A novel microwave method for detection of long surface cracks in metals

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A Novel Microwave Method for Detection of Long Surface Cracks in Metals

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Abstract—A novel microwave technique for detecting long surface cracks in metals is described. This technique utilizes an open-ended waveguide to probe the surface of a metal. In the absence of a crack the metal surface is seen as a relatively good short-circuit load. However, in the presence of a crack higher order modes are generated which in turn change the reflection properties at the waveguide aperture. This change brings about a perturbation in the standing wave characteristics which is then probed by a diode detector. The experimental and theoretical foundations of this technique are given, along with several examples. It is shown that cracks a fraction of a millimeter in width are easily detected at around 20 GHz or lower. Smaller cracks can be detected at higher microwave frequencies.

I. INTRODUCTION

Metal fatigue or failure usually begins from the surface. Aircraft fuselage, nuclear power plant steam generator tubing, and steel bridges are examples of environments in which this type of metal failure occurs. Hence, fatigue and stress crack detection on metallic structures is of utmost importance to the on-line and in-service inspections of metallic components. Currently there are several prominent nondestructive testing (NDT) techniques for detecting surface cracks in metals; however, each method possesses certain limitations and disadvantages. In some environments the technique used may not be an optimum one, but the only one that can be applied. Acoustic emission testing, dye penetrant testing, eddy current testing, ultrasonic testing, radiographic testing, and magnetic particle testing are examples of these techniques [1].

Since the late sixties there have been several researchers who have attempted using microwaves for surface crack detection on metals, with modest success. Microwave techniques offer certain advantages, when detecting hairline stress or fatigue cracks, such as: the sensor may or may not be in contact with the surface under examination; they are applicable in high-temperature environments; the crack may be filled with dielectric materials such as dirt, paint or rust; or the surface of the metal may be covered with paint or a similar compound and the crack may still be detected. Finally polarization properties of microwaves can provide information regarding relative crack orientation. Microwaves have also shown the potential of estimating crack width, depth and length. Feinstein et al. [2]–[4] used a mode conversion technique based on the idea that the crack converts a portion of the incident wave to an orthogonally polarized wave. This noncontact technique utilizes a microwave bridge for nulling out background signals, and a microwave rotary joint for producing incident waves of different polarizations. They were able to detect cracks with widths of 0.05 mm and different depths. The drawbacks of this technique are the introduction of the additional loss associated with the microwave bridge and the low-frequency mechanical modulation associated with the rotary joint. Bahar [5] used a similar technique at 100 GHz. He used mode conversion without polarization modulation. To separate the orthogonally polarized wave from the copolarized backscattered wave an orthomode coupler was utilized. To increase the spatial resolution of the measurement apparatus, he used a focusing lens on a horn antenna to create a beamwidth equivalent to 3.5 mm at the focal point. The integrity of this approach was checked by examining 0.25 mm wide cracks on aluminum plates. He showed that at high enough frequencies, the depth of a crack may also be determined. The disadvantage of this method is that detection is directly dependent on the degree of decoupling between the orthogonally polarized signals created by the mode conversion in the crack. He also used circularly polarized signals and a dielectric waveguide to improve detection sensitivity such that fatigue cracks under loading were detected [6]. Other microwave approaches have included microstrip planar lines and ferromagnetic resonance probes for crack detection [7]–[14].

This paper describes a new and simpler microwave technique for detecting long and straight surface cracks using an open-ended waveguide. The experimental and theoretical foundations of this technique along with several results are described.

II. APPROACH

A. Experimental Foundation

In mid-1992 several experiments, using an open-ended waveguide, were conducted to investigate the feasibility of using this probe to detect long surface cracks in metals. In this context, long refers to a crack whose length is greater than or equal to the broad dimension of a waveguide. Various long cracks of different widths and depths were milled on top of flat metal sheets. Preliminary experiments were conducted by moving (using a computer-controlled stepping motor) the cracked metal surface over the aperture of the open-ended waveguide while monitoring the standing-wave characteristics inside the waveguide. Subsequently, it was observed that when
the crack axis (length) is parallel to the broad dimension of the waveguide (orthogonal to the electric field of the dominant \(TE_{10}\) mode) the standing wave experiences a pronounced shift in location when the crack is exposed to the aperture of the waveguide compared to when the crack is outside the aperture (a short-circuit condition). This shift indicates changes in the reflection coefficient properties of the metal surface perturbed by the crack. It was also observed that this shift is highly dependent on the relative location of the crack within the waveguide aperture (i.e., whether the crack is at the edge or at the center of the aperture). Fig. 1 shows the geometry of a crack with width \(W\), depth \(d\), and length \(L\) and a waveguide aperture with dimensions \(a\) and \(b\), when the crack length is parallel to the broad dimension of the waveguide, and \(\delta\) is a dimension indicating the location of the crack relative to an arbitrary location on the small dimension of the waveguide aperture, \(b\). It was also observed that when the crack was not parallel to the broad dimension of the waveguide, the level of change in the standing wave decreased, and when the crack became parallel to the smaller dimension of the waveguide (parallel to the dominant \(TE_{10}\) mode electric field) there was no measurable perturbation in the characteristics of the standing wave. This is due to the fact that in this case the surface currents on the metal surface are parallel to the crack length which does not disturb the surface currents. It must be noted here that most fatigue and stress cracks in real life are not straight. However, they can usually be considered fairly straight along their lengths.

Fig. 2 shows a simple measurement apparatus that was used for these experiments. An oscillator feeds a (slotted) waveguide terminated by a metal plate in which there is a crack. Placing the diode detector a distance \(l\) away from the waveguide aperture, the metal plate can be scanned by the waveguide aperture and the standing voltage recorded. As will be seen later, different detector locations, \(l\), will change the difference between the measured signals for the short-circuit case and when the crack is in the middle of the aperture. If \(l\) is chosen such that the detector is located between a maximum and a minimum on the standing wave pattern, this difference is maximized.

At 24 GHz, a long crack with \(L > 10.7\) mm, \(W = 0.84\) mm, and \(d = 1.03\) mm was scanned over the aperture of a \(K\)-band waveguide (\(a = 16.67\) mm and \(b = 4.32\) mm). The diode output voltage measured at \(l = 9.45\) cm is shown in Fig. 3 (the solid line). The results indicate that while the crack is outside the waveguide aperture the diode registers very little voltage variation due to the fact that the waveguide is terminated by a short circuit. The noise-like feature associated with the signal is due to the quantization resolution of the A/D converter and the internal noise of the voltmeter. As the crack begins to appear within the waveguide aperture the voltage experiences a rapid magnitude change which is an indication of rapid phase change in the reflection coefficient at the aperture. The same phenomenon occurs when the crack leaves the waveguide aperture. The voltage value does not change very much while the crack is inside the aperture; however, its value is still different than that of a short-circuit case. The diode output voltage as a function of \(\delta\) (here on referred to as the crack characteristics signal) is clearly an indication of the presence of a crack (detection), since the absence of the crack results in a fairly constant voltage.

**B. Theoretical Foundation**

To theoretically model this phenomenon an effort was made to simplify the geometry of the crack with respect to the waveguide. It was decided to investigate the effect of crack length on the characteristic signals. The idea was that
if the length of the crack is approximated to be equal to
the broad dimension of the waveguide aperture, \(a\), then the
problem could be modeled as a large waveguide feeding a
much narrower short-circuited waveguide with the same broad
dimension. Subsequently, an experiment was conducted in
which a crack with the same width and depth as those used
for the solid line in Fig. 3 but with \(L = 10.7\) mm (equal to
the broad dimension of the waveguide) was used to determine
its characteristic signal at 24 GHz. The dashed line in Fig. 3
shows the results of this experiment. Comparing the solid and
the dashed line clearly indicates that, for thin cracks (small
\(W\)), once the length extends beyond the waveguide aperture
there will not be any considerable perturbation in the standing-
wave pattern. Thus, in the subsequent theoretical derivations
we can assume that the length of a crack is equal to the broad
dimension of the waveguide, \(a\). The slight widening of the
characteristic signal at around \(d = 2.5\) mm for the long crack
(solid line) is attributed to a small amount of radiation through
the long crack. This problem becomes much less important as
the width of a crack becomes small which is the case for
many fatigue cracks.

Fig. 4 shows the relative geometry of a crack with respect
to the waveguide aperture and the coordinate system used for
the modeling. The crack dimension is \(W \times d \times a\), and \(W\)
extends from \(c\) to \(c'\) in the \(y\) direction. The dominant mode
propagating in the \(+z\) direction is incident upon the waveguide
aperture. The reflected wave propagates in the \(-z\) direction,
and a standing wave is formed inside the waveguide. The
properties of the standing wave are influenced by the crack size
and its location within the waveguide aperture. The reflected
wave arises as a direct consequence of forcing the boundary
conditions inside and outside the crack at all times. Only those
field components used to force the boundary conditions are
listed below.

The dominant TE\(_{10}\) mode in the waveguide is the incident
wave whose electric and magnetic fields are given by [15]

\[
E_{TE}^i = \sin \frac{\pi x}{a} e^{-j\beta_1 z} \quad (1)
\]

\[
H_{TE}^i = -\frac{1}{\eta_1} \sin \frac{\pi x}{a} e^{-j\beta_1 z} \quad (2)
\]

where

\[
\beta_1 = \sqrt{k_0^2 - \left(\frac{\pi}{a}\right)^2}, \quad k_0 = \frac{2\pi}{\lambda_0}, \quad \eta_1 = \frac{k_0 \mu_0}{\beta_1}, \quad \eta_0 = \sqrt{\frac{\mu_0}{\varepsilon_0}}
\]

and where \(\lambda_0, k_0, \mu_0, \eta_0\) are the free-space wavelength,
wave number, permittivity and permeability, respectively. \(\eta_1\)
and \(\mu_0\) are the free-space and waveguide intrinsic impedances,
respectively. In the presence of a crack the electric field
bends around the crack, and consequently generates an infinite
number of higher order TM modes. Thus, the reflected wave in
the waveguide, due to the crack, consists of the reflected TE\(_{10}\)
mode (since the crack length and waveguide broad dimension
are assumed equal) given by

\[
E_{yTE}^r = A_{10} \sin \frac{\pi x}{a} e^{-j\beta_1 z} \quad (3)
\]

\[
H_{xTE}^r = A_{10} \eta_1^{-1} \sin \frac{\pi x}{a} e^{-j\beta_1 z}. \quad (4)
\]

The reflected TM modes are given by

\[
E_{yTM}^r = \sum_{m=1}^{\infty} A_{1m} \sin \frac{\pi x}{a} \cos \frac{m\pi y}{b} e^{-j\beta_m z} \quad (5)
\]

\[
H_{xTM}^r = \sum_{m=1}^{\infty} A_{1m} \eta_1^{-1} \sin \frac{\pi x}{a} \cos \frac{m\pi y}{b} e^{-j\beta_m z} \quad (6)
\]

where \(A_{10}\) and \(A_{1m}\) \((m = 1, 2, 3, \ldots)\) are unknown coeffi-
cients to be determined and

\[
\beta_m = \sqrt{k_0^2 - \left(\frac{\pi}{a}\right)^2 - \left(\frac{m\pi}{b}\right)^2}, \quad \eta_1 = \frac{\beta_m^2 \eta_0}{k_0}
\]

The waves in the crack consist of forward and reflected TE\(_{10}\)
modes given by

\[
E_{yTE} = (B_{10} e^{j\beta_1 z} + C_{10} e^{-j\beta_1 z}) \sin \frac{\pi x}{a} \quad (7)
\]

\[
H_{xTE} = \frac{1}{\eta_1} (-B_{10} e^{j\beta_1 z} + C_{10} e^{-j\beta_1 z}) \sin \frac{\pi x}{a} \quad (8)
\]

and forward and reflected TM modes given by

\[
E_{yTM} = \sum_{m=1}^{\infty} \left( B_{1m} e^{j\beta_m z} + C_{1m} e^{-j\beta_m z} \right) \sin \frac{\pi x}{a} \cos \frac{m\pi (y-c)}{W} \quad (9)
\]

\[
H_{xTM} = \sum_{m=1}^{\infty} \left( -B_{1m} e^{j\beta_m z} + C_{1m} e^{-j\beta_m z} \right) \sin \frac{\pi x}{a} \cos \frac{m\pi (y-c)}{W} \quad (10)
\]

where \(B_{10}, C_{10}, B_{1m}, C_{1m}\) \((m = 1, 2, 3, \ldots)\) are coeffi-
cients to be determined. \(W\), which is the crack width, is equal
Forcing the appropriate boundary conditions renders the unknown coefficients.

C. Boundary Conditions

The boundary conditions between the waveguide and the crack apertures can be summarized by two cases. Case 1 is when the crack is fully within the waveguide aperture, and case 2 is when the crack is partially within the waveguide aperture as shown in Fig. 4(a) and (b), respectively.

1) Crack Fully Within the Aperture: When the crack is fully within the waveguide aperture as shown in Fig. 4(a), \(0 < c < b - W\), the following boundary conditions must be satisfied for areas 1 and 2:

\[
\begin{align*}
(E_y)_{\text{guide}} &= 0 \quad \text{for } 0 < x < a, \quad 0 < y < c \text{ or } c' < y \leq b, \quad z = 0 \\
(H_z)_{\text{guide}} &= (H_z)_{\text{crack}}, \quad 0 < x < a, \quad c < y \leq c', \quad z = 0
\end{align*}
\]

and for area 3:

\[
(E_y)_{\text{guide}} = (E_y)_{\text{crack}} = 0 \quad \text{for } 0 < x < a, \quad c < y < c', \quad z = 0
\]

and finally for area 4:

\[
(E_y)_{\text{crack}} = 0 \quad \text{for } 0 < x < a, \quad c < y < 0, \quad z = d
\]

2) Crack Partially Within the Aperture: When the crack is at the lower edge of the waveguide aperture as shown in Fig. 4(b), \((-W < c \leq 0\), for areas 1, 3, and 4 similar boundary conditions as above must be satisfied and for area 2:

\[
(E_y)_{\text{crack}} = 0 \quad \text{for } 0 < x < a, \quad c < y < 0, \quad z = d
\]

When the crack is at the upper edge of the waveguide aperture \((b - W < c \leq b)\) the boundary conditions will be identical to those stated here.

D. Unknown Coefficients

Forcing the boundary conditions for case 1 (crack fully within the waveguide aperture) renders the following equations which, once simultaneously solved, the unknown coefficients and hence the field distribution at any point inside the waveguide can be determined as \(c\) varies between 0 and \((b - W)\):

\[
A_{10} + 1 = \frac{W}{b} (1 - e^{-j2\beta_1 d}) B_{10}
\]

\[
A_{10} - 1 + \sum_{m' = 1}^{\infty} h(0, m') A_{1m'} = -B_{10} (1 + e^{-j2\beta_1 d})
\]

\[
A_{1m} = -f(m) B_{10} + \sum_{m' = 1}^{\infty} b(m, m') A_{1m'} \quad m = 1, 2, 3, \ldots
\]

where

\[
h(0, m') = \frac{m b}{W \pi} \frac{1}{m' \eta_{1m'}} \left( \frac{m' \pi c'}{b} - \sin \frac{m' \pi c}{b} \right)
\]

\[
p(m, n) = \frac{m(-1)^n}{b \pi} \left( \frac{m' \pi c}{b} - \sin \frac{m' \pi c}{b} \right) \quad n = 1, 2, 3, \ldots
\]

\[
b(m, m') = -\frac{4}{b W \eta_{1m'}^b} \sum_{n = 1}^{\infty} \eta_{1m'}^b (1 - e^{-j2\beta_1 d}) \frac{1 + e^{-j2\beta_1 d}}{1 + e^{-j2\beta_1 d}} p(m, n) p(m', n)
\]

\[
f(m) = \frac{2}{m \pi} (e^{-j2\beta_1 d} - 1) \left( \frac{m' \pi c}{b} - \sin \frac{m' \pi c}{b} \right)
\]

Similarly, by forcing the boundary conditions for case 2 the following equations are obtained. Once these equations are simultaneously solved the field expressions anywhere inside the waveguide can be obtained as \(c\) varies between \((-W)\) and 0 (or \(b - W\) and \(b\)):

\[
A_{1m} = B_{10} \frac{2}{m \pi} (1 - e^{-j2\beta_1 d}) \sin \frac{m' \pi c'}{b}
\]

\[
+ \sum_{n = 1}^{\infty} \frac{2 B_{1n}}{b} (1 - e^{-j2\beta_1 d}) \sin \frac{m' \pi c}{b}
\]

\[
B_{1n} = \frac{1}{1 - e^{-j2\beta_1 d}} (1 + A_{10}) \frac{2}{m \pi} \sin \frac{m' \pi c}{b}
\]

\[
+ \frac{2}{W} \sum_{n = 1}^{\infty} A_{1m} R(m, n)
\]

\[
R(m, n) = \frac{0.5}{(b + W \pi) \pi} \left[ (-1)^n \sin \frac{m' \pi c}{b} + \sin \frac{m' \pi c}{b} \right] + \frac{0.5}{(b - W \pi) \pi} \left[ (-1)^n \sin \frac{m' \pi c}{b} - \sin \frac{m' \pi c}{b} \right]
\]

Having obtained the electric field distribution anywhere inside the waveguide, \(E_y\) can be calculated at \((x = a/2\) and \(z = \ell\) which simulates the diode detector location. Thus, one can simulate the measurements by calculating \(|E_y|^2\) assuming the...
diode detector is operating in its square-law region. Using the expressions for the incident and the reflected waves, one may also calculate the phase of the reflection coefficient at the aperture. Although the summations in (5), (6), (9) and (10) extend to infinity, in reality the number of required modes are finite and dependent on the crack dimensions and location within the waveguide aperture. This number increases when the crack size decreases and particularly when the crack is at the edge of the waveguide aperture. In the latter case more than a hundred modes may be required to satisfy the boundary conditions.

E. Comparison of the Theoretical and Experimental Results

To compare the results of the theoretical derivations with experimental results, $|E_{y}|^2$ for a crack with $W = 0.84$ mm and $d = 1.53$ mm was calculated at $\ell = 9.45$ cm away from the aperture (between a standing-wave null and maximum) at 24 GHz. Fig. 5 shows the normalized (with respect to the maximum value of each signal) results of the diode output voltage for the experimental case and $|E_{y}|^2$ for the theoretical case. The agreement between the two results is very good. The slight difference between the normalized signal levels is attributed primarily to the crack geometry not having 90° corners as assumed by the theory, and a small airgap present between the metal surface and the waveguide aperture during the measurements. The diode detector may not always operate in the square-law region (particularly for high input signal values) which may also attribute to this difference. The distance between the arrows marked 1 is equal to the width of the crack plus the small dimension of the waveguide ($W + b$). However, due to the causes mentioned above, experimentally the distance between the arrows marked 2 is approximated by ($W + b$). Our experiments have shown that the error associated with measuring a thin crack width in this manner is less than 10% if the airgap is kept to a minimum. Therefore, the characteristic signal can be used to estimate crack width reasonably accurately.

Fig. 6 shows the calculated standing-wave pattern inside the waveguide, as a function of $\ell$, for a short circuit and when the above crack is at the center of the aperture ($y = h/2$). The shift in the standing-wave pattern that was mentioned earlier is apparent. It is also evident that if the diode detector were at locations 1 and 3 there would be a minimal amount of signal (voltage) difference between the short-circuit and the crack-terminated cases. However, when the diode detector probes the standing wave at location 2 there will be a maximum signal (voltage) difference between the two cases.

Fig. 7 shows the characteristic signals for a long crack with $W = 0.277$ mm and two depths of 0.96 mm and 1.488 mm at 24 GHz. The results of these experiments indicate that the distance between the voltage reversals remains unchanged since this distance is primarily a function of the crack widths. However, the signal magnitudes in the middle of the aperture are different and once calibrated may serve as an estimator of crack depth.

Fig. 8(a) shows the calculated electric field distribution, $|E_{y}|(V/m)$, on a cracked metal surface with $W = 0.1$ mm and $d = 1$ mm at $y = h/2$ and three different locations on the $x$-axis at 90 GHz ($a = 2.54$ mm and $b = 1.27$ mm). As expected, the electric field at the center is maximum and diminishes towards the waveguide walls. Fig. 8(b) shows the same information at 10 GHz. It is evident that the same 100-micron wide crack is seen as a much wider perturbation on the metal plate at 90 GHz, as expected. Also note that the relative magnitude of the electric field is much smaller at 10 GHz than that at 90 GHz. At X-band the small crack is much further beyond cutoff. This type of theoretical simulation can be used to check, ahead of time, the feasibility of using a certain frequency range for detecting cracks with various width ranges.

As mentioned earlier, the ability to know the electric and magnetic field characteristics anywhere inside the waveguide not only renders information about the field magnitudes, but also about their phases. Fig. 9 shows the phase of the reflection...
crack dimensions. This method may be used in environments such as aerospace, nuclear power plants, etc.

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REFERENCES


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