Scholars' Mine

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Path planning for general mazes

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PATH PLANNING FOR

GENERAL MAZES

by

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A THESIS

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ABSTRACT

Path planning is used in, but not limited to robotics, telemetry, aerospace, and medical applications. The goal of the path planning is to identify a route from an origination point to a destination point while avoiding obstacles. This path might not always be the shortest in distance as time, terrain, speed limits, and many other factors can affect the optimality of the path. However, in this thesis, the length, computational time, and the smoothness of the path are the only constraints that will be considered with the length of the path being the most important. There are a variety of algorithms that can be used for path planning but Ant Colony Optimization (ACO), Neural Network, and A* will be the only algorithms explored in this thesis.

The problem of solving general mazes has been greatly researched, but the contributions of this thesis extended Ant Colony Optimization to path planning for mazes, created a new landscape for the Neural Network to use, and added a bird's eye view to the A* Algorithm. The Ant Colony Optimization that was used in this thesis was able to discover a path to the goal, but it was jagged and required a larger computational time compared to the Neural Network and A* algorithm discussed in this thesis. The Hopfield-type neural network used in this thesis propagated energy to create a landscape and used gradient decent to find the shortest path in terms of distance, but this thesis modified how the landscape was created to prevent the neural network from getting trapped in local minimas. The last contribution was applying a bird's eye view to the A* algorithm to learn more about the environment which helped to create shorter and smoother paths.

ACKNOWLEDGMENTS

TABLE OF CONTENTS

LIST OF ILLUSTRATIONS

LIST OF TABLES

1. INTRODUCTION

There are various searching techniques, algorithms, and path planning problems such as Hybrid Binary Particle Swarm Optimization (HBPSO) algorithm for a Multi-vehicle Search Area coverage problem [1], Differential Evolution Particle Swarm Optimization (DEPSO) algorithm for clustering [2], and Adaptive Critic Design for the generalized maze problem [3-4]. This thesis will focus only on the generalized maze problem using Ant Colony Optimization (ACO), Neural Networks (NN), and A* (pronounced A-Star) algorithms.

Ant Colony Optimization (ACO) [5-13] was the first algorithm considered for this thesis. There are many different versions of ACO which have been used for problems such as routing, assignment, scheduling, subset, and others [5, 9]. Most of the problems ACO is used for are NP-hard problems [5, 9] and most notably the traveling salesman problem (TSP) [5, 9-11]. This thesis expanded ACO to path planning for mazes. Since the goal of the TSP is to be able to find the shortest path by traveling to each city once and returning to the starting city, finding the shortest path through a maze should be similar.

It is important to note that typically ACO is applied to small scale TSP not necessarily to make strides in solving the TSP problem but more so to be used as a benchmark to show how that version of ACO can be used as an optimization tool and possibly how it compares to other algorithms [5, 9-11]. Using TSP as a benchmark is not limited to ACO or even to small scale TSP problems, Mulder and Wunsch [14] not only compare multiple algorithms but compare how they scale by using large scale TSP

problems (1000+ cities). It is also important to note that TSP problems, especially large

scale TSP problems, are approached by heuristic methods [14-17]. The heuristic uses

special knowledge about the problem and incorporates it to help simplify the problem or

allows certain assumptions to be made which in turn helps to solve the problem quicker.

Since this is usually an estimate, the result might not always be optimal but should return

a close to optimal solution as long as the heuristic was chosen appropriately. This can

most be seen by the algorithms discussed in this paper especially in Section 7.2 where

Dijkstra's algorithm, which doesn't have a heuristic [18-20], is compared to A*, which is

the same algorithm but with a heuristic [18-22].

The ability of the algorithm to learn over time by using the collective swarm

knowledge of how the ants have explored previously and its ability to be used for real-

time environments, as opposed to needing a simulated model of the environment, made

this algorithm desirable. Using a simulated model of the environment to plan a path

might not be possible for unknown environments or environments that are constantly

changing. Since the path created depended on a stochastic process of the algorithm, the

randomization caused the path to be very jagged. The quality of the path and the

computational time in creating the path were also affected by what the parameters for

ACO were set to. This is covered in more detail in Section 3.1. One method that might

have improved the performance would have been to make the ants stubborn [12, 13].

A new neural network method for path planning created by Zhong et al. [23] was

the next algorithm to be employed. Unlike ACO, this algorithm could be used in

environments that change with the respect to time, had a much smaller computational

time, and did not rely on parameters or randomization. For the environments studied in

this thesis, the algorithm tended to become stuck in local minima. Section 5.1 describes a way to improve the algorithm to avoid this problem. While the algorithm was superior to ACO for the problems investigated, it generated paths that had zero radius or sharp turns. It was not immediately obvious how one would modify the neural network algorithm to favor smoother paths, which motivated us to explore other algorithms. Instead of looking at other algorithms, further research into biasing neural networks to avoid obstacles might have yielded better results [24].

A* [18-22] was studied in Section 6 and 7 of this thesis because of its known performance and popularity as a path planning algorithm. A* finds an optimal path in terms of distance but is generally not used for real-time environments since the environment needs to be static, or unchanging. The A* algorithm was improved by using a "bird's eye view". This allowed the algorithm to generate smoother paths, which could possibly allow the robot to traverse the paths faster, and avoids the need to have as many sharp turns. For environments that are constantly changing, a modified version of A* called LRTA* can be used [25].

The environments for each algorithm were all modeled using discrete space by creating an evenly spaced binary matrix where nodes that contained a value of one were considered travelable and nodes with a zero represented an obstacle. This method was chosen for simplicity. Since the nodes were discretely spaced instead of being continuous, the paths were not as good as they could have been. Some of the issues with these paths include traveling too close to obstacles, creating 90 degree angles with small turning radius, and producing a jagged path.

Traveling too close to obstacles could cause the mobile robot to hit an obstacle or could lead to having to make sharper turns. Having sharp turns or 90 degree angles with small turning radius could cause longer traveling time or could generate turns that are not feasibly possible for the mobile robot. Jagged paths might slow down the robot and could be difficult to follow. Many of these algorithms are also based on the length of the path instead of the time required to travel the path. Therefore, creating or modifying an algorithm that could produce a path without these issues was desired. Having more nodes to represent the environment could have also helped with some of these problems and would have made the paths seem more continuous but increasing the number of nodes also increases the computational time since there will be more nodes that would have to be traveled through and more searching done by the algorithms.

All three algorithms (ACO, NN, and A*) will be covered respectively in sections 2-7. Each algorithm will be broken into two different sections, a literature review part and an implementation part. The literature review section will give a brief explanation of each algorithm. The implementation section will focus on modifications made by this thesis, issues discovered with the algorithm, and the results for the algorithm.

2. ACO LITERATURE REVIEW

Ant Colony Optimization simulates the behavior of biological ants. For path planning, this behavior is that of the foraging ants. Dorigo [5] developed this foraging behavior which he called the Ant System (AS). Foraging ants randomly explore in search for food. Once a food source is found, the ants deposit pheromone from the food back to the colony. This pheromone trail attracts other ants. Since only one pheromone deposit has been made, the pheromone level will be weak and will have limited attraction to other ants. This means that most ants will still randomly explore for food instead of following the initial ant's path.

Over time as ants lay pheromone across the paths, the pheromone levels will increase. Even though each ant's path is different, there is generally some overlapping for certain areas especially where the path is the best. Since multiple ants cross this section, pheromone is deposited at a much quicker rate. The areas with the largest amount of pheromone attract the most ants. This reduces the amount of exploration and causes the ants to exploit the pheromone paths. As time passes, pheromone slowly decays which weakens the attraction and if pheromone is not replenished, the path will disappear. This allows the longer, rarely traveled paths to be forgotten. Eventually the ants will converge on the shortest path.

3. ACO IMPLEMENTATION

3.1. PARAMETERS

In order to replicate the foraging behavior artificially, all of the parameters (population size, pheromone decay rate, pheromone weight, heuristic weight, and pheromone intensity) need to be optimized. However, since optimizing these parameters is a nonlinear multivariable problem, finding an optimized value is difficult. The methods typically used to optimize these parameters are with trial-and-error where the length and computational time is checked with each parameter modification or to use another optimizing algorithm. Both of these methods add to the computational time, and the values found for each parameter will have to constantly change as the environment changes. Trial-and-error was used in this thesis.

3.1.1. Population Size. Having a large population size gives a more thorough search but also increases computational time due to more searches being done. The larger the environment, the larger the population size will have to be to explore it.

3.1.2. Pheromone Decay. The pheromone decay rate determines the rate at which paths are forgotten. Having poor paths remain in the environment to be explored over and over again is a waste of computational time, however, if the decay rate is too fast, it might be possible to forget an optimal path due to the path not remaining long enough for ants to deposit enough pheromone to be biased to it.

3.1.3. Heuristic Weight. The heuristic weight is the bias to the goal based on the heuristic information. The heuristic information is the distant to the goal and is calculated using the Euclidean Distance Formula. If the value for the heuristic weight is

too low then there will be no feedback to the goal and the ants' paths will depend only on the pheromone quantity. If the heuristic weight is too high then there will be no exploration and will only be a greedy search. The ants might also get trapped.

3.1.4. Pheromone Weight. The pheromone weight represents how strongly the pheromone influences the ant's behavior. If it's too low then the searching will be based only on the heuristic information but if the heuristic weight is low too when the pheromone weight is low then the ants will randomly explore. When the pheromone weight is too high, there will be very little exploration. Instead, previous discovered paths will be exploited.

3.1.5. Pheromone Intensity. The amount of pheromone applied to each node is the pheromone intensity. The pheromone quantity of each node is stored in matrix. The pheromone intensity is the only parameter that has an equation to set it. All nodes need to start with an equal amount of pheromone. It should be equal so there is no initial bias. If the pheromone level is initialized too low the ants will converge too quickly and an optimal path will not be found. When the pheromone intensity is too high, there will be many wasted iterations waiting for the pheromone to evaporate enough for the ants' paths to be biased by the pheromone levels since the ants deposit only a small amount of pheromone. Pheromone intensity can be determined by the following equation which is still estimated:

$$\tau_0 = m/f^*$$

Where:

- τ_0 is the pheromone intensity

- m is the number of ants

- f^* is an estimation of the optimal value, or distance, of the shortest path for the function.

3.2. TOUR CONSTRUCTION

Ants use a probabilistic selection based on the quantity of the pheromone and the heuristic information to decide which node to travel to. The ACO literature [5-9] does not describe how these probabilities were applied so the probability mass function was used. In order to prevent the ants from traveling through a single node multiple times during a single trip, a revisiting prevention method was created.

Since obstacles have a pheromone value of zero to prevent being traveled to, a temporary pheromone matrix was created to set the pheromone level to zero for previously traveled to nodes. A temporary matrix is initialized as an exact copy of the actual pheromone values at the start of each ant's tour. A temporary matrix is used because the actual pheromone values still need to be used for future explorations. Each time an ant travels to a new node, the temporary pheromone value will be set to zero to prevent the ant from staying at that node or returning to it but this could cause the ant to be able to trap itself by being surrounded by nodes with a pheromone level of zero. Therefore, any time the current node and surrounding nodes are zero, the temporary pheromone matrix is re-initialized with the same values as the actual pheromone matrix. Since it is still possible to visit a node more than once in a tour, a check is done to see when the first and last time a repeated node is visited. All nodes in-between the first and last time are removed from the tour.

3.3. RESULTS

There are many different versions of ACO but only three of them were tested: Ant System (AS) [5, 9] Figure 3.1., Elitist Ant System (EAS) [5, 9] Figure 3.2., and Rank Based Ant System (ASrank) [5, 9] Figure 3.3. The computational time and paths change each time the algorithms are used. This can be seen from Figure 3.4. where Ant System is simulated five times. Do to these changes, the average and standard deviation for computational time and path lengths of each algorithm for five trials are recorded in Table 3.1. The parameters were optimized through trial-and-error for AS, and then, those same parameters were used for ASrank and EAS.
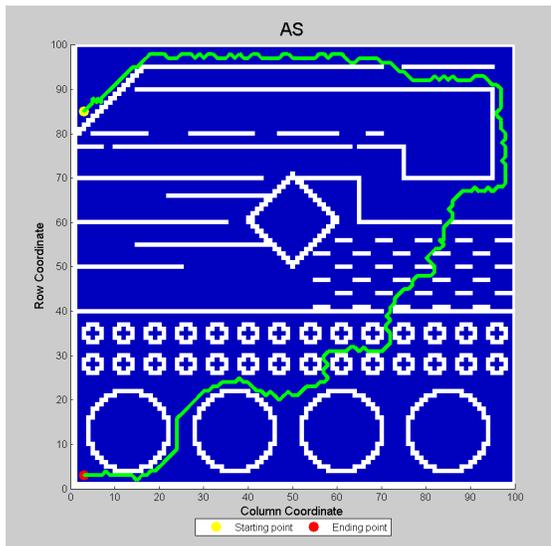

Figure 3.1. Ant System
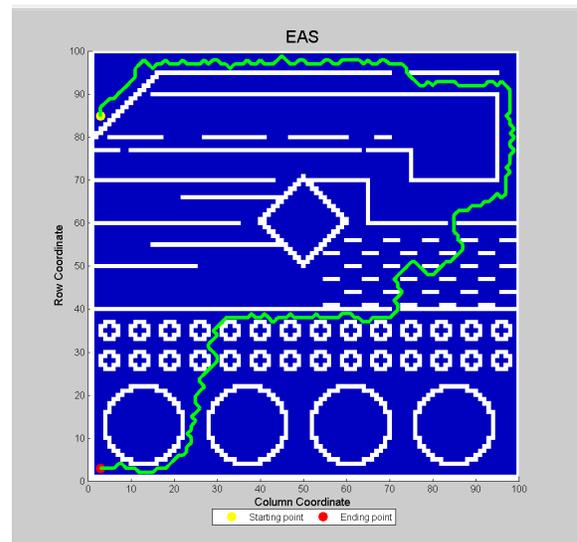
Figure 3.2. Elitist Ant System
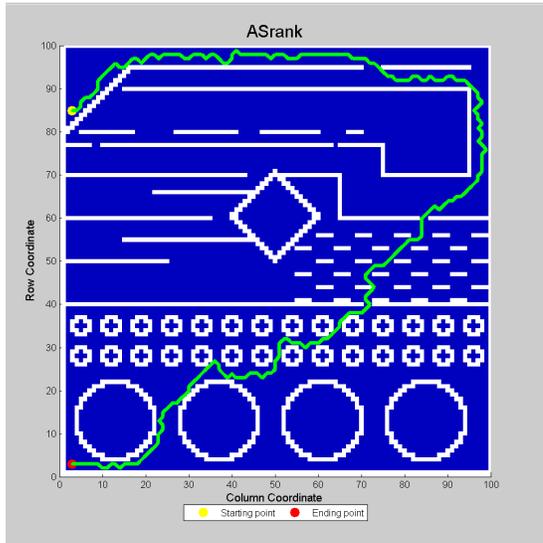
Figure 3.3. Rank Based Ant System
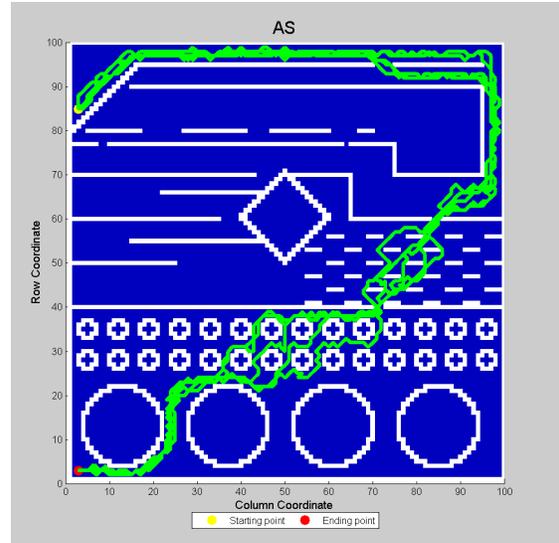
Figure 3.4. AS Simulated 5 Times

Table 3.1. ACO Simulated Five Times Result

Name	Average Computational Time	Standard Deviation of Time	Average Path Length	Standard Deviation of Path Length
Ant System	48 minutes 27.2134 seconds	7 minutes 40.5503 seconds	309.4074	5.2346
Elitist Ant System	48 minutes 26.4 seconds	3 minutes 53.0489 seconds	309.4476	10.8615
Rank Based Ant System	54 minutes 11.0868 seconds	5 minutes 28.6259 seconds	305.1532	6.1198

3.4. CONCLUSION

Upon implementation of the algorithm, it was discovered that, due to the randomization and needing to optimize the parameters, paths were jagged and were not optimal in terms of distance. The over-all path as far as which areas were best to travel through was optimal, but how it traveled through those areas was far from optimal. Most of the paths contained "zig-zags" instead of being a straight line. The ants use a

probabilistic selection based on the quantity of pheromone and the heuristic information when deciding which node to travel to which causes the randomization. This randomization is good for finding different paths but bad for being able to create an optimal path and causes the paths to not be smooth.

Even though the algorithm learned over time to improve its path, it would not work in a real-time environment where the environment constantly changes because of parameter changes and needing time to learn. It would work best in an environment where it could first be trained offline and then when a change in the environment occurred it would need to have time to learn the new environment. For each change, the parameters would need to be re-optimized, but I am unaware of a formula to optimize these parameters. Trial-and-error or another optimizing algorithm would have to be used instead which both methods would add to computational time. It took ACO on average over 48 minutes computationally to create the path not counting time spent for trial-and-error. It took the neural network and A* only seconds to solve the same maze and they were both able to find shorter paths than ACO. The time and paths might have been improved by making the ants stubborn. Stubborn ants can differentiate their own pheromone compared to other ants' pheromone and will be biased more to their own pheromone which helps to create diversity in the paths [12, 13].

4. NEURAL NETWORK LITERATURE REVIEW

Neural networks have successfully been applied to path planning by using neural networks to recognize patterns for a wall following algorithm [26], using spiking neural networks with dynamic memory for autonomous mobile robots [27], and using Hopfield neural networks for direction in a direction map [28]. A different collision-free path planning algorithm that uses a Hopfield-type neural network that does not need any previous knowledge of the search space or learning procedures was purposed by Zhong et al. [23]. This was accomplished by treating the target as an energy source. The energy was propagated in a square formation from the target to all of the connecting neurons which represent free spaces in the search space. The neurons not connected to other neurons represented obstacles and thus, were never given any energy. This energy was then used as a landscape in which the highest energy, the target, represented the peak of the landscape while the obstacles represented the lowest elevation of the landscape. By traveling up the steepest gradient from the starting point, an optimal or close to optimal path was found in terms of shortest distance. The main ways this paper differs from the paper purposed by Zhong et al. [23] was by creating a separate landscape instead of using the actual energy and by propagating in a cross fashion instead of a square formation.

5. NEURAL NETWORK IMPLEMENTATION

5.1. PROPAGATION

To propagate the energy, a matrix was created to store the amount of energy of each neuron in the search space. The target was then given an initial integer value of one while all other neurons were set to zero as shown in Figure 5.1.

	1	2	3	4	5	6
1	0	0	0	0	0	0
2	0	0	0	0	0	0
3	0	0	1	0	0	0
4	0	0	0	0	0	0
5	0	0	0	0	0	0
6	0	0	0	0	0	0
7	0	0	0	0	0	0
8	0	0	0	0	0	0

Figure 5.1. Initial Energy with Target at (3,3)

Another matrix was created which was used for the elevation. This matrix adds a one to any position within itself that has energy located at that position (Figure 5.2.).

	1	2	3	4	5	6
1	0	0	0	0	0	0
2	0	0	0	0	0	0
3	0	0	1	0	0	0
4	0	0	0	0	0	0
5	0	0	0	0	0	0
6	0	0	0	0	0	0
7	0	0	0	0	0	0
8	0	0	0	0	0	0

Figure 5.2. Elevation of Figure 5.1. at (3,3)

The energy matrix values were propagated by shifting the energy up one node, down one node, left one node, and to the right one node. These shifts were then added back into the original energy matrix after being multiplied by a weight. The weights for diagonal movements should have been given a value of 0.5 and all horizontal and vertical movements should have a weights of 1 [23], but since the energy was not used as the landscape, all weights were set to 1. A check was then done to see if any of these nodes with energy were unconnected neurons. If they were unconnected, the energy was reset to zero for that particular neuron (Figure 5.3.).

	1	2	3	4	5	6
1	0	0	0	0	0	0
2	0	0	1	0	0	0
3	0	1	1	1	0	0
4	0	0	1	0	0	0
5	0	0	0	0	0	0
6	0	0	0	0	0	0
7	0	0	0	0	0	0
8	0	0	0	0	0	0

Figure 5.3. Energy After First Propagation

The main difference from this method and the method purposed in the neural network paper [23] was that only the neighbors above, below, to the left, and to the right were allowed to propagate, not diagonal, and since energy wasn't used for the landscape, there was no additional energy deposited to the target after each iteration. This can be seen from the following equations:

$$up\_shift_{i,j} = M_{i,j} + M_{i,j-1}$$

$$down\_shift_{i,j} = M_{i,j} + M_{i,j+1}$$

$$left\_shift_{i,j} = M_{i,j} + M_{i+1,j}$$

$$right\_shift_{i,j} = M_{i,j} + M_{i-1,j}$$

$$M_{i,j} = up\_shift + down\_shift + left\_shift + right\_shift$$

Where:

M = The matrix

R = The number of rows in the matrix

C = The number of columns in the matrix

$1 < i < R$

$1 < j < C$

After the energy propagation, the elevation matrix added a one to itself for any node that contained energy (Figure 5.4.).

	1	2	3	4	5	6
1	0	0	0	0	0	0
2	0	0	1	0	0	0
3	0	1	2	1	0	0
4	0	0	1	0	0	0
5	0	0	0	0	0	0
6	0	0	0	0	0	0
7	0	0	0	0	0	0
8	0	0	0	0	0	0

Figure 5.4. Elevation of Figure 5.3

This process continued until a certain number of iterations had passed or until the energy had propagated from the target to the starting point (Figures 5.5.-5.6.).

	1	2	3	4	5	6
1	0	0	0	0	0	0
2	0	2.6264e+190	4.7396e+190	5.9674e+190	6.1764e+190	5.4956e+190
3	0	4.7396e+190	8.5123e+190	1.0622e+191	1.0829e+191	9.3976e+190
4	0	5.9674e+190	1.0622e+191	1.3028e+191	1.2888e+191	1.0604e+191
5	0	6.1764e+190	1.0829e+191	1.2888e+191	1.2055e+191	8.8670e+190
6	0	5.4956e+190	9.3975e+190	1.0604e+191	8.8670e+190	4.9135e+190
7	0	4.2609e+190	6.9888e+190	7.1208e+190	4.4297e+190	0
8	0	2.8941e+190	4.4451e+190	3.6774e+190	0	0

Figure 5.5. Final Energy

	1	2	3	4	5	6
1	0	0	0	0	0	0
2	0	289	290	289	288	287
3	0	290	291	290	289	288
4	0	289	290	289	288	287
5	0	288	289	288	287	286
6	0	287	288	287	286	285
7	0	286	287	286	285	0
8	0	285	286	285	0	0

Figure 5.6. Final Elevation

The target, which should have the largest value for gradient decent to work, is located at (3,3). Figure 5.6. has the largest value at the target at (3,3) but in Figure 5.5. the largest value is at (4,4) which is not the correct target which is why the landscape in Figure 5.6. had to be used instead of the energy. Iterations were used to prevent an infinite loop just in case there was no solution to the search space such as obstacles completely surrounding the target space preventing any movement to it.

5.2. RESULTS

The results of the simulations are illustrated in Figures 5.7.-5.15. These paths almost identically match those from the neural network paper [23] even though the weights, landscape, and propagation were different from the purposed method. Another

main difference was instead of plotting the path on the vertices of the grid they were plotted on the center of the free space squares. Each simulation took less than a second.

Propagating energy from the target to the starting point as purposed from Zhong et al. [23] did not always create a peak at the target in which case the path never traveled to the target. They added an additional amount to the target, but since the propagation expands exponentially, adding an additional amount did not solve the problem. Instead, the target had to be manually set once the propagation was done to have the most energy. Because energy is propagated from each neighbor, any neuron next to an obstacle (an unconnected neuron) did not receive as much energy from its neighbors. This was desired to keep the robot away from the obstacles but this also caused multiple peaks to form which the path would get stuck on and was also the reason why the target was not always the maximum point. No where in the paper did it state how their algorithm prevented these problems.

Using a separate landscape based on if any energy was present at each specific location was used instead. This method ensured the target was always at the maximum and that all the obstacles were minimums. Propagating in a square formation as in the replicated paper caused certain areas to not change in elevation for a few steps. When looking at the surrounding neighbors, it appeared that the neuron was a peak even though at least one neighbor had the same value. So instead of making a sloping elevation, it made a stair-like elevation. This could be fixed in the code where the robot always has to choose a new neuron to travel to, but in certain dynamic situations, it might be better for the robot to wait where it is instead of moving. Propagating in a cross fashion solved this problem by evenly disperse the elevation of the landscape which made it sloped. The

weights recommended were then used in the computing of the path instead of in propagating the energy even though some weights were also used in the propagation.

The modified neural network method purposed by this thesis can be seen in Figures 5.7.-5.15. Figures 5.7-5.9. show the path found using the new method for three different mazes. Figures 5.10.-5.15. contain elevations that correspond to the three different mazes. Table 5.1. displays the average and standard deviation for computational time and path lengths of each maze for five trials.
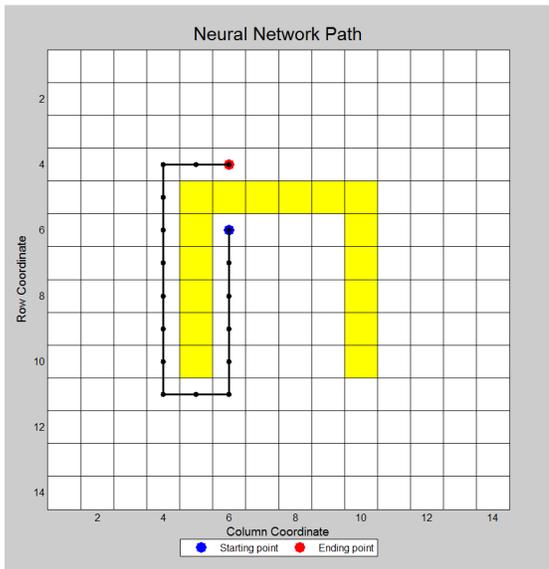
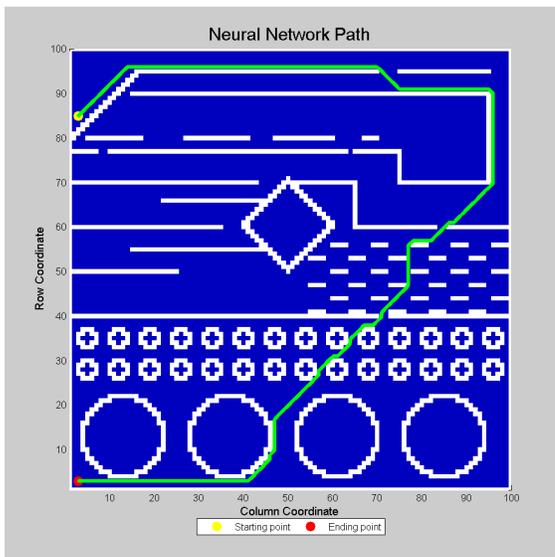Figure 5.7. First Maze
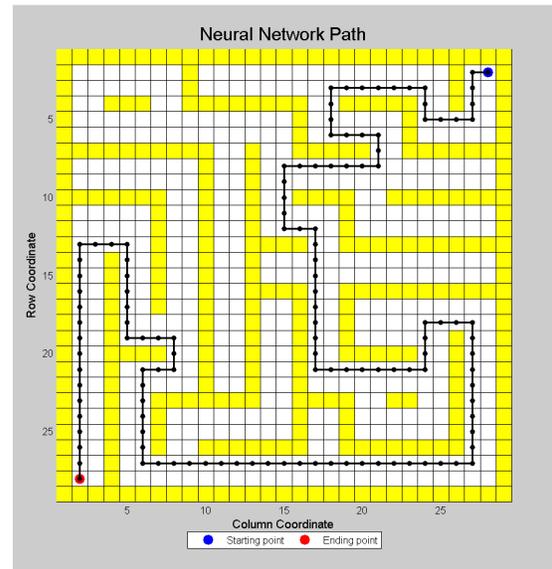
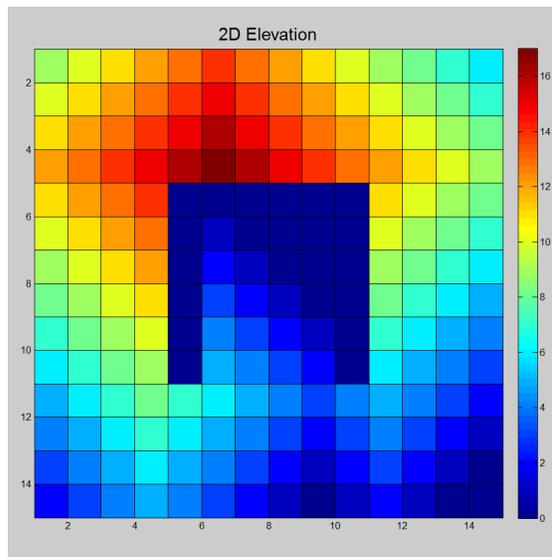Figure 5.8. Second Maze

Figure 5.9. Third Maze

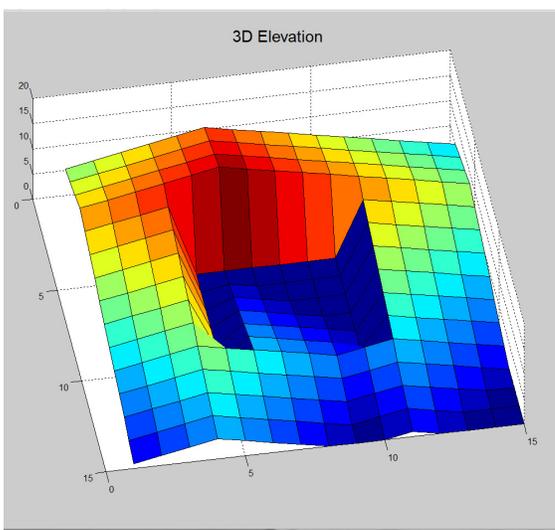Figure 5.10. First Maze 2D Elevation

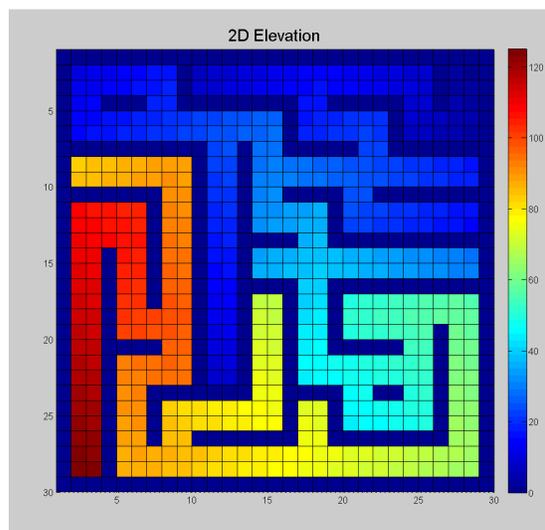Figure 5.11. First Maze 3D Elevation

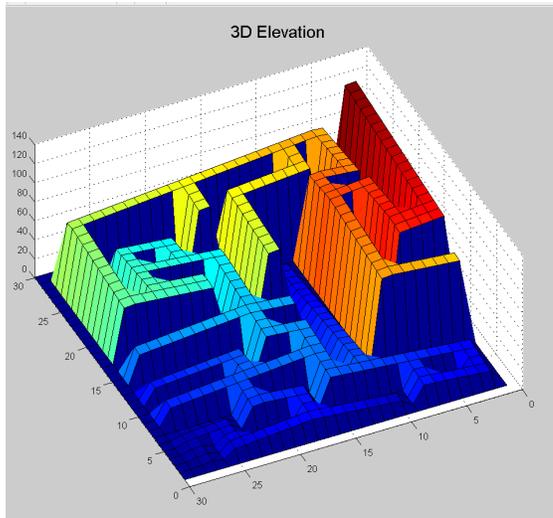Figure 5.12. Second Maze 2D Elevation
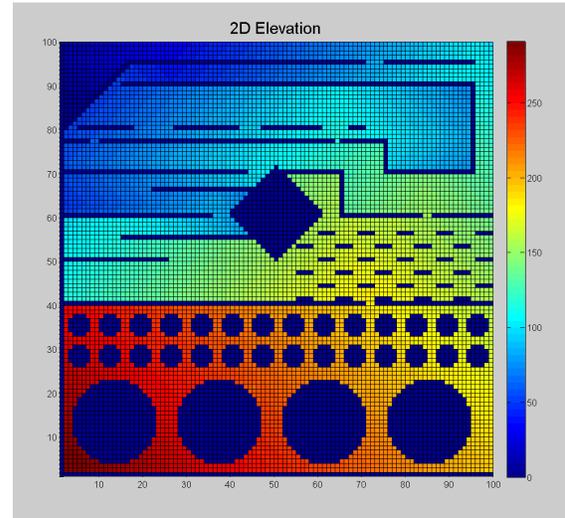
Figure 5.13. Second Maze 3D Elevation

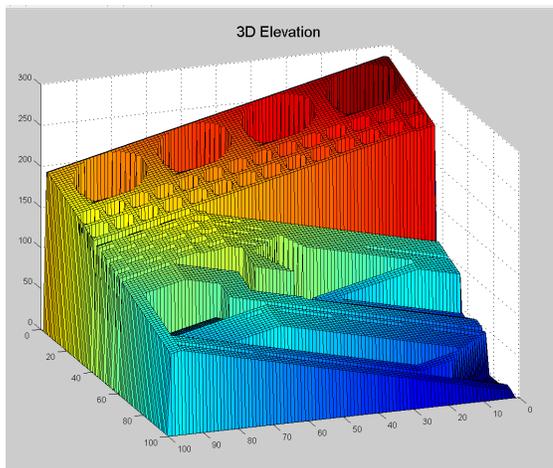Figure 5.14. Third Maze 2D Elevation

Figure 5.15. Third Maze 3D Elevation

Table 5.1. Neural Network Simulated Five Times Result

Name	Average Computational Time	Standard Deviation of Time	Average Path Length	Standard Deviation of Path Length
First Maze	0.8061 seconds	0.0134 seconds	16	0.0
Second Maze	0.9442 seconds	0.0790 seconds	124	0.0
Third Maze	1.2730 seconds	0.0558 seconds	252.51	0.0

5.3. CONCLUSION

By propagating energy through the connected neurons, a landscape was created in which the target was at the peak while the obstacles were at the bottom. Even though a different method was used in creating the landscape, propagating the energy, and using the weights, the results were very similar to what Zhong et al. [23] found. This is most likely because the overall idea of how the neural network is suppose to work by traveling up the gradient to the target since the target is the largest while the starting point is the smallest besides for obstacles was exactly the same. In their paper, they did not fully describe their process well enough for it to be replicated using the exact same method as them.

The neural network was able to solve each maze substantially faster than ACO. Even the path discovered was smoother and had a better result in terms of distance. Every path could be exactly replicated since there was no randomization or probabilities used. There were no parameters that needed to be optimized so the exact algorithm could be used on any path planning problem. Since the gradient decent method was used, the only way to modify the paths to become smoother would be to improve the elevation. The original method [23] was supposed to work on dynamic problems and keep a slight distance from all obstacles but the method actually employed will work only on static environments and has no distant requirement from obstacles as long as it does not collide with them. Since the elevation depends on the environment, modifying the elevation to get smoother paths would be difficult. As stated in the introduction, adding an extra biasing to the neural network could possibly solve this problem [24].

6. A* LITERATURE REVIEW

The A* algorithm was chosen for its popularity, its ability to find an optimal solution, and its use in navigation systems and video games [18-22]. A*'s ability for its paths to be replicated by constantly finding the optimal solution and for the search algorithm to be easily modified made this algorithm desirable for path planning. A*, however, will only work for static environments, environments that do not change, since all obstacles and costs need to be known.

A* is a combination of both an exhaustive search, guaranteed to find the optimal path but will typically require a large amount of computational time, and a greedy search, directs the search towards the goal and is generally faster but will not usually find the optimal solution [18-22]. The movement cost, a known cost from the starting point to get to its current location, is the exhaustive part. The heuristic, an estimation of the distance from its current location to the desired ending location, is the greedy part [18-22]. Since A* is a combination of each, the algorithm is guaranteed that an optimal path will be found and usually in a faster time than an exhaustive search.

There are numerous ways to calculate these costs. Which way works the best depends on the method of travel and the desired speed and accuracy of the algorithm. If only horizontal and vertical movements are allowed, the Manhattan Distance Formula should work the best for accuracy, but if movement in all directions is allowed, then the Euclidean Distance Formula would most likely be a better option [19-21]. Other methods and situations for choosing the correct heuristic are thoroughly covered by Amit [18]. A* without the heuristic part is known as Dijkstra's algorithm [18-20].

7. A* IMPLEMENTATION

7.1. BIRD'S EYE VIEW

A* consists of two lists, an open-list and a closed-list. The open-list contains a list of nodes that can currently be traveled to and the closed-list contains all the nodes already traveled to [18-22]. The typical version of A* checks all adjacent nodes from its current location and adds them to the open-list as long as they are not obstacles or already on the open or closed list. The movement cost is then calculated from its current location for all adjacent nodes that are free of obstacles. If this new movement cost is lower than the previous calculated one, then that becomes the new value for the movement cost and current node is remembered as the best way to get to that node. The following equation uses the Euclidean Distance Formula for calculating the movement cost.

$$G_n = G_c + \sqrt{(r_n - r_c)^2 + (c_n - c_c)^2}$$

Where:

- G_n movement cost of the adjacent node.

- G_c movement cost of the current node.

- r_n row coordinate of the adjacent node.

- r_c row coordinate of the current node.

- c_n column coordinate of the adjacent node.

- c_c column coordinate of the current node.

The heuristic cost will also be calculated but only for the adjacent nodes that are free of obstacles and where the heuristic has yet to be calculated since the heuristic cost will never change. The Euclidean Distance Formula was used in the following heuristic cost equation.

$$H_n = \sqrt{(r_f - r_n)^2 + (c_f - c_n)^2}$$

Where:

- H_n heuristic cost of the adjacent node.

- r_f row coordinate of the desired ending location.

- r_n row coordinate of the adjacent node.

- c_f column coordinate of the desired ending location.

- c_n column coordinate of the adjacent node.

The movement and heuristic costs are added together for each node on the open list, and the node with the lowest overall cost will become the new current node.

$$F_n = G_n + H_n$$

Where:

- F_n fitness cost of the adjacent node.

- G_n movement cost of the adjacent node.

- H_n heuristic cost of the adjacent node.

This process is repeated until the desired ending location is reached.

Instead of using the adjacent nodes, a bird's eye view was implemented. The bird's eye view was created by first checking the adjacent nodes for obstacles. If an obstacle was found in any of the adjacent nodes, then the original A* algorithm was used. However, if there are not any obstacles, then the unchecked adjacent nodes from the original adjacent nodes are checked. This square-formation expansion is continued until at least one obstacle is found and all nodes are checked from that square formation. The outer parameter nodes of this square are the only nodes added to the open-list. The rest of the A* algorithm works the same.

7.2. RESULTS

Using the bird's eye view method sometimes lowered the computational time required to find the shortest path but some mazes it also increased the time. It was also able to find a better path for certain mazes. These results can be seen from Figures 7.1-7.12 and Table 7.1. By having a larger viewing area for creating a path, allowed the paths to be more direct and even though not used in this thesis, provided knowledge if there was enough room for arc style turns to be used. The rest of the algorithm's searching procedure was the same as the original A*.
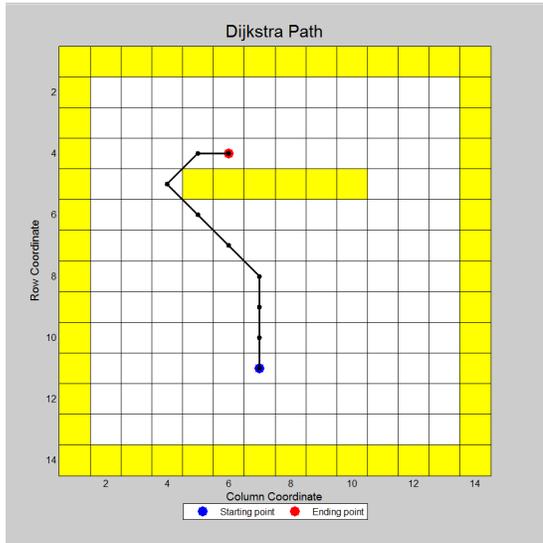
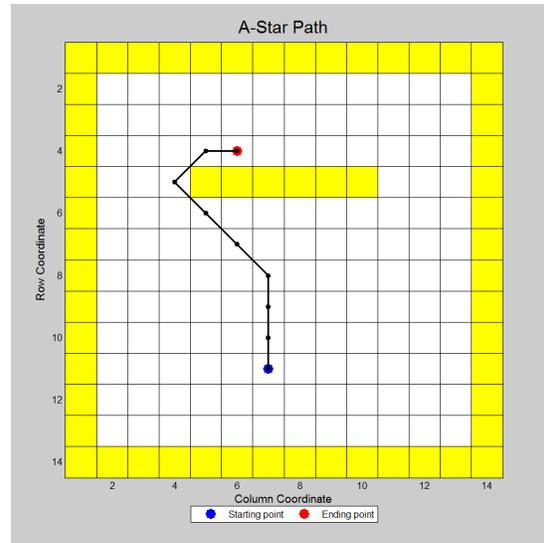Figure 7.1. Dijkstra's Test Maze
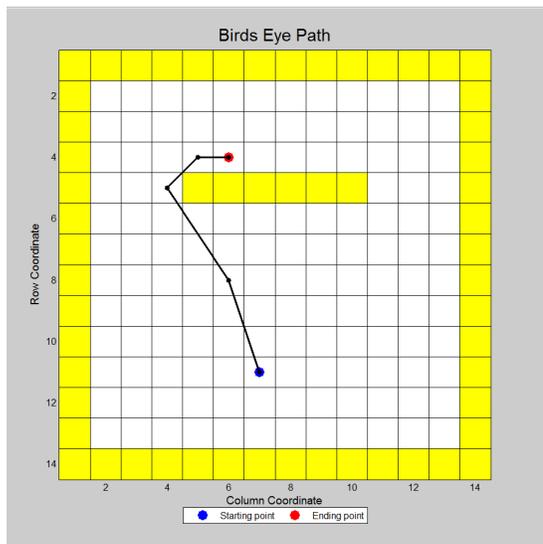

Figure 7.2. A* Test Maze

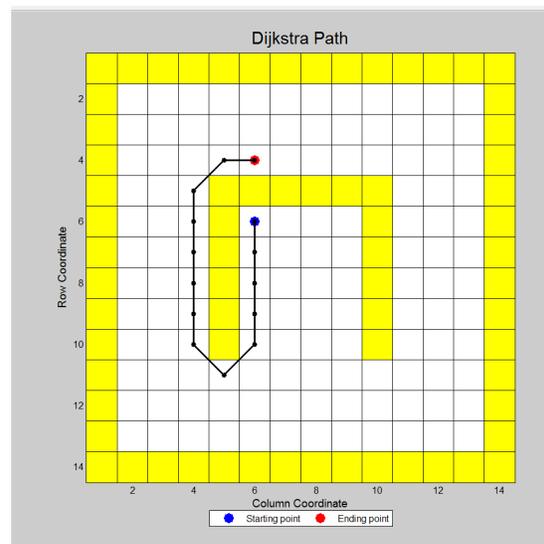Figure 7.3. A* W/ Bird's Eye Test Maze
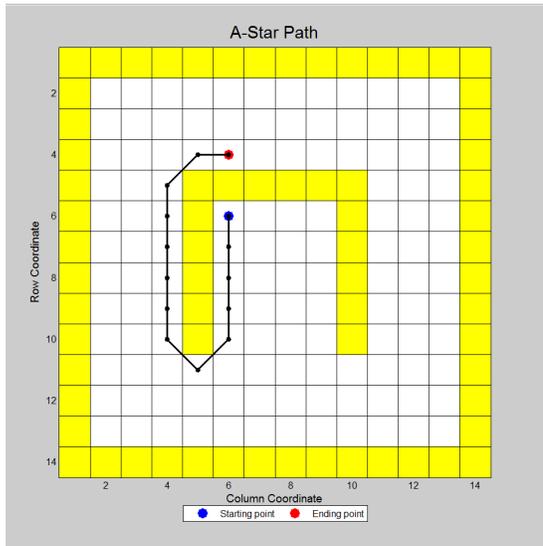

Figure 7.4. Dijkstra's First Maze
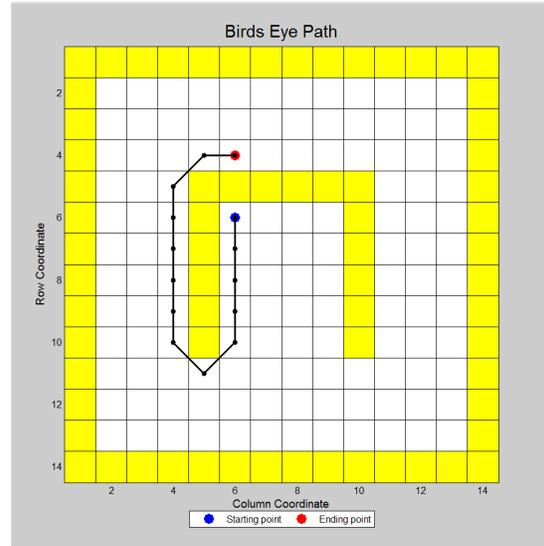
Figure 7.5. A* First Maze

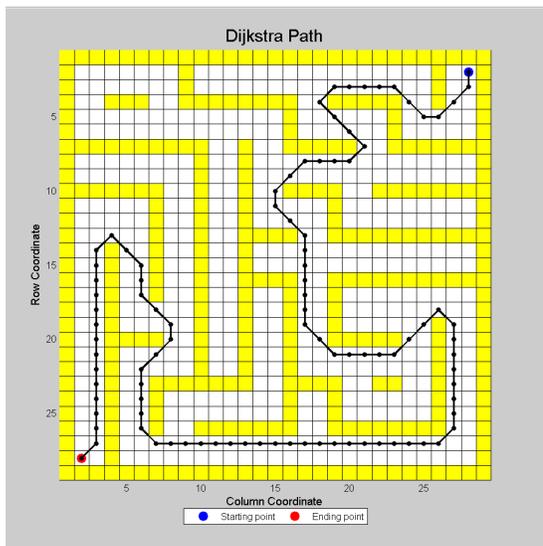Figure 7.6. A* W/ Bird's Eye First Maze

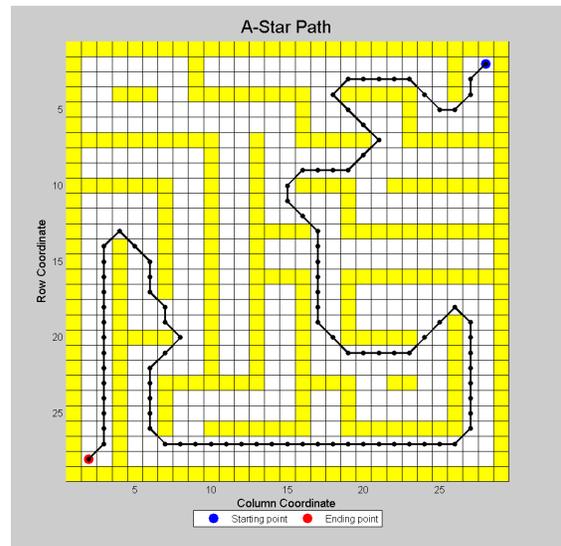Figure 7.7. Dijkstra's Second Maze
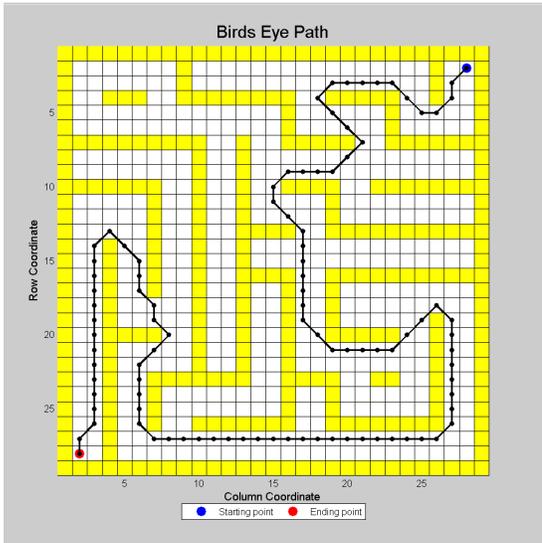

Figure 7.8. A* Second Maze
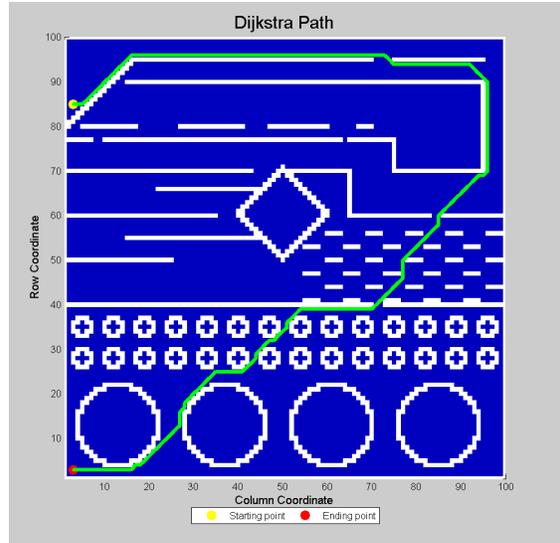
Figure 7.9. A* W/ Bird's Eye Second Maze

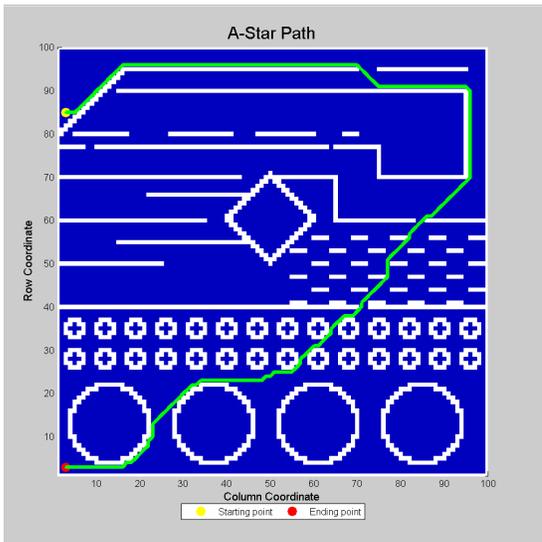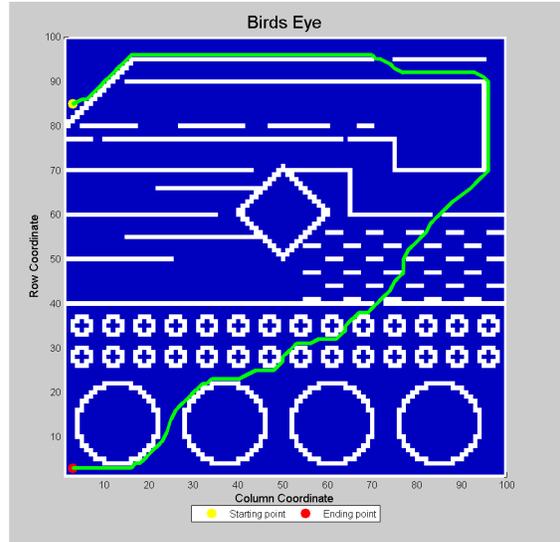Figure 7.10. Dijkstra's Third Maze

Figure 7.11. A* Third Maze

Figure 7.12. A* W/ Bird's Eye Third Maze

Table 7.1. A* Simulated Five Times Result

Name	Average Computational Time	Standard Deviation of Time	Average Path Length	Standard Deviation of Path Length
Dijkstra Test Maze	0.0348 seconds	0.0063 seconds	9.65685	0.0
A* Test Maze	0.0164 seconds	0.0087 seconds	9.65685	0.0
A* W/ Bird-Eye Test Maze	0.0136 seconds	0.0158 seconds	9.18204	0.0
Dijkstra First Maze	0.0230 seconds	0.0045 seconds	14.2426	0.0
A* First Maze	0.0142 seconds	0.0072 seconds	14.2426	0.0
A* W/ Bird-Eye First Maze	0.0224 seconds	0.0222 seconds	14.2426	0.0
Dijkstra Second Maze	0.2570 seconds	0.0208 seconds	107.012	0.0
A* Second Maze	0.2172 seconds	0.0119 seconds	107.012	0.0
A* W/ Bird-Eye Second Maze	0.2052 seconds	0.0171 seconds	107.012	0.0
Dijkstra Third Maze	25.4634 seconds	0.4297 seconds	247.823	0.0
A* Third Maze	10.4932 seconds	0.0206 seconds	247.823	0.0
A* W/ Bird-Eye Third Maze	15.9394 seconds	0.0845 seconds	245.191	0.0

7.3. CONCLUSION

Using a bird's eye view of the search space, attempted to improve the computational time of the A* algorithm, tried to create smoother paths, and made an effort to develop the ability of making arc turns. However, as the results showed, the computational time to discover the shortest path actually got worse for some mazes but did better for other ones. This was because the bird's eye view method requires more computational time to process all of the additional knowledge about the search space.

This computational time lost is usually made up by the fact that certain nodes can be skipped over which decreases the number of steps. Having less steps, can make the bird's eye view faster than the normal A* method. The bird's eye view had more computational time than A* for the mazes where steps were rarely skipped. The length of the path and creating a smoother path had similar results by improving for some mazes and other mazes there were no improvements. Once again, this performance improves if steps can be skipped. One change, that should help to improve the bird's eye method by allowing more steps to be skipped, is to change the view from a uniform square view to a more realistic view. Instead of expanding out until an obstacle is reached, it would work better if the expansion in that one particular direction stops while the other directions still expand until they reach an obstacle.

8. CONCLUSION

Even though Ant Colony Optimization can improve itself over time, the algorithm had too long of a computational time and found sub-optimal solutions. Not every ACO algorithm was tested but the ones that were tested (Ant System, Elitist Ant System, and Rank Based Ant System) typically had similar results. The algorithm could be modified but because of the parameters and randomization looking into neural networks seemed like a better solution.

The neural network did not have parameters or randomization and had a small computational time, but it still had problems of its own. The neural network could work in environments that changed over time, but when replicating the results from the literature [23], the algorithm got trapped in local minimas so a slight variant of the algorithm was used instead. This variation no longer got trapped but changed the algorithm where it could only be used for static environments. Due to the propagation and using gradient decent, the neural network could not easily be modified and this meant creating a method for smooth turning arcs would be difficult.

A* was the final algorithm tested. It had a similar performance to that of the neural network but was much easier to modify since its path was based on formulas instead of propagation. By adding a bird's eye view, a larger portion of the environment was known which helped to create a smoother, more direct path. With a few more tweaks to the algorithm, smoother paths with arc turns appear to be feasible.

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