹ M. Fays,³⁵ C. Fee,⁸³ H. Fehrmann,¹⁰ J. Feicht,¹ M. M. Fejer,⁵⁰ A. Fernandez-Galiana,¹⁵ I. Ferrante,^{23,24} E. C. Ferreira,¹⁶ F. Ferrini,³⁰ F. Fidecaro,^{23,24} D. Finstad,⁴³ I. Fiori,³⁰ D. Fiorucci,³⁸ M. Fishbach,⁸⁹ R. P. Fisher,⁴³ M. Fitz-Axen,⁴⁴ R. Flaminio,^{26,110} M. Fletcher,⁴⁵ H. Fong,¹¹¹ J. A. Font,^{84,112} P. W. F. Forsyth,²⁵ S. S. Forsyth,⁷⁵ J.-D. Fournier,⁶⁵ S. Frasca,^{95,34} F. Frasconi,²⁴ Z. Frei,⁵⁴ A. Freise,⁵⁷ R. Frey,⁶⁸ V. Frey,²⁸ E. M. Fries,¹ P. Fritschel,¹⁵ V. V. Frolov,⁷ P. Fulda,⁵ M. Fyffe,⁷ H. Gabbard,⁴⁵ B. U. Gadre,¹⁹ S. M. Gaebel,⁵⁷ J. R. Gair,¹¹³ L. Gammaitoni,⁴¹ M. R. Ganija,⁷¹ S. G. Gaonkar,¹⁹ C. Garcia-Quiros,¹⁰⁰ F. Garufi,^{77,4} B. Gateley,⁴⁶ S. Gaudio,³⁶ G. Gaur,¹¹⁴ V. Gayathri,¹¹⁵ N. Gehrels,^{78,†} G. Gemme,⁵⁸ E. Genin,³⁰ A. Gennai,²⁴ D. George,¹² J. George,⁵⁹ L. Gergely,¹¹⁶ V. Germain,⁸ S. Ghonge,⁷⁵ Abhirup Ghosh,²⁰ Archisman Ghosh,^{20,14} S. Ghosh,^{64,14,21} J. A. Giaime,^{2,7} K. D. Giardina,⁷ A. Giazotto,^{24,‡} K. Gill,³⁶ L. Glover,¹⁰⁷ E. Goetz,¹¹⁷ R. Goetz,⁵ S. Gomes,³⁵ B. Goncharov,⁶ G. González,² J. M. Gonzalez Castro,^{23,24} A. Gopakumar,¹¹⁸ M. L. Gorodetsky,⁶⁰ S. E. Gossan,¹ M. Gosselin,³⁰ R. Gouaty,⁸ A. Grado,^{119,4} C. Graef,⁴⁵ M. Granata,²⁶ A. Grant,⁴⁵ S. Gras,¹⁵ C. Gray,⁴⁶ G. Greco,^{120,121} A. C. Green,⁵⁷ E. M. Gretarsson,³⁶ P. Groot,⁶⁴ H. Grote,¹⁰ S. Grunewald,³⁷ P. Gruning,²⁸ G. M. Guidi,^{120,121} X. Guo,⁸¹ A. Gupta,⁶² M. K. Gupta,¹⁰³ K. E. Gushwa,¹ E. K. Gustafson,¹ R. Gustafson,¹¹⁷

O. Halim,^{18,17} B. R. Hall,⁶⁷ E. D. Hall,¹⁵ E. Z. Hamilton,³⁵ G. Hammond,⁴⁵ M. Haney,¹²² M. M. Hanke,¹⁰ J. Hanks,⁴⁶
 C. Hanna,⁶² M. D. Hannam,³⁵ O. A. Hannuksela,⁹¹ J. Hanson,⁷ T. Hardwick,² J. Harms,^{17,18} G. M. Harry,¹²³ I. W. Harry,³⁷
 M. J. Hart,⁴⁵ C.-J. Haster,¹¹¹ K. Haughian,⁴⁵ J. Healy,⁵⁶ A. Heidmann,⁶⁹ M. C. Heintze,⁷ H. Heitmann,⁶⁵ P. Hello,²⁸
 G. Hemming,³⁰ M. Hendry,⁴⁵ I. S. Heng,⁴⁵ J. Hennig,⁴⁵ A. W. Heptonstall,¹ M. Heurs,^{10,22} S. Hild,⁴⁵ T. Hinderer,⁶⁴
 D. Hoak,³⁰ D. Hofman,²⁶ K. Holt,⁷ D. E. Holz,⁸⁹ P. Hopkins,³⁵ C. Horst,²¹ J. Hough,⁴⁵ E. A. Houston,⁴⁵ E. J. Howell,⁶³
 A. Hreibi,⁶⁵ Y. M. Hu,¹⁰ E. A. Huerta,¹² D. Huet,²⁸ B. Hughey,³⁶ S. Husa,¹⁰⁰ S. H. Huttner,⁴⁵ T. Huynh-Dinh,⁷ N. Indik,¹⁰
 R. Inta,⁸² G. Intini,^{95,34} H. N. Isa,⁴⁵ J.-M. Isac,⁶⁹ M. Isi,¹ B. R. Iyer,²⁰ K. Izumi,⁴⁶ T. Jacqmin,⁶⁹ K. Jani,⁷⁵ P. Jaranowski,¹²⁴
 S. Jawahar,⁶¹ F. Jiménez-Forteza,¹⁰⁰ W. W. Johnson,² D. I. Jones,¹²⁵ R. Jones,⁴⁵ R. J. G. Jonker,¹⁴ L. Ju,⁶³ J. Junker,¹⁰
 C. V. Kalaghatgi,³⁵ V. Kalogera,⁸⁸ B. Kamai,¹ S. Kandhasamy,⁷ G. Kang,³⁹ J. B. Kanner,¹ S. J. Kapadia,²¹ S. Karki,⁶⁸
 K. S. Karvinen,¹⁰ M. Kasprzack,² M. Katolik,¹² E. Katsavounidis,¹⁵ W. Katzman,⁷ S. Kaufer,²² K. Kawabe,⁴⁶ F. Kéfélian,⁶⁵
 D. Keitel,⁴⁵ A. J. Kemball,¹² R. Kennedy,¹⁰⁴ C. Kent,³⁵ J. S. Key,¹²⁶ F. Y. Khalili,⁶⁰ I. Khan,^{17,32} S. Khan,¹⁰ Z. Khan,¹⁰³
 E. A. Khazanov,¹²⁷ N. Kijbunchoo,²⁵ Chunglee Kim,¹²⁸ J. C. Kim,¹²⁹ K. Kim,⁹¹ W. Kim,⁷¹ W. S. Kim,¹³⁰ Y.-M. Kim,⁹⁰
 S. J. Kimbrell,⁷⁵ E. J. King,⁷¹ P. J. King,⁴⁶ M. Kinley-Hanlon,¹²³ R. Kirchhoff,¹⁰ J. S. Kissel,⁴⁶ L. Kleybolte,³³ S. Klimentko,⁵
 T. D. Knowles,⁴⁰ P. Koch,¹⁰ S. M. Koehlenbeck,¹⁰ S. Koley,¹⁴ V. Kondrashov,¹ A. Kontos,¹⁵ M. Korobko,³³ W. Z. Korth,¹
 I. Kowalska,⁷² D. B. Kozak,¹ C. Krämer,¹⁰ V. Kringel,¹⁰ A. Królak,^{131,132} G. Kuehn,¹⁰ P. Kumar,¹¹¹ R. Kumar,¹⁰³ S. Kumar,²⁰
 L. Kuo,⁸⁶ A. Kutynia,¹³¹ S. Kwang,²¹ B. D. Lackey,³⁷ K. H. Lai,⁹¹ M. Landry,⁴⁶ R. N. Lang,¹³³ J. Lange,⁵⁶ B. Lantz,⁵⁰
 R. K. Lanza,¹⁵ A. Lartaux-Vollard,²⁸ P. D. Lasky,⁶ M. Laxen,⁷ A. Lazzarini,¹ C. Lazzaro,⁵³ P. Leaci,^{95,34} S. Leavey,⁴⁵
 C. H. Lee,⁹⁰ H. K. Lee,¹³⁴ H. M. Lee,¹³⁵ H. W. Lee,¹²⁹ K. Lee,⁴⁵ J. Lehmann,¹⁰ A. Lenon,⁴⁰ M. Leonardi,^{108,93} N. Leroy,²⁸
 N. Letendre,⁸ Y. Levin,⁶ T. G. F. Li,⁹¹ S. D. Linker,¹⁰⁷ T. B. Littenberg,¹³⁶ J. Liu,⁶³ R. K. L. Lo,⁹¹ N. A. Lockerbie,⁶¹
 L. T. London,³⁵ J. E. Lord,⁴³ M. Lorenzini,^{17,18} V. Lorette,¹³⁷ M. Lormand,⁷ G. Losurdo,²⁴ J. D. Lough,¹⁰ C. O. Lousto,⁵⁶
 G. Lovelace,²⁹ H. Lück,^{22,10} D. Lumaca,^{31,32} A. P. Lundgren,¹⁰ R. Lynch,¹⁵ Y. Ma,⁴⁷ R. Macas,³⁵ S. Macfoy,²⁷
 B. Machenschalk,¹⁰ M. MacInnis,¹⁵ D. M. Macleod,³⁵ I. Magaña Hernandez,²¹ F. Magaña-Sandoval,⁴³
 L. Magaña Zertuche,⁴³ R. M. Magee,⁶² E. Majorana,³⁴ I. Maksimovic,¹³⁷ N. Man,⁶⁵ V. Mandic,⁴⁴ V. Mangano,⁴⁵
 G. L. Mansell,²⁵ M. Manske,^{21,25} M. Mantovani,³⁰ F. Marchesoni,^{51,42} F. Marion,⁸ S. Márka,⁴⁹ Z. Márka,⁴⁹ C. Markakis,¹²
 A. S. Markosyan,⁵⁰ A. Markowitz,¹ E. Maros,¹ A. Marquina,⁹⁸ F. Martelli,^{120,121} L. Martellini,⁶⁵ I. W. Martin,⁴⁵
 R. M. Martin,¹⁰⁹ D. V. Martynov,¹⁵ K. Mason,¹⁵ E. Massera,¹⁰⁴ A. Masserot,⁸ T. J. Massinger,¹ M. Masso-Reid,⁴⁵
 S. Mastrogiovanni,^{95,34} A. Matas,⁴⁴ F. Matichard,^{1,15} L. Matone,⁴⁹ N. Mavalvala,¹⁵ N. Mazumder,⁶⁷ R. McCarthy,⁴⁶
 D. E. McClelland,²⁵ S. McCormick,⁷ L. McCuller,¹⁵ S. C. McGuire,¹³⁸ G. McIntyre,¹ J. McIver,¹ D. J. McManus,²⁵
 L. McNeill,⁶ T. McRae,²⁵ S. T. McWilliams,⁴⁰ D. Meacher,⁶² G. D. Meadors,^{37,10} M. Mehmet,¹⁰ J. Meidam,¹⁴
 E. Mejuto-Villa,⁹ A. Melatos,⁹⁴ G. Mendell,⁴⁶ R. A. Mercer,²¹ E. L. Merilh,⁴⁶ M. Merzougui,⁶⁵ S. Meshkov,¹
 C. Messenger,⁴⁵ C. Messick,⁶² R. Metzdorff,⁶⁹ P. M. Meyers,⁴⁴ H. Miao,⁵⁷ C. Michel,²⁶ H. Middleton,⁵⁷ E. E. Mikhailov,¹³⁹
 L. Milano,^{77,4} A. L. Miller,^{5,95,34} B. B. Miller,⁸⁸ J. Miller,¹⁵ M. Millhouse,⁹⁹ M. C. Milovich-Goff,¹⁰⁷ O. Minazzoli,^{65,140}
 Y. Minenkov,³² J. Ming,³⁷ C. Mishra,¹⁴¹ S. Mitra,¹⁹ V. P. Mitrofanov,⁶⁰ G. Mitselmakher,⁵ R. Mittleman,¹⁵ D. Moffa,⁸³
 A. Moggi,²⁴ K. Mogushi,¹¹ M. Mohan,³⁰ S. R. P. Mohapatra,¹⁵ M. Montani,^{120,121} C. J. Moore,¹³ D. Moraru,⁴⁶ G. Moreno,⁴⁶
 S. R. Morris,¹⁰¹ B. Mours,⁸ C. M. Mow-Lowry,⁵⁷ G. Mueller,⁵ A. W. Muir,³⁵ Arunava Mukherjee,¹⁰ D. Mukherjee,²¹
 S. Mukherjee,¹⁰¹ N. Mukund,¹⁹ A. Mullavey,⁷ J. Munch,⁷¹ E. A. Muñoz,⁴³ M. Muratore,³⁶ P. G. Murray,⁴⁵ K. Napier,⁷⁵
 I. Nardecchia,^{31,32} L. Naticchioni,^{95,34} R. K. Nayak,¹⁴² J. Neilson,¹⁰⁷ G. Nelemans,^{64,14} T. J. N. Nelson,⁷ M. Nery,¹⁰
 A. Neunzert,¹¹⁷ L. Nevin,¹ J. M. Newport,¹²³ G. Newton,^{45,†} K. K. Y. Ng,⁹¹ T. T. Nguyen,²⁵ D. Nichols,⁶⁴ A. B. Nielsen,¹⁰
 S. Nissanke,^{64,14} A. Nitz,¹⁰ A. Noack,¹⁰ F. Nocera,³⁰ D. Nolting,⁷ C. North,³⁵ L. K. Nuttall,³⁵ J. Oberling,⁴⁶ G. D. O'Dea,¹⁰⁷
 G. H. Ogin,¹⁴³ J. J. Oh,¹³⁰ S. H. Oh,¹³⁰ F. Ohme,¹⁰ M. A. Okada,¹⁶ M. Oliver,¹⁰⁰ P. Oppermann,¹⁰ Richard J. Oram,⁷
 B. O'Reilly,⁷ R. Ormiston,⁴⁴ L. F. Ortega,⁵ R. O'Shaughnessy,⁵⁶ S. Ossokine,³⁷ D. J. Ottaway,⁷¹ H. Overmier,⁷ B. J. Owen,⁸²
 A. E. Pace,⁶² J. Page,¹³⁶ M. A. Page,⁶³ A. Pai,^{115,144} S. A. Pai,⁵⁹ J. R. Palamos,⁶⁸ O. Palashov,¹²⁷ C. Palomba,³⁴
 A. Pal-Singh,³³ Howard Pan,⁸⁶ Huang-Wei Pan,⁸⁶ B. Pang,⁴⁷ P. T. H. Pang,⁹¹ C. Pankow,⁸⁸ F. Pannarale,³⁵ B. C. Pant,⁵⁹
 F. Paoletti,²⁴ A. Paoli,³⁰ M. A. Papa,^{37,21,10} A. Parida,¹⁹ W. Parker,⁷ D. Pascucci,⁴⁵ A. Pasqualetti,³⁰ R. Passaquieti,^{23,24}
 D. Passuello,²⁴ M. Patil,¹³² B. Patricelli,^{145,24} B. L. Pearlstone,⁴⁵ M. Pedraza,¹ R. Pedurand,^{26,146} L. Pekowsky,⁴³ A. Pele,⁷
 S. Penn,¹⁴⁷ C. J. Perez,⁴⁶ A. Perreca,^{1,108,93} L. M. Perri,⁸⁸ H. P. Pfeiffer,^{111,37} M. Phelps,⁴⁵ O. J. Piccinni,^{95,34} M. Pichot,⁶⁵
 F. Piergiovanni,^{120,121} V. Pierro,⁹ G. Pillant,³⁰ L. Pinard,²⁶ I. M. Pinto,⁹ M. Pirello,⁴⁶ M. Pitkin,⁴⁵ M. Poe,²¹ R. Poggiani,^{23,24}
 P. Popolizio,³⁰ E. K. Porter,³⁸ A. Post,¹⁰ J. Powell,¹⁴⁸ J. Prasad,¹⁹ J. W. W. Pratt,³⁶ G. Pratten,¹⁰⁰ V. Predoi,³⁵ T. Prestegard,²¹
 M. Prijatelj,¹⁰ M. Principe,⁹ S. Privitera,³⁷ G. A. Prodi,^{108,93} L. G. Prokhorov,⁶⁰ O. Puncken,¹⁰ M. Punturo,⁴² P. Puppó,³⁴

M. Pürrer,³⁷ H. Qi,²¹ V. Quetschke,¹⁰¹ E. A. Quintero,¹ R. Quitzow-James,⁶⁸ F. J. Raab,⁴⁶ D. S. Rabeling,²⁵ H. Radkins,⁴⁶ P. Raffai,⁵⁴ S. Raja,⁵⁹ C. Rajan,⁵⁹ B. Rajbhandari,⁸² M. Rakhmanov,¹⁰¹ K. E. Ramirez,¹⁰¹ A. Ramos-Buades,¹⁰⁰ P. Rapagnani,^{95,34} V. Raymond,³⁷ M. Razzano,^{23,24} J. Read,²⁹ T. Regimbau,⁶⁵ L. Rei,⁵⁸ S. Reid,⁶¹ D. H. Reitze,^{1,5} W. Ren,¹² S. D. Reyes,⁴³ F. Ricci,^{95,34} P. M. Ricker,¹² S. Rieger,¹⁰ K. Riles,¹¹⁷ M. Rizzo,⁵⁶ N. A. Robertson,^{1,45} R. Robie,⁴⁵ F. Robinet,²⁸ A. Rocchi,³² L. Rolland,⁸ J. G. Rollins,¹ V. J. Roma,⁶⁸ J. D. Romano,¹⁰¹ R. Romano,^{3,4} C. L. Romel,⁴⁶ J. H. Romie,⁷ D. Rosińska,^{149,55} M. P. Ross,¹⁵⁰ S. Rowan,⁴⁵ A. Rüdiger,¹⁰ P. Ruggi,³⁰ G. Rutins,²⁷ K. Ryan,⁴⁶ S. Sachdev,¹ T. Sadecki,⁴⁶ L. Sadeghian,²¹ M. Sakellariadou,¹⁵¹ L. Salconi,³⁰ M. Saleem,¹¹⁵ F. Salemi,¹⁰ A. Samajdar,¹⁴² L. Sammut,⁶ L. M. Sampson,⁸⁸ E. J. Sanchez,¹ L. E. Sanchez,¹ N. Sanchis-Gual,⁸⁴ V. Sandberg,⁴⁶ J. R. Sanders,⁴³ B. Sassolas,²⁶ P. R. Saulson,⁴³ O. Sauter,¹¹⁷ R. L. Savage,⁴⁶ A. Sawadsky,³³ P. Schale,⁶⁸ M. Scheel,⁴⁷ J. Scheuer,⁸⁸ J. Schmidt,¹⁰ P. Schmidt,^{1,64} R. Schnabel,³³ R. M. S. Schofield,⁶⁸ A. Schönbeck,³³ E. Schreiber,¹⁰ D. Schuette,^{10,22} B. W. Schulte,¹⁰ B. F. Schutz,^{35,10} S. G. Schwalbe,³⁶ J. Scott,⁴⁵ S. M. Scott,²⁵ E. Seidel,¹² D. Sellers,⁷ A. S. Sengupta,¹⁵² D. Sentenac,³⁰ V. Sequino,^{31,32,17} A. Sergeev,¹²⁷ D. A. Shaddock,²⁵ T. J. Shaffer,⁴⁶ A. A. Shah,¹³⁶ M. S. Shahriar,⁸⁸ M. B. Shaner,¹⁰⁷ L. Shao,³⁷ B. Shapiro,⁵⁰ P. Shawhan,⁷⁴ A. Sheperd,²¹ D. H. Shoemaker,¹⁵ D. M. Shoemaker,⁷⁵ K. Siellez,⁷⁵ X. Siemens,²¹ M. Sieniawska,⁵⁵ D. Sigg,⁴⁶ A. D. Silva,¹⁶ L. P. Singer,⁷⁸ A. Singh,^{37,10,22} A. Singhal,^{17,34} A. M. Sintes,¹⁰⁰ B. J. J. Slagmolen,²⁵ B. Smith,⁷ J. R. Smith,²⁹ R. J. E. Smith,^{1,6} S. Somala,¹⁵³ E. J. Son,¹³⁰ J. A. Sonnenberg,²¹ B. Sorazu,⁴⁵ F. Sorrentino,⁵⁸ T. Souradeep,¹⁹ A. P. Spencer,⁴⁵ A. K. Srivastava,¹⁰³ K. Staats,³⁶ A. Staley,⁴⁹ M. Steinke,¹⁰ J. Steinlechner,^{33,45} S. Steinlechner,³³ D. Steinmeyer,¹⁰ S. P. Stevenson,^{57,148} R. Stone,¹⁰¹ D. J. Stops,⁵⁷ K. A. Strain,⁴⁵ G. Stratta,^{120,121} S. E. Strigin,⁶⁰ A. Strunk,⁴⁶ R. Sturani,¹⁵⁴ A. L. Stuver,⁷ T. Z. Summerscales,¹⁵⁵ L. Sun,⁹⁴ S. Sunil,¹⁰³ J. Suresh,¹⁹ P. J. Sutton,³⁵ B. L. Swinkels,³⁰ M. J. Szczepańczyk,³⁶ M. Tacca,¹⁴ S. C. Tait,⁴⁵ C. Talbot,⁶ D. Talukder,⁶⁸ D. B. Tanner,⁵ D. Tao,⁷⁰ M. Tápai,¹¹⁶ A. Taracchini,³⁷ J. D. Tasson,⁷⁰ J. A. Taylor,¹³⁶ R. Taylor,¹ S. V. Tewari,¹⁴⁷ T. Theeg,¹⁰ F. Thies,¹⁰ E. G. Thomas,⁵⁷ M. Thomas,⁷ P. Thomas,⁴⁶ K. A. Thorne,⁷ E. Thrane,⁶ S. Tiwari,^{17,93} V. Tiwari,³⁵ K. V. Tokmakov,⁶¹ K. Toland,⁴⁵ M. Tonelli,^{23,24} Z. Tornasi,⁴⁵ A. Torres-Forné,⁸⁴ C. I. Torrie,¹ D. Töyrä,⁵⁷ F. Travasso,^{30,42} G. Traylor,⁷ J. Trinastic,⁵ M. C. Tringali,^{108,93} L. Trozzo,^{156,24} K. W. Tsang,¹⁴ M. Tse,¹⁵ R. Tso,¹ L. Tsukada,⁸⁰ D. Tsuna,⁸⁰ D. Tuyenbayev,¹⁰¹ K. Ueno,²¹ D. Ugolini,¹⁵⁷ C. S. Unnikrishnan,¹¹⁸ A. L. Urban,¹ S. A. Usman,³⁵ H. Vahlbruch,²² G. Vajente,¹ G. Valdes,² N. van Bakel,¹⁴ M. van Beuzekom,¹⁴ J. F. J. van den Brand,^{73,14} C. Van Den Broeck,^{14,158} D. C. Vander-Hyde,⁴³ L. van der Schaaf,¹⁴ J. V. van Heijningen,¹⁴ A. A. van Veggel,⁴⁵ M. Vardaro,^{52,53} V. Varma,⁴⁷ S. Vass,¹ M. Vasúth,⁴⁸ A. Vecchio,⁵⁷ G. Vedovato,⁵³ J. Veitch,⁴⁵ P. J. Veitch,⁷¹ K. Venkateswara,¹⁵⁰ G. Venugopalan,¹ D. Verkindt,⁸ F. Vetrano,^{120,121} A. Viceré,^{120,121} A. D. Viets,²¹ S. Vinciguerra,⁵⁷ D. J. Vine,²⁷ J.-Y. Vinet,⁶⁵ S. Vitale,¹⁵ T. Vo,⁴³ H. Vocca,^{41,42} C. Vorvick,⁴⁶ S. P. Vyatchanin,⁶⁰ A. R. Wade,¹ L. E. Wade,⁸³ M. Wade,⁸³ R. Walet,¹⁴ M. Walker,²⁹ L. Wallace,¹ S. Walsh,^{37,10,21} G. Wang,^{17,121} H. Wang,⁵⁷ J. Z. Wang,⁶² W. H. Wang,¹⁰¹ Y. F. Wang,⁹¹ R. L. Ward,²⁵ J. Warner,⁴⁶ M. Was,⁸ J. Watchi,⁹⁶ B. Weaver,⁴⁶ L.-W. Wei,^{10,22} M. Weinert,¹⁰ A. J. Weinstein,¹ R. Weiss,¹⁵ L. Wen,⁶³ E. K. Wessel,¹² P. Weßels,¹⁰ J. Westerweck,¹⁰ T. Westphal,¹⁰ K. Wette,²⁵ J. T. Whelan,⁵⁶ B. F. Whiting,⁵ C. Whittle,⁶ D. Wilken,¹⁰ D. Williams,⁴⁵ R. D. Williams,¹ A. R. Williamson,⁶⁴ J. L. Willis,^{1,159} B. Willke,^{22,10} M. H. Wimmer,¹⁰ W. Winkler,¹⁰ C. C. Wipf,¹ H. Wittel,^{10,22} G. Woan,⁴⁵ J. Woehler,¹⁰ J. Wofford,⁵⁶ K. W. K. Wong,⁹¹ J. Worden,⁴⁶ J. L. Wright,⁴⁵ D. S. Wu,¹⁰ D. M. Wysocki,⁵⁶ S. Xiao,¹ H. Yamamoto,¹ C. C. Yancey,⁷⁴ L. Yang,¹⁶⁰ M. J. Yap,²⁵ M. Yazback,⁵ Hang Yu,¹⁵ Haocun Yu,¹⁵ M. Yvert,⁸ A. Zadrożny,¹³¹ M. Zanolin,³⁶ T. Zelenova,³⁰ J.-P. Zendri,⁵³ M. Zevin,⁸⁸ L. Zhang,¹ M. Zhang,¹³⁹ T. Zhang,⁴⁵ Y.-H. Zhang,⁵⁶ C. Zhao,⁶³ M. Zhou,⁸⁸ Z. Zhou,⁸⁸ S. J. Zhu,^{37,10} X. J. Zhu,⁶ M. E. Zucker,^{1,15} and J. Zweizig¹

(LIGO Scientific Collaboration and Virgo Collaboration)

¹LIGO, California Institute of Technology, Pasadena, California 91125, USA

²Louisiana State University, Baton Rouge, Louisiana 70803, USA

³Università di Salerno, Fisciano, I-84084 Salerno, Italy

⁴INFN, Sezione di Napoli, Complesso Universitario di Monte S. Angelo, I-80126 Napoli, Italy

⁵University of Florida, Gainesville, Florida 32611, USA

⁶OzGrav, School of Physics & Astronomy, Monash University, Clayton 3800, Victoria, Australia

⁷LIGO Livingston Observatory, Livingston, Louisiana 70754, USA

⁸Laboratoire d'Annecy-le-Vieux de Physique des Particules (LAPP), Université Savoie Mont Blanc, CNRS/IN2P3, F-74941 Annecy, France

- ⁹University of Sannio at Benevento, I-82100 Benevento, Italy and INFN, Sezione di Napoli, I-80100 Napoli, Italy
- ¹⁰Max Planck Institute for Gravitational Physics (Albert Einstein Institute), D-30167 Hannover, Germany
- ¹¹The University of Mississippi, University, Mississippi 38677, USA
- ¹²NCSA, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA
- ¹³University of Cambridge, Cambridge CB2 1TN, United Kingdom
- ¹⁴Nikhef, Science Park, 1098 XG Amsterdam, Netherlands
- ¹⁵LIGO, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA
- ¹⁶Instituto Nacional de Pesquisas Espaciais, 12227-010 São José dos Campos, São Paulo, Brazil
- ¹⁷Gran Sasso Science Institute (GSSI), I-67100 L'Aquila, Italy
- ¹⁸INFN, Laboratori Nazionali del Gran Sasso, I-67100 Assergi, Italy
- ¹⁹Inter-University Centre for Astronomy and Astrophysics, Pune, Maharashtra 411007, India
- ²⁰International Centre for Theoretical Sciences, Tata Institute of Fundamental Research, Bengaluru, Karnataka 560089, India
- ²¹University of Wisconsin-Milwaukee, Milwaukee, Wisconsin 53201, USA
- ²²Leibniz Universität Hannover, D-30167 Hannover, Germany
- ²³Università di Pisa, I-56127 Pisa, Italy
- ²⁴INFN, Sezione di Pisa, I-56127 Pisa, Italy
- ²⁵OzGrav, Australian National University, Canberra, Australian Capital Territory 0200, Australia
- ²⁶Laboratoire des Matériaux Avancés (LMA), CNRS/IN2P3, F-69622 Villeurbanne, France
- ²⁷SUPA, University of the West of Scotland, Paisley PA1 2BE, United Kingdom
- ²⁸LAL, Université Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, F-91898 Orsay, France
- ²⁹California State University Fullerton, Fullerton, California 92831, USA
- ³⁰European Gravitational Observatory (EGO), I-56021 Cascina, Pisa, Italy
- ³¹Università di Roma Tor Vergata, I-00133 Roma, Italy
- ³²INFN, Sezione di Roma Tor Vergata, I-00133 Roma, Italy
- ³³Universität Hamburg, D-22761 Hamburg, Germany
- ³⁴INFN, Sezione di Roma, I-00185 Roma, Italy
- ³⁵Cardiff University, Cardiff CF24 3AA, United Kingdom
- ³⁶Embry-Riddle Aeronautical University, Prescott, Arizona 86301, USA
- ³⁷Max Planck Institute for Gravitational Physics (Albert Einstein Institute), D-14476 Potsdam-Golm, Germany
- ³⁸APC, AstroParticule et Cosmologie, Université Paris Diderot, CNRS/IN2P3, CEA/Irfu, Observatoire de Paris, Sorbonne Paris Cité, F-75205 Paris Cedex 13, France
- ³⁹Korea Institute of Science and Technology Information, Daejeon 34141, Korea
- ⁴⁰West Virginia University, Morgantown, West Virginia 26506, USA
- ⁴¹Università di Perugia, I-06123 Perugia, Italy
- ⁴²INFN, Sezione di Perugia, I-06123 Perugia, Italy
- ⁴³Syracuse University, Syracuse, New York 13244, USA
- ⁴⁴University of Minnesota, Minneapolis, Minnesota 55455, USA
- ⁴⁵SUPA, University of Glasgow, Glasgow G12 8QQ, United Kingdom
- ⁴⁶LIGO Hanford Observatory, Richland, Washington 99352, USA
- ⁴⁷Caltech CaRT, Pasadena, California 91125, USA
- ⁴⁸Wigner RCP, RMKI, H-1121 Budapest, Konkoly Thege Miklós út 29-33, Hungary
- ⁴⁹Columbia University, New York, New York 10027, USA
- ⁵⁰Stanford University, Stanford, California 94305, USA
- ⁵¹Università di Camerino, Dipartimento di Fisica, I-62032 Camerino, Italy
- ⁵²Università di Padova, Dipartimento di Fisica e Astronomia, I-35131 Padova, Italy
- ⁵³INFN, Sezione di Padova, I-35131 Padova, Italy
- ⁵⁴Institute of Physics, Eötvös University, Pázmány P. s. 1/A, Budapest 1117, Hungary
- ⁵⁵Nicolaus Copernicus Astronomical Center, Polish Academy of Sciences, 00-716 Warsaw, Poland
- ⁵⁶Rochester Institute of Technology, Rochester, New York 14623, USA
- ⁵⁷University of Birmingham, Birmingham B15 2TT, United Kingdom
- ⁵⁸INFN, Sezione di Genova, I-16146 Genova, Italy
- ⁵⁹RRCAT, Indore Madhya Pradesh 452013, India
- ⁶⁰Faculty of Physics, Lomonosov Moscow State University, Moscow 119991, Russia
- ⁶¹SUPA, University of Strathclyde, Glasgow G1 1XQ, United Kingdom
- ⁶²The Pennsylvania State University, University Park, Pennsylvania 16802, USA
- ⁶³OzGrav, University of Western Australia, Crawley, Western Australia 6009, Australia
- ⁶⁴Department of Astrophysics/IMAPP, Radboud University Nijmegen, P.O. Box 9010, 6500 GL Nijmegen, Netherlands
- ⁶⁵Artemis, Université Côte d'Azur, Observatoire Côte d'Azur, CNRS, CS 34229, F-06304 Nice Cedex 4, France
- ⁶⁶Institut FOTON, CNRS, Université de Rennes 1, F-35042 Rennes, France
- ⁶⁷Washington State University, Pullman, Washington 99164, USA

- ⁶⁸University of Oregon, Eugene, Oregon 97403, USA
- ⁶⁹Laboratoire Kastler Brossel, UPMC-Sorbonne Universités, CNRS, ENS-PSL Research University, Collège de France, F-75005 Paris, France
- ⁷⁰Carleton College, Northfield, Minnesota 55057, USA
- ⁷¹OzGrav, University of Adelaide, Adelaide, South Australia 5005, Australia
- ⁷²Astronomical Observatory Warsaw University, 00-478 Warsaw, Poland
- ⁷³VU University Amsterdam, 1081 HV Amsterdam, Netherlands
- ⁷⁴University of Maryland, College Park, Maryland 20742, USA
- ⁷⁵School of Physics, Georgia Institute of Technology, Atlanta, Georgia 30332, USA
- ⁷⁶Université Claude Bernard Lyon 1, F-69622 Villeurbanne, France
- ⁷⁷Università di Napoli 'Federico II,' Complesso Universitario di Monte S. Angelo, I-80126 Napoli, Italy
- ⁷⁸NASA Goddard Space Flight Center, Greenbelt, Maryland 20771, USA
- ⁷⁹Dipartimento di Fisica, Università degli Studi di Genova, I-16146 Genova, Italy
- ⁸⁰RESCEU, University of Tokyo, Tokyo, 113-0033, Japan
- ⁸¹Tsinghua University, Beijing 100084, China
- ⁸²Texas Tech University, Lubbock, Texas 79409, USA
- ⁸³Kenyon College, Gambier, Ohio 43022, USA
- ⁸⁴Departamento de Astronomía y Astrofísica, Universitat de València, E-46100 Burjassot, València, Spain
- ⁸⁵Museo Storico della Fisica e Centro Studi e Ricerche Enrico Fermi, I-00184 Roma, Italy
- ⁸⁶National Tsing Hua University, Hsinchu City, 30013 Taiwan, Republic of China
- ⁸⁷Charles Sturt University, Wagga Wagga, New South Wales 2678, Australia
- ⁸⁸Center for Interdisciplinary Exploration & Research in Astrophysics (CIERA), Northwestern University, Evanston, Illinois 60208, USA
- ⁸⁹University of Chicago, Chicago, Illinois 60637, USA
- ⁹⁰Pusan National University, Busan 46241, Korea
- ⁹¹The Chinese University of Hong Kong, Shatin, NT, Hong Kong
- ⁹²INAF, Osservatorio Astronomico di Padova, I-35122 Padova, Italy
- ⁹³INFN, Trento Institute for Fundamental Physics and Applications, I-38123 Povo, Trento, Italy
- ⁹⁴OzGrav, University of Melbourne, Parkville, Victoria 3010, Australia
- ⁹⁵Università di Roma 'La Sapienza,' I-00185 Roma, Italy
- ⁹⁶Université Libre de Bruxelles, Brussels 1050, Belgium
- ⁹⁷Sonoma State University, Rohnert Park, California 94928, USA
- ⁹⁸Departamento de Matemáticas, Universitat de València, E-46100 Burjassot, València, Spain
- ⁹⁹Montana State University, Bozeman, Montana 59717, USA
- ¹⁰⁰Universitat de les Illes Balears, IAC3—IEEC, E-07122 Palma de Mallorca, Spain
- ¹⁰¹The University of Texas Rio Grande Valley, Brownsville, Texas 78520, USA
- ¹⁰²Bellevue College, Bellevue, Washington 98007, USA
- ¹⁰³Institute for Plasma Research, Bhat, Gandhinagar, Gujarat 382428, India
- ¹⁰⁴The University of Sheffield, Sheffield S10 2TN, United Kingdom
- ¹⁰⁵Dipartimento di Scienze Matematiche, Fisiche e Informatiche, Università di Parma, I-43124 Parma, Italy
- ¹⁰⁶INFN, Sezione di Milano Bicocca, Gruppo Collegato di Parma, I-43124 Parma, Italy
- ¹⁰⁷California State University, Los Angeles, 5151 State University Dr, Los Angeles, California 90032, USA
- ¹⁰⁸Università di Trento, Dipartimento di Fisica, I-38123 Povo, Trento, Italy
- ¹⁰⁹Montclair State University, Montclair, New Jersey 07043, USA
- ¹¹⁰National Astronomical Observatory of Japan, 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan
- ¹¹¹Canadian Institute for Theoretical Astrophysics, University of Toronto, Toronto, Ontario M5S 3H8, Canada
- ¹¹²Observatori Astronòmic, Universitat de València, E-46980 Paterna, València, Spain
- ¹¹³School of Mathematics, University of Edinburgh, Edinburgh EH9 3FD, United Kingdom
- ¹¹⁴University and Institute of Advanced Research, Koba Institutional Area, Gandhinagar Gujarat 382007, India
- ¹¹⁵IISER-TVM, CET Campus, Trivandrum Kerala 695016, India
- ¹¹⁶University of Szeged, Dóm tér 9, Szeged 6720, Hungary
- ¹¹⁷University of Michigan, Ann Arbor, Michigan 48109, USA
- ¹¹⁸Tata Institute of Fundamental Research, Mumbai, Maharashtra 400005, India
- ¹¹⁹INAF, Osservatorio Astronomico di Capodimonte, I-80131, Napoli, Italy
- ¹²⁰Università degli Studi di Urbino "Carlo Bo," I-61029 Urbino, Italy
- ¹²¹INFN, Sezione di Firenze, I-50019 Sesto Fiorentino, Firenze, Italy
- ¹²²Physik-Institut, University of Zurich, Winterthurerstrasse 190, 8057 Zurich, Switzerland
- ¹²³American University, Washington, D.C. 20016, USA
- ¹²⁴University of Białystok, 15-424 Białystok, Poland
- ¹²⁵University of Southampton, Southampton SO17 1BJ, United Kingdom

- ¹²⁶*University of Washington Bothell, 18115 Campus Way NE, Bothell, Washington 98011, USA*
¹²⁷*Institute of Applied Physics, Nizhny Novgorod 603950, Russia*
¹²⁸*Korea Astronomy and Space Science Institute, Daejeon 34055, Korea*
¹²⁹*Inje University Gimhae, South Gyeongsang 50834, Korea*
¹³⁰*National Institute for Mathematical Sciences, Daejeon 34047, Korea*
¹³¹*NCBJ, 05-400 Świerk-Otwock, Poland*
¹³²*Institute of Mathematics, Polish Academy of Sciences, 00656 Warsaw, Poland*
¹³³*Hillsdale College, Hillsdale, Michigan 49242, USA*
¹³⁴*Hanyang University, Seoul 04763, Korea*
¹³⁵*Seoul National University, Seoul 08826, Korea*
¹³⁶*NASA Marshall Space Flight Center, Huntsville, Alabama 35811, USA*
¹³⁷*ESPCI, CNRS, F-75005 Paris, France*
¹³⁸*Southern University and A&M College, Baton Rouge, Louisiana 70813, USA*
¹³⁹*College of William and Mary, Williamsburg, Virginia 23187, USA*
¹⁴⁰*Centre Scientifique de Monaco, 8 quai Antoine 1er MC-98000, Monaco*
¹⁴¹*Indian Institute of Technology Madras, Chennai, Tamil Nadu 600036, India*
¹⁴²*IISER-Kolkata, Mohanpur, West Bengal 741252, India*
¹⁴³*Whitman College, 345 Boyer Avenue, Walla Walla, Washington 99362 USA*
¹⁴⁴*Indian Institute of Technology Bombay, Powai, Mumbai, Maharashtra 400076, India*
¹⁴⁵*Scuola Normale Superiore, Piazza dei Cavalieri 7, I-56126 Pisa, Italy*
¹⁴⁶*Université de Lyon, F-69361 Lyon, France*
¹⁴⁷*Hobart and William Smith Colleges, Geneva, New York 14456, USA*
¹⁴⁸*OzGrav, Swinburne University of Technology, Hawthorn VIC 3122, Australia*
¹⁴⁹*Janusz Gil Institute of Astronomy, University of Zielona Góra, 65-265 Zielona Góra, Poland*
¹⁵⁰*University of Washington, Seattle, Washington 98195, USA*
¹⁵¹*King's College London, University of London, London WC2R 2LS, United Kingdom*
¹⁵²*Indian Institute of Technology, Gandhinagar Ahmedabad Gujarat 382424, India*
¹⁵³*Indian Institute of Technology Hyderabad, Sangareddy, Khandi, Telangana 502285, India*
¹⁵⁴*International Institute of Physics, Universidade Federal do Rio Grande do Norte, Natal, Rio Grande do Norte 59078-970, Brazil*
¹⁵⁵*Andrews University, Berrien Springs, Michigan 49104, USA*
¹⁵⁶*Università di Siena, I-53100 Siena, Italy*
¹⁵⁷*Trinity University, San Antonio, Texas 78212, USA*
¹⁵⁸*Van Swinderen Institute for Particle Physics and Gravity, University of Groningen, Nijenborgh 4, 9747 AG Groningen, Netherlands*
¹⁵⁹*Abilene Christian University, Abilene, Texas 79699, USA*
¹⁶⁰*Colorado State University, Fort Collins, Colorado 80523, USA*

[†]Deceased.